

$$(1! + 2! + 3! + \dots + 100!) (1! + 2! + 3! + \dots + 100!) =$$

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از اینجا بعد خاطر اینکه هم ۵ داریم رقم یکان صفر است.

$$(1 + 4 + 9 + \dots + 100) (2 + 4 + \dots + 100) = 5 \times 4 = 20$$

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الف) $\sqrt[4]{(4 + \sqrt{5})^{-1}} \cdot \frac{\sqrt{1 + \sqrt{5}}}{\sqrt[4]{(1 + \sqrt{5})^2}} = \sqrt[4]{\frac{1 + \sqrt{5}}{8 + 4\sqrt{5}}}$

$$= \sqrt[4]{\frac{1 + \sqrt{5}}{4(2 + \sqrt{5})}} = \sqrt[4]{\frac{1 + \sqrt{5}}{4(2 + \sqrt{5}) \cdot (2 - \sqrt{5})}} = \sqrt[4]{\frac{1 + \sqrt{5}}{4(4 - 5)}} = \sqrt[4]{\frac{1 + \sqrt{5}}{-4}}$$

ب) $\left(\frac{\sqrt{5} + \sqrt{2}}{\sqrt{5} - \sqrt{2}}\right) (\sqrt{5} - \sqrt{2} - \sqrt{2 + \sqrt{5}})$

$$\frac{\sqrt{5} + \sqrt{2}}{\sqrt{5} - \sqrt{2}} = \frac{1}{\sqrt{5} - \sqrt{2}} = \frac{\sqrt{5} + \sqrt{2}}{5 - 2} = \frac{\sqrt{5} + \sqrt{2}}{3}$$

$$A^2 = 2 - \sqrt{5} + 2 + \sqrt{5} - 2\sqrt{(5 - \sqrt{5})(2 + \sqrt{5})}$$

$$= 4 - 2\sqrt{9 - 5} = 4 - 4 = 0 \Rightarrow A = 0$$

چون از اینجا بعد داریم از اینجا اول فرستاده.

$$\frac{\sqrt{5}}{2} \times -\sqrt{5} = -1$$

الف) $\frac{\sqrt{5} + \sqrt{2}}{5 - \sqrt{2}} - 2 \left(\frac{\sqrt{5} - 1}{\sqrt{5} - 1} \right)^{-1}$

$$\frac{2\sqrt{5} + 2\sqrt{2}}{5 - \sqrt{2}} = \frac{10\sqrt{5} + 4\sqrt{2} + 10\sqrt{2} + 9\sqrt{5}}{19}$$

$$= \frac{19(\sqrt{5} + \sqrt{2})}{19} = \sqrt{5} + \sqrt{2} - 2 \left(\frac{1}{\sqrt{5} - 1} \right) = \sqrt{5} + \sqrt{2} - \sqrt{5} - 1 = \sqrt{2} - 1$$

$$= \sqrt{2} - 1$$

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ب) $\frac{\sqrt{5} - 1}{5 + \sqrt{2}} + (2 - \sqrt{5})^{-1}$

$$\frac{3\sqrt{5} - 1}{5 + \sqrt{2}} = \frac{15\sqrt{5} - 9 - 4 + \sqrt{2}}{13} = \frac{15\sqrt{5} - 13}{13}$$

$$= \frac{15\sqrt{5} - 13}{13} = \frac{15(\sqrt{5} - 1)}{13} = \sqrt{5} - 1$$

$$\Rightarrow \sqrt{5} - 1 + 2 + \sqrt{5} = \sqrt{5} + 1$$

$$= \sqrt{5} + 1$$

الف) $\frac{(\sqrt{1 + \sqrt{5}} + \sqrt{\sqrt{5} - 1})}{\sqrt{\sqrt{5} - \sqrt{5}}} = A$

$$A^2 = 1 + \sqrt{5} + \sqrt{5} - 1 + 2\sqrt{(\sqrt{5} + 1)(\sqrt{5} - 1)} = 2\sqrt{5} + 2\sqrt{5} \Rightarrow A = \sqrt{4\sqrt{5} + 4\sqrt{5}}$$

$$\sqrt{\frac{2(\sqrt{5} + \sqrt{5}) \times (\sqrt{5} + \sqrt{5})}{\sqrt{5} - \sqrt{5}}} = \sqrt{\frac{2(\sqrt{5} + \sqrt{5})^2}{1}} = (\sqrt{5} + \sqrt{5})\sqrt{2} = \sqrt{4} + \sqrt{4} = 2 + 2 = 4$$

$$= \sqrt{4}$$

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$$\begin{aligned} & \sqrt[r]{r} \times \sqrt[r]{r^4} \times \sqrt[r]{r^2} = r^{\frac{r}{r}} \times r^{\frac{4}{r}} \times r^{\frac{2}{r}} = r \times r \times r = \boxed{1r} \\ & = \sqrt[r]{r^2} \times \sqrt[r]{r^6} = \sqrt[r]{r^8} = r^{\frac{8}{r}} = r^{\frac{1}{r}} \times r^{\frac{7}{r}} = r \times r^{\frac{7}{r}} \end{aligned}$$

$$\begin{aligned} & r^x (1 + r + r^2 + r^3 + r^4 + r^5 + r^6) = 2r \Rightarrow \left(\frac{r}{r}\right)^x \times \frac{r^4 r}{10, 100} = 2r \\ & \Rightarrow \left(\frac{r}{r}\right)^x = \frac{2r \times 10, 100}{r^4 r} = 2, 200 \end{aligned}$$

$$(a-b)(a+b)^r = (a^r - b^r)^r = (\sqrt{r^2-1} - \sqrt{r^2+1})^r = ((\sqrt{r^2-1} - \sqrt{r^2+1})^r)^r$$

$$\begin{aligned} & \left(\left(a + \frac{1}{a}\right)^r - (r^r)^r \right)^r = \left(a^r + \frac{1}{a^r} + r - r^r \right)^r = \left(a^r + \frac{1}{a^r} \right)^r = (r^r - r^r)^r = 0 \\ & = a^r + \frac{1}{a^r} + r = r - r^r + \frac{1}{r - r^r} + r = 1r + r = 14 \\ & a = \sqrt[r]{r - r^r} \Rightarrow a^r = r - r^r \Rightarrow 14 = r^2 \Rightarrow \boxed{r = 4} \end{aligned}$$

$$\begin{aligned} & A = \sqrt[r]{r^4} \left(\frac{1}{r}\right)^{-\frac{r}{r}}, (rA)^{-\frac{1}{r}} = ? \\ & r^{\frac{r}{r}} \times r^{\frac{r}{r}} \times r^{\frac{r}{r}} = A = r^{\frac{r}{r}} = r^r = r \end{aligned}$$

$$\begin{aligned} & \sqrt{a} = r \sqrt{a^{\frac{10}{r}}} \rightarrow a^{\frac{1}{r}} = r \sqrt{a^{\frac{10}{r}}} \Rightarrow \frac{a^{\frac{1}{r}}}{a^{\frac{10}{r}}} = r \Rightarrow a^{-\frac{9}{r}} = r \Rightarrow a = r^{-\frac{r}{9}} \end{aligned}$$

$$\begin{aligned} & \frac{1}{a} = \frac{1}{r^{-\frac{r}{9}}} = r^{\frac{r}{9}} = r \sqrt{r} \\ & \frac{r^{\frac{r}{9}} - r^{\frac{r}{9}} (1 - \sqrt{r})}{1 + \sqrt{r} \times (1 - \sqrt{r})} = \frac{r^{\frac{r}{9}} (\sqrt{r} - 1) (1 - \sqrt{r})}{-r} = \frac{-r^{\frac{r}{9}} (\sqrt{r} - 1)^2}{-r} = \frac{r^{\frac{r}{9}} (r - r\sqrt{r})}{r} \end{aligned}$$

$$\sqrt{a+a} - \sqrt{a-1} = r, \sqrt{a+a} + \sqrt{a-1} = ? \Rightarrow \frac{a}{r} + r - r = \boxed{\frac{a}{r}} = 4 - r\sqrt{r}$$

$$(\sqrt{a+a} - \sqrt{a-1})(\sqrt{a+a} + \sqrt{a-1}) = rA = a+1 \Rightarrow A = \frac{a}{r} + r$$