

$$(11+3!+5!+...+25!)(2!+4!+6!+...+24!)$$

$$1+4=5$$

$$24$$

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$$24 \times 5 \rightarrow 120$$

$$\int \frac{1}{x+\sqrt{x}} (1+\sqrt{x})^2 = \int \frac{(x-\sqrt{x}) \times (1+2\sqrt{x})}{9} = \int \frac{(x-\sqrt{x})(1+\sqrt{x})^2}{9} \cdot 2$$

$$\int \frac{(14-\sqrt{x})^2}{2} - 4\sqrt{x}$$

$$\text{ب) } \frac{(\sqrt{2}+\sqrt{5})(\sqrt{10}-2)}{\sqrt{10}+2(\sqrt{10}-2)} = \frac{2\sqrt{2}}{4} = \frac{\sqrt{2}}{2} \left(\sqrt{3-\sqrt{5}} - \sqrt{3+\sqrt{5}} \right)$$

$$\frac{\sqrt{4-2\sqrt{5}} - \sqrt{4+2\sqrt{5}}}{2} = \frac{(\sqrt{5}-1)^2 - (\sqrt{5}+1)^2}{2}$$

$$\frac{\sqrt{5}-1 - \sqrt{5}-1}{2} = -1$$

$$\text{الف) } \frac{(2\sqrt{2}+3\sqrt{3})(5+\sqrt{4})}{(5-\sqrt{4})(5+\sqrt{4})} = \frac{10\sqrt{2}+15\sqrt{3}+6\sqrt{2}+9\sqrt{3}}{19} = \frac{16(\sqrt{2}+\sqrt{3})}{19} = \sqrt{2+\sqrt{3}}$$

$$-2(\sqrt{3}-1)^{-1} = 2 \left(\frac{\sqrt{3}+1}{(\sqrt{3}-1)(\sqrt{3}+1)} \right) = -\sqrt{3}-1$$

$$-\sqrt{3}-1 + \sqrt{2}+\sqrt{3} = \sqrt{2}-1$$

$$\text{ب) } \frac{2\sqrt{3}-1}{(2+\sqrt{3})(2-\sqrt{3})} = \frac{13\sqrt{3}-13}{13} = \sqrt{3}-1$$

$$\frac{1}{2-\sqrt{3}} \times \frac{(2+\sqrt{3})}{(2+\sqrt{3})} = 2+\sqrt{3}$$

$$\frac{2+\sqrt{3}}{2-\sqrt{3}} = \sqrt{3}+1$$

$$1) \left(\sqrt{1+\sqrt{2}} \right) \left(\sqrt{2+\sqrt{2}} \right) + \left(\sqrt{1-\sqrt{2}} \right) \left(\sqrt{2+\sqrt{2}} \right) \quad : 2\sqrt{2}$$

$$1 = \frac{\sqrt{2+\sqrt{2}}}{\sqrt{2+\sqrt{2}}}$$

$$\left(\sqrt{\underbrace{1+\sqrt{2}}_a} + \sqrt{\underbrace{2+\sqrt{2}}_b} + \sqrt{\underbrace{1-\sqrt{2}}_a} - \sqrt{\underbrace{2+\sqrt{2}}_b} \right)^2 = \left(\sqrt{a+b} + \sqrt{a-b} \right)^2$$

$$2a + 2\sqrt{a^2 - b^2}$$

$$2(1+\sqrt{2}) + 2\sqrt{(1+\sqrt{2})^2 - (2+\sqrt{2})^2}$$

$$4 + 2\sqrt{2} + 2\sqrt{1 + 2\sqrt{2} + 2 - 4 - 4\sqrt{2} - 2} = 4 + 2\sqrt{2} - 2\sqrt{1 + 2\sqrt{2}}$$

$$10 + 4\sqrt{2} \Rightarrow \sqrt{10 + 4\sqrt{2}} = \sqrt{4 + 2} - \sqrt{4 + 2} - 2 = \sqrt{4}$$

$$\sqrt[12]{2^1} \times \sqrt[12]{1 \times 2} \times \sqrt[12]{2^{12}} = \sqrt[12]{2^{13}} = 2^1 \times 2^1 = 4$$

$$\rightarrow a=1, 4, 2^2 \rightarrow S_2 = \left(\frac{1^4-1}{1} \right) = 0 \quad : 0$$

$$2^n (1 + 2 + 2^2 + 2^3 + 2^4 + 2^5)$$

$$2^n \left(\frac{1}{2} + \frac{1}{2} + 1 + 2 + 4 + 8 \right)$$

$$\Rightarrow \frac{2^n}{2^n} = \frac{2^n}{2^n} = \frac{1}{2} \Rightarrow \sqrt{2}$$

$$S_2 = \frac{1}{2} \left(\frac{1^4-1}{1} \right) = \frac{0}{2}$$

$$\left((a+b)^2 \right)^2 \left((a-b)^2 \right)^2 (a^2-b^2)^2$$

$$\sqrt{4-2} = a^2, b^2 = \sqrt{4+2} \Rightarrow (a^2-b^2)^2 = (\sqrt{4-2})^2 + (\sqrt{4+2})^2 + 2\sqrt{4-2}\sqrt{4+2}$$

$$(2\sqrt{4-2} - 2\sqrt{4+2})^2 = 16 - 16\sqrt{2} = 16(1-\sqrt{2})$$

$$\Rightarrow (a^2-b^2)^2 = 16$$

$$a \pm \sqrt{v - \sqrt{r}} = \sqrt{v} \pm \sqrt{r-1}$$

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$$\left(a + \frac{1}{a} + (\sqrt{r})\right)^2 \left(a + \frac{1}{a} - (\sqrt{r})\right)^2 = \left(\left(a + \frac{1}{a} + r\right) - r\right)^2$$

$$\frac{1}{a^2} + a^2 + r = \frac{1}{v - \sqrt{r}} + v - \sqrt{r} + r + v + \sqrt{r} + v - \sqrt{r} + r = 14$$

$$r^2 = 14 \Rightarrow \boxed{r = 2\sqrt{14}}$$

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$$A = \int \sqrt{x} \sqrt{14} = \sqrt{r} \cdot \sqrt{r} = r$$

$$\left(\frac{1}{r}\right)^{\frac{1}{2}} \cdot \left(r\right)^{\frac{1}{2}} = \sqrt{r} \cdot \sqrt{r}$$

$$(rA)^{\frac{1}{2}} = \left(\frac{1}{r}\right)^{\frac{1}{2}} \cdot \sqrt{r} = \frac{1}{r}$$

$$a^{\frac{1}{v}} \cdot r \cdot v \cdot a^{\frac{1}{v}} \Rightarrow a^{\frac{1+1}{v}} \cdot r \cdot v \Rightarrow \frac{1}{a^r} \cdot r \cdot v \Rightarrow \frac{1}{a} \cdot 2\sqrt{r} \cdot v$$

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$$\frac{1}{a} - r \cdot 2\sqrt{r} - r \rightarrow \frac{(r\sqrt{r} - r)(\sqrt{r} - 1)}{(\sqrt{r} + 1)(\sqrt{r} - 1)} = \frac{r(\sqrt{r} - 1)^2}{r}$$

$$r(\sqrt{r} - 1)^2 (r - r\sqrt{r}) = 12 - 4\sqrt{r} \Rightarrow \frac{r(4 - r\sqrt{r})}{r} = \boxed{4 - r\sqrt{r}}$$

$$\sqrt{n+a} = u \quad \left\{ \begin{array}{l} u^2 - v^2 = (u+v)(u-v) \\ \sqrt{n-a} = v \end{array} \right. \quad \left\{ \begin{array}{l} n+a = (u+v) \\ n-a = (u-v) \end{array} \right. \Rightarrow \left(\sqrt{n+a} + \sqrt{n-a} \right) \left(\sqrt{n+a} - \sqrt{n-a} \right) = r$$

$$\sqrt{n+a} + \sqrt{n-a} = \frac{a+r}{r} \Rightarrow \frac{a}{r} + r \Rightarrow \frac{a}{r} + r - r = \boxed{\frac{a}{r}}$$