

الف) $3x - y = 9 \Rightarrow 3x - 2y = 18$
 $x + 2y = -6 \Rightarrow x + 2y = -6 \Rightarrow \begin{cases} 3x - 2y = 18 \\ x + 2y = -6 \end{cases} \Rightarrow \begin{cases} 4x = 12 \\ x = 3, y = -3 \end{cases}$

ب) $\frac{1}{x} - \frac{1}{y} = -1 \Rightarrow \frac{y-x}{xy} = -1 \Rightarrow y-x+xy=0$
 $\frac{2}{x} - \frac{3}{y} = -3 \Rightarrow \frac{2y-3x}{xy} = -3 \Rightarrow 2y-3x+3xy=0$

$f = \{(a, 2a), (1, a+1), (1, -2), (2, b)\}$ $f(a) + 2f(2) = 3f(1)$

$2a + 2b = 2a + 3$ $3(1) + 2(-2) = 3(a+1) \Rightarrow 3 - 4 = 3a + 3 \Rightarrow a = -2$

$-4 + 2b = -4$

$2b = 0 \Rightarrow b = 0$

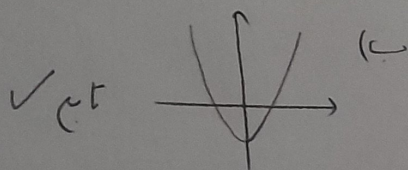
$f = \{(-1, m^2-2m), (3, 5), (-1, -2), (m+1, 4), (3, 4), (m^2+2, 5m+1)\}$

$m^2 - 2m = -2 \Rightarrow m^2 - 2m + 2 = 0$
 $(m-1)(m-2) = 0 \Rightarrow \begin{cases} m=1 \text{ } \alpha \\ m=2 \text{ } \alpha \end{cases}$

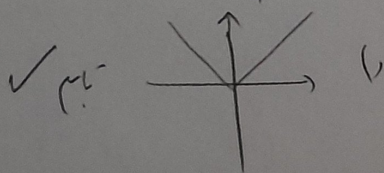
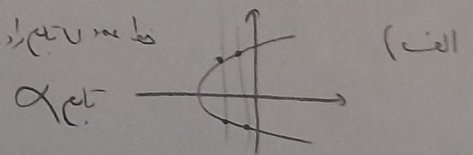
$m=2 \Rightarrow \{(1, -2), (3, 5), (-1, -2), (3, 4), (6, 9)\}$
 (توجه: $(3, 4)$ و $(6, 9)$ نیز قابل قبول است)

$m=1 \Rightarrow \{(-1, -2), (3, 5), (-1, -2), (2, 4), (3, 4), (3, 5)\}$
 (توجه: $(-1, -2)$ و $(3, 5)$ نیز قابل قبول است)

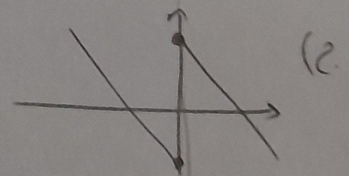
به ازای هیچ مقدار m



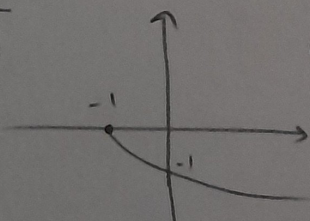
خط $m=1$ و $m=2$ را در نمودار نشان دهید.



ب) α به دلیل (الف)



الف) $y = -\sqrt{x+1}$



ب) α

ب) $x = \frac{y}{\sqrt{1-y^2}}$

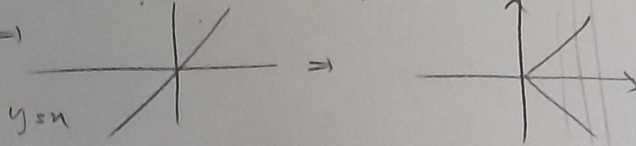
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ب) $|y| = n \Rightarrow$  \Rightarrow $\frac{1}{n}$

6

$$f(n) = \frac{n^r + \epsilon n + a}{n^r + \epsilon n + v} \Rightarrow \frac{(n+r)^r + 1}{(n+r)^r + \mu} \xrightarrow{f(\sqrt{\mu-r})} \frac{(\sqrt{\mu-r+r})^r + 1}{(\sqrt{\mu-r+r})^r + \mu} \Rightarrow \frac{\epsilon}{\mu} = \left(\frac{\mu}{\mu}\right)$$

7

$$y = \mu n + a \leq 0 \xrightarrow{(-b, -c)} -c + \mu + a \leq 0 \rightarrow a \leq 1$$

$$f(n) = \mu n + n + b \xrightarrow{(-b, -c)} -c \leq -1 - 1 + b \Rightarrow b \leq -2$$

$$y = \mu n - 1 \Rightarrow n^r + n - \mu n - 1 \rightarrow n^r - \mu n - 1 \leq 0 \Rightarrow$$

8

$$f = \left\{ (r, a-b), (b, ra), (-1, a-rb+1) \right\}$$

$$a+b = ra = a-rb+1$$

$$\underbrace{a+b}_{a=b} \Rightarrow \underbrace{ra}_{-a+1=ra} \Rightarrow ra \leq 1, \left(a \leq \frac{1}{\mu} \right)$$

9

$$f(n) = \frac{\mu n - an + \epsilon + 1}{bn + \mu} \Rightarrow c \leq 1$$

$$\boxed{a+b+c \leq 0}$$

$$f(n) \Rightarrow \frac{n(\epsilon n - a)}{bn + \mu} \Rightarrow b = \epsilon, a = -\mu$$

10