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الف) $3 \times 1^2 - 1, 3 \times 2^2 - 1, 3 \times 3^2 - 1, 3 \times 4^2 - 1, 3 \times 5^2 - 1 \rightarrow 2, 11, 26, 49, 74, \dots$

ب) $\frac{3}{5}, \frac{5}{9}, 1, \frac{9}{16}, \frac{16}{25}, \dots$

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الف) $t_{13} = \frac{(-1)^{13}}{\sqrt{13+13}} = \frac{-1}{\sqrt{26}} = -\frac{1}{\sqrt{26}}$

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ب) $t_{13} = \frac{26}{\sqrt{26}} - \left[\frac{13}{\sqrt{26}} \right] = 26 - 3 = 23$
 $\hookrightarrow 3 \frac{1}{3}$

الف) $2n - 10 < 0 \rightarrow 2n < 10 \rightarrow n < 5 \rightarrow 1, 2, 3, 4 \rightarrow \bar{4}$

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ب) $n^2 - 14n + 40 < 0 \rightarrow \frac{n^2 - 14n + 40}{(n-4)(n-10)} \rightarrow \begin{array}{c} 4 \quad 10 \\ + \quad - \quad + \end{array} \rightarrow (4, 10) \rightarrow 5, 6, 7, 8, 9 \rightarrow \bar{5}$

الف) $2n - 14 \leq 0 \rightarrow 2n \leq 14 \rightarrow n \leq 7 \rightarrow 1, 2, 3, 4, 5, 6, 7 \rightarrow \bar{7}$

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ب) $n^2 - 12n + 27 \leq 0 \rightarrow \frac{n^2 - 12n + 27}{(n-3)(n-9)} \rightarrow \begin{array}{c} 3 \quad 9 \\ + \quad - \quad + \end{array} \rightarrow [3, 9] \rightarrow 4, 5, 6, 7, 8 \rightarrow \bar{6}$

$t_n = an + b \rightarrow 3n - 2$ $t_4 = 4a + b = 7 \rightarrow 4 \times 3 - 2 = -b \rightarrow 10 = -b \rightarrow b = -10$
 $t_4 = 4a + b = 7$
 $t_9 = 9a + b = 22$
 $5a = 15 \rightarrow a = 3$
 $t_4 = 3 \times 4 - 2 = 10$

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الف) $t_n = n^2 - 5n + 2 \rightarrow \min \mid \textcircled{5} = n \rightarrow 3^2 - 5 \times 3 + 2 = \textcircled{-4}$ ۱۱۵ ب) $t_n = n^2 + 4n + 1 \rightarrow \min \mid \frac{b}{2a} = n \rightarrow n = -2 \Rightarrow (-2)^2 + 4 \times (-2) + 1 = \textcircled{-3}$ نمی توانیم با $n=1$ باشد - n نمی تواند ۲- باشد	۶
① $t_n = -4, -7, -1, -5, -2, 1, 4, 7, 9, 11, 13$ ② $2a = 2 \rightarrow a = 1, c = 1$ $an^2 + bn + c \rightarrow n^2 + bn + 1 \Rightarrow 1^2 + 1 \times b + 1 = -4 \rightarrow b = -7$ $\hookrightarrow n^2 - 7n + 1 = a_n \rightarrow a_{10} = 10^2 - 7 \times 10 + 1 = \textcircled{41}$ ③ $1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100$ $\hookrightarrow a(x-3)^2 - 1 = y \rightarrow (x-3)^2 - 1 = y$	۷
$t_n = -4, -1, 1, 2, 1$ $C = -9$ $2a = 4 \rightarrow a = 2$ $C = -9$ $t_n = an^2 + bn + c$ $t_n = 2n^2 + bn - 9$ $t_1 = 2 + b - 9 = -4 \rightarrow b = 1$ $\hookrightarrow t_n = 2n^2 + n - 9$	۸
$2a + 1 \geq a + 4 \rightarrow a \geq 3 \rightarrow a = [3, +\infty)$	۹
الف) $1 \leq 3n \leq 100 \rightarrow \frac{1}{3} \leq n \leq 33.\bar{3} \rightarrow 1, 2, \dots, 33 \rightarrow \bar{33} = A$ ب) $1 \leq 5n \leq 100 \rightarrow \frac{1}{5} \leq n \leq 20 \rightarrow 1, 2, \dots, 20 \rightarrow \bar{20} = B$ ج) $A \cap B = 1 \leq n \leq 100 \rightarrow \frac{1}{5} \leq n \leq 20 \rightarrow 1, 2, 3, 4, 5, 6, 7 \rightarrow A \cap B = \bar{7}$ د) $A \cup B = n(A) + n(B) - n(A \cap B) = 33 + 20 - 7 = 46$	۱۰