

19 آفرین!

آینه عطا الله

$$f(x) = \sqrt{4-x^2} = I \quad x^2 \leq 4 \quad II \quad 4-x^2 \geq 0 \quad x \geq \sqrt{4-x^2}$$

$$f(x) = \sqrt{3-\sqrt{x^2-2}} = I \quad x^2-2 \geq 0 \quad x \geq 2 \quad II \quad 3-\sqrt{x^2-2} \geq 0$$

$$x^2 \geq \sqrt{x^2-2} \quad 9 \geq x^2-2 \quad x \geq 2 \quad Df = [2, \infty)$$

$$x \geq \sqrt{4-x^2} \quad 14 \geq 2-2x \quad x \geq -14$$

$$Df = [-14, 2]$$

1, 75
81x

$$f(x) = \sqrt{4-2x^2} = 4-2x^2 \geq 0 \quad x^2 \leq 2 \quad \sqrt{2} \leq x \leq \sqrt{2}$$

$$Df = [-\sqrt{2}, \sqrt{2}]$$

$$f(x) = \sqrt{3|x|+9} = 3|x|+9 \geq 0 \quad x \geq 0$$

$$Df = (-\infty, 0] \cup [3, +\infty)$$

2: 14

$$f(x) = \sqrt{\frac{|x|+1}{|x|-3}} = |x| \neq 3 \quad x \neq \pm 3$$

$$f(x) = \sqrt{\frac{\sqrt{x}+1}{\sqrt{x}-3}} = Df = \mathbb{R} \setminus \{\pm 3\}$$

$$Df = [0, 3) \cup (3, +\infty)$$

$$f(x) = \sqrt{\frac{3-|x|}{|x|+2}} \quad I \quad 3-|x| \geq 0 \quad x \leq 3 \quad II \quad |x|+2 \neq 0$$

$$Df = [-3, 3]$$

$$f(x) = \sqrt{\frac{4-x^2}{|x|-1}} \quad I \quad 4-x^2 \geq 0 \quad x \leq 2 \quad II \quad |x|-1 \neq 0 \quad x \neq \pm 1$$

$$Df = [2, 2] \cup (-1, 1) \cup (1, 2]$$

$$f(x) = \frac{x+1}{\sqrt{x^2+|x|}} = Df = \mathbb{R}^+ \quad f(x) = \frac{1}{\sqrt{x|x|}} \quad x|x| > 0 \quad Df = \mathbb{R}^+$$

$$f(x) = \sqrt{2-[x]} = 2-[x] \geq 0 \quad x \geq [x] \quad Df = (-\infty, 3]$$

$$2-[x] > 0 \quad 2 > [x] \quad 2 > x \quad Df = (-\infty, 2)$$

$$f(x) = \frac{1}{x[x]} = x[x] \neq 0 \quad Df = \mathbb{R} \setminus \{0\}$$

$$f(x) = \frac{1}{\sqrt{-x[x]}} = -x[x] > 0 \quad Df = \emptyset$$

$$[x] \neq 0 \rightarrow Df = \mathbb{R} \setminus [0, 1)$$

1, 0

$$a) y = \sqrt{\left[x - \frac{1}{p}\right] + \left[x + \frac{p}{p}\right]} = \left[x - \frac{1}{p}\right] + \left[x + \frac{p}{p}\right] \geq 0 \xrightarrow{+1} \left[x + \frac{p}{p}\right] + \left[x + \frac{p}{p}\right] \geq 1$$

$$x + \frac{p}{p} \geq 1 \quad x \geq \frac{1}{p} \quad D_f = \left[\frac{1}{p}, +\infty\right)$$

$$b) y = \sqrt{\left[x - \frac{1}{p}\right] + \left[-x + \frac{1}{p}\right]} = \text{if } \begin{cases} a \in \mathbb{Z} & [a] + [-a] = 0 \\ a \notin \mathbb{Z} & [a] + [-a] = -1 \end{cases} \Rightarrow D_f = \left\{x \mid x = k + \frac{1}{p}, k \in \mathbb{Z}\right\}$$

$$a) y = \frac{1}{p \sin x - 1} \quad D_f = \mathbb{R} - \left\{\frac{k\pi}{p} + \frac{\pi}{2}\right\}$$

$$p \sin x - 1 \neq 0 \quad \sin x \neq \frac{1}{p} \quad \sin x \geq \frac{1}{p} \Rightarrow \frac{\sqrt{1 - \frac{1}{p^2}}}{\sqrt{p}} = \frac{1}{p} \Rightarrow \frac{1}{p} \leq \sin x \leq 1$$

$$b) y = \frac{\cot x + 1}{\tan x + 1} \quad \tan x + 1 \neq 0 \quad \tan x \neq -1 \quad D_f = \mathbb{R} - \left\{k\pi - \frac{\pi}{4}, k\pi, k\pi - \frac{\pi}{2}\right\}$$

$$a) y = \sqrt{p \sin x - 1} = p \sin x - 1 \geq 0$$

$$p \sin x \geq 1 \quad \sin x \geq \frac{1}{p} \quad -1 \leq \sin x \leq 1$$

$$b) y = \sqrt{1 - p \cos x} = 1 - p \cos x \geq 0$$

$$1 \geq p \cos x \quad \frac{1}{p} \geq \cos x \quad -1 \leq \cos x \leq 1$$

$$D_f = \left[k\pi + \frac{\pi}{2}, k\pi + \frac{3\pi}{2}\right]$$

$$D_f = \left[k\pi + \frac{\pi}{p}, k\pi + \frac{3\pi}{p}\right]$$