

$$y = \frac{n+1}{\sqrt{n+|n|}} = n+|n| > 0 \rightarrow n > 0 \rightarrow |n| = n \quad (2) \quad (a)$$

$$Df = [0, +\infty)$$

$$n+|n| = n+n = 2n > 0$$

$$n > 0$$

$$n < 0 \rightarrow |n| = -n$$

$$n+|n| = n-n = 0 \quad \text{بازگشت به صفر}$$

$$y = \frac{1}{\sqrt{n|n|}} \rightarrow n|n| > 0 \rightarrow n > 0 \quad |n| = n$$

$$D = (0, +\infty)$$

$$n|n| = n^2 > 0$$

فقط اعداد مثبت بزرگتر از صفر

$$y = \sqrt{2-[n]} = 2-[n] \geq 0 \quad [n] \leq 2 \quad [n] = 2 \rightarrow 2 \leq n < 3 \quad (6)$$

$$[n] = 1 \rightarrow 1 \leq n < 2 \quad (2)$$

$$Df = (-\infty, 2)$$

$$y = \frac{1}{\sqrt{2-[n]}} \rightarrow 2-[n] > 0 \quad [n] < 2 \quad [n] = 1 \rightarrow 1 \leq n < 2$$

$$Df = (-\infty, 2)$$

$$[n] = 0 \rightarrow 0 \leq n < 1$$

$$y = \frac{1}{n[n]} \rightarrow n[n] \neq 0 \rightarrow n < 0 \rightarrow [n] \leq -1$$

$$n \geq 1 \rightarrow [n] \geq 1$$

$$(1, 5)$$

$$Df = (-\infty, 0) \cup [1, +\infty)$$

همه اعداد صحیح بجز 0 و 1

$$y = \frac{1}{\sqrt{-n[n]}} \rightarrow -n[n] > 0 \quad \text{غیر ممکن!}$$

$n, [n]$ هم‌علامه نیستند

$$Df = (-\infty, 0)$$

$$Df = \emptyset$$

$$[n + \frac{1}{n}] \geq \frac{1}{n} \rightarrow n + \frac{1}{n} \geq 1 \quad n \geq \frac{1}{n} \quad Df = [\frac{1}{n}, +\infty)$$

$$y = \sqrt{[n - \frac{1}{n}] + [n + \frac{1}{n}]} = y = \sqrt{2[n] + \frac{1}{n}} \rightarrow 2[n] + \frac{1}{n} \geq 0 \quad (1)$$

$$2[n] \geq -\frac{1}{n} \rightarrow [n] \geq -\frac{1}{2} \rightarrow Df = [0, +\infty)$$

$$n \geq 0$$

$$y = \sqrt{[n - \frac{1}{n}] + [-n + \frac{1}{n}]} \rightarrow [n - \frac{1}{n}] + [-n + \frac{1}{n}] \geq 0 \quad Df = [-\frac{1}{n}, -\frac{1}{n}]$$

$$Df = \{n | n = k + \frac{1}{k}, k \in \mathbb{Z}\}$$

$$y = \frac{1}{r \sin^2 \alpha - 1} \quad r \sin^2 \alpha - 1 \neq 0 \quad (9)$$

$$r \sin^2 \alpha = 1 \rightarrow \sin \alpha = \frac{1}{r}$$

$$\sin \alpha = \pm \frac{\sqrt{r}}{r}$$

$$\sin \alpha = \frac{\sqrt{r}}{r} \rightarrow \frac{\pi}{r} + 2k\pi$$

$$D = R - \left\{ \alpha = \frac{\pi}{r} + \frac{k\pi}{r}, k \in \mathbb{Z} \right\}$$

$$\sin \alpha = -\frac{\sqrt{r}}{r} \rightarrow -\frac{\pi}{r} + 2k\pi$$

$$y = \frac{\cot \alpha + 1}{\tan \alpha + 1} \rightarrow \tan \alpha + 1 \neq 0 \quad \tan \alpha \neq -1$$

$$\tan \alpha \neq -1 \rightarrow \alpha = -\frac{\pi}{r} + k\pi$$

$$D \neq R - \left\{ k\pi, \frac{\pi}{r} + k\pi, -\frac{\pi}{r} + k\pi \mid k \in \mathbb{Z} \right\}$$

$$y = \sqrt{r \sin \alpha - 1} \rightarrow r \sin \alpha - 1 \geq 0$$

$$\sin \alpha \geq \frac{1}{r}$$

$$D = \left\{ \frac{\pi}{r} + 2k\pi, \frac{2\pi}{r} + 2k\pi \right\} \cup k \in \mathbb{Z}$$

$$y = \sqrt{1 - r \cos \alpha} = 1 - r \cos \alpha \geq 0 \quad \cos \alpha \leq \frac{1}{r}$$

$$\alpha \in \left[\frac{\pi}{r}, 2\pi - \frac{\pi}{r} \right] = \frac{\pi}{r}, \frac{2\pi}{r} \quad \alpha \in \left[\frac{\pi}{r} + 2k\pi, \frac{2\pi}{r} + 2k\pi \right]$$

$$D \neq k \in \mathbb{Z} \cup \left[\frac{\pi}{r} + 2k\pi, \frac{2\pi}{r} + 2k\pi \right]$$