

الف) $y = \sqrt{x - \sqrt{x-2}}$ $x-2 \geq 0 \Rightarrow x \geq 2$ $x - \sqrt{x-2} \geq 0 \Rightarrow \sqrt{x-2} \leq x-2$
 $x-2 \leq 1 \Rightarrow x \leq 3$ $\Rightarrow x \in [2, 3]$ $D_f = [2, 3]$ ✓

ب) $y = \sqrt{x - \sqrt{x-2}}$ $x-2 \geq 0 \Rightarrow x \geq 2$ $x - \sqrt{x-2} \geq 0 \Rightarrow \sqrt{x-2} \leq x-2$
 $x-2 \leq 9 \Rightarrow x \leq 11$ $\Rightarrow x \in [2, 11]$ $D_f = [2, 11]$ ✓

الف) $y = \sqrt{x-2}$ $x-2 \geq 0 \Rightarrow x \geq 2$ $D_f = [2, +\infty)$ ✓

ب) $y = \sqrt{x-2}$ $x-2 \geq 0 \Rightarrow x \geq 2$ $D_f = (-\infty, -2] \cup [2, +\infty)$ ✓

الف) $y = \sqrt{\frac{x+1}{x-2}}$ $x-2 \neq 0 \Rightarrow x \neq 2$ $D_f = \mathbb{R} - \{2\}$ ✓

ب) $y = \sqrt{\frac{x+1}{x-2}}$ $x-2 \neq 0 \Rightarrow x \neq 2$ $D_f = \mathbb{R} - \{2\}$
 $\sqrt{x} \rightarrow x \geq 0 \Rightarrow D_f = [0, +\infty) - \{2\}$

الف) $y = \sqrt{\frac{x-2}{x+2}}$ $x+2 \neq 0 \Rightarrow x \neq -2$ $D_f = [-2, 2]$ ✓

ب) $y = \sqrt{\frac{x-2}{x+2}}$ $x+2 \neq 0 \Rightarrow x \neq -2$ $D_f = [-2, 2] - \{-2\}$ ✓

الف) $y = \frac{x+1}{\sqrt{x+1}}$ $x+1 \geq 0 \Rightarrow x \geq -1$ $D_f = [0, +\infty) \subset \mathbb{R}^+$ ✓

ب) $y = \frac{1}{\sqrt{x+1}}$ $x+1 \geq 0 \Rightarrow x \geq -1$ $D_f = [0, +\infty) \subset \mathbb{R}^+$ ✓

الف) $y = \sqrt{r-x}$ $r-x \geq 0 \Rightarrow -x \geq -r \Rightarrow x \leq r$ $\frac{0}{r}$ $D_f = (-\infty, r)$

ب) $y = \frac{1}{\sqrt{r-x}}$ $r-x > 0 \Rightarrow -x > -r \Rightarrow x < r$ $D_f = (-\infty, r)$

$y = \frac{1}{x[x]}$ $x[x] \neq 0 \Rightarrow x \neq 0 \Rightarrow (0, 1)$ $D_f = \mathbb{R} - [0, 1)$

ب) $y = \frac{1}{\sqrt{-x[x]}}$ $-x[x] > 0$ $D_f = \emptyset$

برای x و $x[x]$ هم علامت هستند و آن یکی از آن ها مثبت نشوند برای همینه
یا صفر یا منفی می شوند بنابراین این عبارت $-x[x]$ تخریب نشده می باشد.

الف) $y = \sqrt{[x-\frac{1}{p}] + [x+\frac{r}{p}]}$ $[x-\frac{1}{p}] + [x+\frac{r}{p}] \geq 0 \Rightarrow [x+\frac{r}{p}-\frac{1}{p}-1] + [x+\frac{r}{p}] \geq 0 \Rightarrow [x+\frac{r}{p}-1][x+\frac{r}{p}] \geq 0$
 $[x+\frac{r}{p}]-1 + [x+\frac{r}{p}] \geq 0 \Rightarrow r[x+\frac{r}{p}] \geq 1 \Rightarrow [x+\frac{r}{p}] \geq \frac{1}{r} \Rightarrow x+\frac{r}{p} \geq \frac{1}{r} \Rightarrow x \geq \frac{1}{p}$ $D_f = [\frac{1}{p}, +\infty)$

ب) $y = \sqrt{\frac{[x-\frac{1}{p}] + [x+\frac{1}{p}]}{a}}$ $\frac{[x-\frac{1}{p}] + [x+\frac{1}{p}]}{a} \geq 0 \Rightarrow \frac{-(x-\frac{1}{p})}{-a} \geq 0 \Rightarrow x - \frac{1}{p} \in \mathbb{Z}$
 $D_f = \{x \mid x = k + \frac{1}{p}, k \in \mathbb{Z}\}$

الف) $y = \frac{1}{r \sin^r x - 1}$ $r \sin^r x - 1 \neq 0 \Rightarrow r \sin^r x \neq 1 \Rightarrow \sin^r x \neq \frac{1}{r}$ $\sin^r x \neq \pm (\frac{1}{r})^{\frac{1}{r}}$ $D_f = \mathbb{R} - \{k\pi \pm \frac{\pi}{r}\}$

ب) $\frac{\cot x + 1}{\tan x + 1}$ $\frac{\cos x + 1}{\sin x}$ $\frac{\sin x}{\cos x} x + 1$ $\sin x \neq 0$ $\cos x \neq 0$ $\tan x + 1 \neq 0 \Rightarrow \tan x \neq -1 \Rightarrow \tan x \neq k\pi - \frac{\pi}{4}$ $D_f = \mathbb{R} - \{k\pi, k\pi + \frac{\pi}{4}, k\pi - \frac{\pi}{4}\}$

الف) $y = \sqrt{r \sin x - 1}$ $r \sin x - 1 \geq 0 \Rightarrow \sin x \geq \frac{1}{r}$ $D_f = [r\pi + \frac{\pi}{4}, r\pi + \frac{3\pi}{4}]$

ب) $y = \sqrt{1 - \cos x}$ $1 - \cos x \geq 0 \Rightarrow -\cos x \geq -1 \Rightarrow \cos x \leq 1$ $D_f = \mathbb{R} - \{r\pi \pm \frac{\pi}{2}\}$
 $D_f \subset \mathbb{R} - [r\pi + \frac{\pi}{2}, r\pi + \frac{3\pi}{2}]$