

در برای a

$$\begin{aligned} x^r + rx &= ax - r \\ a^r + ra &= ar - r \\ ra &= -r \\ \boxed{a} &= \boxed{-1} \end{aligned}$$

$f(x) = \frac{x^r + a}{rx - b}$, $g(x) = rx + b$

$$\frac{x^r + a}{rx - b} = rx + b \xrightarrow{\begin{matrix} |r \\ |r \end{matrix}} \frac{r+a}{r-b} = r+b \Rightarrow r+a = r-b^r$$

$$\left. \begin{aligned} f+a &= 1a \\ \boxed{a} &= \boxed{1} \end{aligned} \right\} f(x) = \frac{x^r + 1}{rx + 1} \rightarrow f(1) = \frac{1^r}{r} = \frac{1}{r}$$

$$g(x) = rx + b \xrightarrow{\begin{matrix} r \\ -1 \end{matrix}} \begin{aligned} r &= r+b \\ \boxed{-1} &= \boxed{b} \end{aligned}$$

$f(x) = \frac{rx + 1}{rx^2 + ax + b}$, $D_f = \mathbb{R} - \{-1, 1\}$, $f(1) = ?$

$rx^2 + ax + b \neq 0$, $r - a + b = 0 \rightarrow r + 1 + b = 0$, $rx + a + b = 0 \rightarrow r + a + b = 0$, $rx + a = 0 \rightarrow \boxed{a} = \boxed{-r}$

$$f(x) = \frac{rx + 1}{rx^2 - rx - 1} \rightarrow f(1) = \frac{-1}{-1-1} = \frac{1}{2}$$

$f(x) = \frac{x^r - \sqrt{r}}{-rx^2 + ax + b}$, $\mathbb{R} - \{1\}$

$$\begin{aligned} -rx^2 + ax + b &= 0 \\ x = \frac{-b}{ra} = \frac{-a}{-1} = \frac{a}{1} = 1 &\rightarrow \boxed{a} = \boxed{1} \\ -r + a + b &= 0 \rightarrow \boxed{b} = \boxed{-r} \end{aligned}$$

$f(x) = \frac{rx}{(x-1)(x^r + mx + 1)}$, $\mathbb{R} - \{1\}$

$$\Delta = m^r - r \rightarrow \begin{cases} m^r - r = 0 \\ m^r = r \end{cases} \rightarrow m = \sqrt[r]{r}$$

$\rightarrow \{m \mid r - m \in [-r, r]\}$

$f(x) = \sqrt{r - \frac{1}{x^r}}$, $r - \frac{1}{x^r} \geq 0$, $x \neq 0$, $D_f = (-\infty, -\frac{1}{r}] \cup [\frac{1}{r}, +\infty)$

$$\left(\frac{1}{x}\right)^{\frac{1}{r}} \left(r - \frac{1}{x}\right) \geq 0 \rightarrow \frac{1}{x} \left(r - \frac{1}{x}\right) \geq 0$$

$f(x) = \sqrt{mx^r + rx + 1}$, $mx^r + rx + 1 \geq 0$, $m > 0$, $\Delta \leq 0 \Rightarrow \begin{cases} 4m^2 - 4m \leq 0 \\ m(m-1) \leq 0 \end{cases}$, $m \in [0, 1]$

$x = \frac{1}{r} \rightarrow g(x) = f(x)$, $r = r + k$, $\boxed{0} = \boxed{k}$, $a + k = \frac{1}{r} + 0 = \frac{1}{r}$

$D_g = \mathbb{R} \rightarrow D_f = \mathbb{R} \Rightarrow \boxed{a} = \boxed{\frac{1}{r}}$

$$g(x) = rx + b$$

$$\left. \begin{array}{l} a=1 \\ r=r \end{array} \right\} a-b = -1$$

$$\begin{aligned} \underline{x = -\frac{r}{r}} \rightarrow rx + b &= rax + r \\ -r + b &= -ra + r \end{aligned}$$

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$$x = r \rightarrow x + r = rar + ax$$

$$r = rar + ra \quad \frac{r}{r}$$

$$r = a^r + a - r$$

$$r = \underbrace{(a-1)}_{(1)} \underbrace{(a+r)}_{(-r)}$$