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الف) $\sqrt{4-5x-x^2} = 2-x \geq 0 \quad x \leq 2$ $Df \in [-2, 2]$
 $4-5x-x^2 \geq 0 \quad (x+1)(x-4) \leq 0$ $Df \in [-1, 4]$
 $2-x \leq 4 \quad x \geq -2$
 $-2 \leq x \leq 2$

ب) $\sqrt{3-\sqrt{x-2}} = x-2 \geq 0 \quad x \geq 2$ $Df \in [2, 11]$
 $3-\sqrt{x-2} \geq 0 \quad (3)^2 \geq (\sqrt{x-2})^2 \quad 9 \geq x-2 \quad 11 \geq x$

الف) $\sqrt{4-2x^2} = 4-2x^2 \geq 0 \quad \frac{2x^2}{2} \leq \frac{4}{2} \quad x^2 \leq 2 \quad x \leq \sqrt{2}$
 $x^2 \leq 2 \quad -\sqrt{2} \leq x \leq \sqrt{2} \quad Df \in [-\sqrt{2}, \sqrt{2}]$ $Df \in (+\infty, \sqrt{2}]$

ب) $\sqrt{3|x|-9} = 3|x|-9 \geq 0 \quad \frac{3|x|}{3} \geq \frac{9}{3} \quad |x| \geq 3$
 $|x| \geq 3 \quad x \geq 3 \quad Df \in [3, +\infty)$
 $|x| \geq 3 \quad x \leq -3 \quad Df \in (-\infty, -3]$
 $-3 \geq x \geq 3$

الف) $\sqrt[3]{\frac{|x|+1}{|x|-3}} = |x|-3 \neq 0 \quad |x| \neq 3 \quad |x| \neq \pm 3$
 $Df \in \mathbb{R} - \{3, -3\}$ فرم فشرده صورت تشریحی ندارد

ب) $\sqrt[3]{\frac{\sqrt{x}+1}{\sqrt{x}-3}} = \sqrt{x}-3 \neq 0 \quad \sqrt{x} \neq 3 \quad x \neq 9$
 $\sqrt{x} \rightarrow x \geq 0$
 $Df \in \mathbb{R} - \{9\}$
 $Df \in [0, +\infty) - \{9\}$

الف) $\frac{\sqrt{3-|x|}}{|x|-1} = 3-|x| \geq 0 \quad |x| \leq 3 \quad -3 \leq x \leq 3$
 $|x|-1 \neq 0 \quad x \neq \pm 1$ $Df \in [-3, 3] - \{\pm 1\}$ ارفاق نکرد!
 صحت سوال! اشتباه نوشتن $|x|+2$

ب) $\frac{\sqrt{4-x^2}}{|x|-1} = 4-x^2 \geq 0 \quad x^2 \leq 4 \quad x \leq 2 \quad x \geq -2$
 $|x|-1 \neq 0 \quad |x| \neq 1 \quad x \neq \pm 1$ $Df \in [-2, 2] - \{\pm 1\}$

الف) $\frac{x+1}{\sqrt{x+|x|}} = x+|x| > 0 \quad x \geq -|x| \quad Df \in \mathbb{R}^+$

ب) $\frac{1}{\sqrt{x|x|}} = x|x| > 0 \quad Df \in \mathbb{R} - \{0\}$
 $Df \in (0, +\infty)$

الف) $\sqrt{2-[x]} = 2-[x] \geq 0 \quad [x] \leq 2 \quad Df \in (-\infty, 3)$

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ب) $\frac{1}{\sqrt{2-[x]}} = 2-[x] > 0 \quad [x] < 2 \quad Df \in (-\infty, 2)$

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الف) $\frac{1}{x[x]} = x[x] \neq 0 \quad Df \in \mathbb{R} - \{0\}$

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$[x] \neq 0 \quad x \neq [0, 1) \rightarrow Df = \mathbb{R} - [0, 1)$

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ب) $\frac{1}{\sqrt{-x[x]}} = -x[x] > 0 \quad x[x] < 0 \quad \left\{ \begin{array}{l} -1 < x < 1 \\ Df \in (0, 1) \end{array} \right.$

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$Df = \emptyset \leftarrow$ همواره هم علامت هستند

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الف) $\sqrt{[x-\frac{1}{x}] + [x+\frac{1}{x}]} = [x-\frac{1}{x}] + [x+\frac{1}{x}] \geq 0 \quad [x+\frac{1}{x}-1] + [x+\frac{1}{x}] \geq 0$
 $2[x+\frac{1}{x}] \geq 1 \quad [x+\frac{1}{x}] \geq \frac{1}{2} \quad x+\frac{1}{x} \geq 1 \quad x \geq \frac{1}{2} \quad Df \in [\frac{1}{2}, +\infty)$
 $2[x+\frac{1}{x}] \geq \frac{1}{2} \quad [x+\frac{1}{x}] \geq \frac{1}{4} \quad x+\frac{1}{x} \geq \frac{1}{4} \quad x \geq \frac{1}{4} - \frac{1}{4} \quad x \geq -\frac{1}{4}$

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ب) $\sqrt{[x-\frac{1}{x}] + [-x+\frac{1}{x}]} = \sqrt{[x-\frac{1}{x}] + [-(x-\frac{1}{x})]} \xrightarrow{\text{if } \begin{cases} a \in \mathbb{Z} & [a] + [-a] = 0 \\ a \notin \mathbb{Z} & [a] + [-a] = -1 \end{cases}} \downarrow$
 $Df = \{x | x = k + \frac{1}{x}, k \in \mathbb{Z}\} \quad x - \frac{1}{x} \in \mathbb{Z}$

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الف) $\frac{1}{x \sin^2 x - 1} = \frac{x \sin^2 x \neq \frac{1}{x}}{\sin^2 x \neq \frac{1}{x} \quad \sin x \neq \pm \sqrt{\frac{1}{x}}}$
 $Df: \mathbb{R} - \left\{ \frac{k\pi}{x} + \frac{\pi}{2} \right\}$

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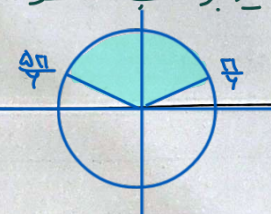
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ب) $\frac{\cot x + 1}{\tan x + 1} = \tan \neq -1$
 $Df: \mathbb{R} - \left\{ \frac{k\pi}{x}, \frac{k\pi - \frac{\pi}{2}}{x} \right\}$
 $\tan x \neq -1$

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باید بر حسب دستوراتش بنویس!



الف) $\sqrt{x \sin x - 1} = \frac{x \sin x \geq \frac{1}{x}}{\sin x \geq \frac{1}{x}}$

$Df \in \mathbb{R} - \{1, 0, \pi, 2\pi, 3\pi, 4\pi, 5\pi, 6\pi, 7\pi, 8\pi, 9\pi, 10\pi, 11\pi, 12\pi\}$
 $Df = [2k\pi + \frac{\pi}{4}, 2k\pi + \frac{5\pi}{4}]$

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ب) $\sqrt{1-x \cos x} = \frac{x \cos x \leq \frac{1}{x}}{\cos x \leq \frac{1}{x}} \quad Df \in \mathbb{R} - \{\frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \frac{7\pi}{2}, \frac{9\pi}{2}, \frac{11\pi}{2}, \frac{13\pi}{2}, \frac{15\pi}{2}\}$
 $Df: [2k\pi + \frac{\pi}{4}, 2k\pi + \frac{5\pi}{4}]$

