

$$ax^2 - a^2x + b$$

$$1 < a < 3$$

$$a + b = 9$$

$$1 + 3 = \frac{-(a)}{1}$$

$$a = 4$$

$$3 \times 1 = \frac{b}{1} \quad \boxed{b = 5}$$

$$a + b \rightarrow \boxed{4 + 5 = 9}$$

$$(x - 2m)^2 ((k-2)x + m-1)$$

$$-1 - 2m = 0$$

$$2m = -1$$

$$m = -\frac{1}{2}$$

$$f(k-1) + m-1 = 0 \quad f(k-m-1) = 0$$

$$k - m - 1 = 0 \quad m = 1 - k$$

از $k-2 < 0 \rightarrow k < 2 \rightarrow k=1$

$$(-\frac{1}{2}x^2 + 2x + 6) > \frac{1}{2}x^2$$

$$-1x^2 + 4x + 12 > 1x^2$$

$$-2x^2 + 4x + 12 > 0$$

$$-(2x^2 - 4x - 12) > 0$$

$$-\Delta < 0 \rightarrow \text{همواره}$$

$$x^3 - 3x^2 - x + 3 = 0 \quad (x^3 - 3x^2) - (x - 3) = 0$$

$$x^2(x-3) - (x-3) = 0 \quad (x^2-1)(x-3) = 0 \quad (x-1)(x+1)(x-3) = 0$$

$$\frac{-1 \pm \sqrt{1+3}}{-2 \pm 2} \rightarrow x > 0 \quad f(x) < 0 \Rightarrow (1, 3)$$

$$f(2) = 1 - 12 - 2 + 3 = \boxed{-6}$$

$$(a-1)x^2 + (a-1)x + 1 < 0 \quad \frac{-(a-1)}{2(a-1)} = -\frac{1}{2} \quad a-1 > 0 \rightarrow a < 1$$

$$f(\max x) = (a-1) \times \frac{1}{2} - \frac{a-1}{4} + 1 = 1 - \frac{a-1}{4} < 0 \quad f - (a-1) < 0$$

$$-a + 1 < 0 \quad a > 1$$

$$(a > 1) \cap (a < 1) \rightarrow \emptyset$$

$$\frac{m(m^p+m)}{m-p} \geq 0 \Rightarrow \frac{m^p(m^p+1)}{m-p} \geq 0 \quad m \neq \pm 1$$

$\begin{array}{c} -1 & 0 & 1 & p \\ \hline - & + & - & + \end{array}$

$m \in (-1, 1) \cup (p, +\infty)$

$$\frac{(x-1)(x+1)(x-1)^p}{(x+1)(1-x)^p} \leq 0$$

$\begin{array}{c} -1 & 1 & p & p \\ \hline - & + & - & + \end{array}$

$(-\infty, -1] \cup (1, p]$

$\Delta < 0 \rightarrow$ always true

$p-x=0 \Rightarrow x=p$

$$\frac{px^p - px}{x^p + p} < p \quad \frac{px^p - px - p(x^p + p)}{x^p + p} < 0 \quad \frac{x^p - px - 1}{x^p + p} < 0$$

$$\frac{(x-p)(x+p)}{x^p + p} < 0 \quad \begin{array}{c} -p & p \\ \hline + & - \end{array} \rightarrow (p, p)$$

$p - (-p) = \boxed{2}$

$\rightarrow x^p \neq -p \rightarrow$ always true

$$\frac{px^p - px}{x+1} > -1 \quad \frac{px^p - px}{x+1} < 0 \quad \frac{x(px^p - p)}{x+1} < 0$$

$\begin{array}{c} -1 & 1 & p \\ \hline - & + & - \end{array}$

$(-1, \frac{p}{p+1})$

$\Delta = b^2 - 4ac \rightarrow 9 - 4 \rightarrow \Delta < 0 \rightarrow$ always true

$$\frac{x^p - 10}{x} \leq p \quad x^p - 10 \leq px \quad x^p - px - 10 \leq 0 \quad (x-1)(x+1) \leq 0$$

$\begin{array}{c} -1 & 1 \\ \hline + & - \end{array}$

$x \in [1, 1]$