

۱۹۲۵ تیر ۱۳۵۷

الف) $\sqrt{4-\sqrt{2}x}$ $2-x \geq 0$ $2 \geq x$ $D_f = [-14, 2]$
 $4-\sqrt{2}x \geq 0$ $4 \geq \sqrt{2}x \Rightarrow 14 \geq 2-x$ $x \geq -14$

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ب) $\sqrt{3-\sqrt{x-2}}$ $x-2 \geq 0$ $x \geq 2$ $D_f = [2, 11]$
 $3-\sqrt{x-2} \geq 0$ $3 \geq \sqrt{x-2} \Rightarrow 9 \geq x-2 \Rightarrow 11 \geq x$

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الف) $y = \sqrt{4-2x^2}$ $4-2x^2 \geq 0$ $4 \geq 2x^2$ $2 \geq x^2 \Rightarrow \sqrt{2} \geq x \geq -\sqrt{2}$
 $D_f = [-\sqrt{2}, \sqrt{2}]$

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ب) $y = \sqrt{3|x|-9}$ $3|x|-9 \geq 0$ $3|x| \geq 9$ $|x| \geq 3$ $x \geq 3$ $x \leq -3$ $D_f = [3, +\infty) \cup (-\infty, -3]$

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الف) $y = \sqrt[3]{\frac{|x|+1}{|x|-3}}$ $|x|-3 \neq 0$ $D_f = \mathbb{R} - \{-3, 3\}$
 $\frac{|x|}{-3} \neq 3$

ب) $y = \sqrt[3]{\frac{\sqrt{x+1}}{\sqrt{x-3}}}$ $\sqrt{x} \neq 3$ $x \neq 9$ $D_f = [0, +\infty) - \{9\}$

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الف) $y = \frac{\sqrt{3-|x|}}{|x|+2}$ $3-|x| \geq 0$ $3 \geq |x| \Rightarrow 3 \geq x \geq -3 \Rightarrow D_f = [-3, 3]$
 $|x|+2 \neq 0$ $|x| \neq -2$

ب) $y = \frac{\sqrt{4-x^2}}{|x|-1}$ $4-x^2 \geq 0$ $4 \geq x^2$ $2 \geq x \geq -2$ $D_f = [-2, 2] - \{-1, 1\}$
 $|x|-1 \neq 0$ $\frac{|x|}{-1} \neq 1$

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الف) $y = \frac{x+1}{\sqrt{x+|x|}}$ $x < 0$ $x+1 > 0 \Rightarrow x > -1$ $D_f = (-1, +\infty)$
 $x+|x| > 0 \Rightarrow x > 0$

ب) $y = \frac{1}{\sqrt{x|x|}}$ $x|x| > 0$ $x^2 > 0 \Rightarrow x \neq 0$ $D_f = (0, +\infty)$
 $x < 0$ $x|x| > 0 \Rightarrow x < 0$

$x_1, x_2, \dots$

الف) $y = \sqrt{1-x}$ $1-x \geq 0$ $x \leq 1 \rightarrow D_f = (-\infty, 1]$

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ب) $y = \frac{1}{\sqrt{1-x}}$ $1-x > 0$
 $x < 1 \rightarrow D_f = (-\infty, 1)$

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الف) $y = \frac{1}{x[x]}$ $x[x] \neq 0$ $D_f = \mathbb{R} - [0, 1) \rightarrow (-\infty, 0) \cup [1, \infty)$

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ب) $y = \frac{1}{\sqrt{-x[x]}}$ $-x[x] > 0$
 $x[x] < 0$

حاصل می شود: $\left. \begin{matrix} [x] \geq 0 \\ x > 0 \end{matrix} \right\} \rightarrow x > 0$
 $\left. \begin{matrix} [x] \leq 0 \\ x < 0 \end{matrix} \right\} \rightarrow x < 0$

مجموعه مقادیر برای x وجود ندارد: $\emptyset$

الف) $y = \sqrt{\left[x - \frac{1}{x}\right] + \left[x + \frac{1}{x}\right]}$ $\left[x - \frac{1}{x}\right] + \left[x + \frac{1}{x}\right] \geq 0$ $D_f = \left[\frac{1}{x}, +\infty\right)$
 $\left[x - \frac{1}{x}\right] + \left[x + \frac{1}{x}\right] - 1 + \left[x + \frac{1}{x}\right] \geq 0$
 $2\left[x + \frac{1}{x}\right] \geq 1$ $\left[x + \frac{1}{x}\right] \geq \frac{1}{2} \rightarrow x + \frac{1}{x} \geq \frac{1}{2}$

ب) $y = \sqrt{\left[x - \frac{1}{x}\right] + \left[-x + \frac{1}{x}\right]}$ $a \in \mathbb{Z} [a] + [-a] = 0$
 $a \notin \mathbb{Z} [a] + [-a] = -1 \Rightarrow x - \frac{1}{x} \in \mathbb{Z}$
 $D_f = \left\{x \mid x \in k + \frac{1}{x}, k \in \mathbb{Z}\right\}$

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$\frac{1}{x} \geq \frac{1}{2}$

الف) $y = \frac{1}{x \sin^2 x - 1}$ $x \sin^2 x - 1 \neq 0$ $D_f = \mathbb{R} - \left\{x \mid x \sin^2 x = 1\right\}$
 $x \sin^2 x \neq 1$
 $\sin^2 x \neq \frac{1}{x}$
 $\sin x \neq \pm \frac{1}{\sqrt{x}}$

ب) $y = \frac{\cot x + 1}{\tan x + 1}$ $\tan x + 1 \neq 0$ $\tan x \neq -1 \Rightarrow x \neq k\pi - \frac{\pi}{4}$
 $\cot x \neq 0$ $x \neq k\pi + \frac{\pi}{2}$ $D_f = \mathbb{R} - \left\{x \mid x \neq k\pi - \frac{\pi}{4}, k\pi + \frac{\pi}{2}\right\}$

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الف) $y = \sqrt{1 - \sin x}$ $1 - \sin x \geq 0$ $\sin x \leq 1$
 $D_f = \left[2k\pi + \frac{\pi}{2}, 2k\pi + \frac{3\pi}{2}\right]$

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ب) $y = \sqrt{1 - 2\cos x}$ $1 - 2\cos x \geq 0$
 $1 \geq 2\cos x$
 $\frac{1}{2} \geq \cos x$

$D_f = \left[2k\pi + \frac{\pi}{3}, 2k\pi + \frac{5\pi}{3}\right]$

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$D_f = \left[2k\pi + \frac{\pi}{3}, 2k\pi + \frac{5\pi}{3}\right]$