

1915

يسعدنا توافقي تكليفيا 24

(م) قدر

(1)

(الف)  $y = 2x^2 - 4x + 1$

(ب)  $y = -2x^2 + 4x - 9$

ext  $\left| \begin{array}{l} -\frac{b}{2a} = \frac{4}{4} = 1 \\ -\frac{\Delta}{4a} = \frac{-4}{4} = -1 \end{array} \right.$

ext  $\left| \begin{array}{l} \frac{b}{2a} = \frac{-4}{-2} = 2 \\ -\frac{\Delta}{4a} = \frac{16}{-4} = -4 \end{array} \right.$

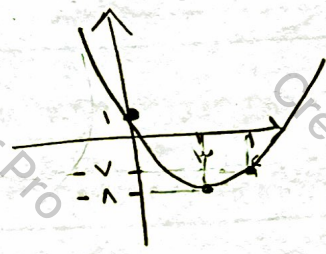
$\Delta = b^2 - 4ac \Rightarrow 16 - 4 = 12$

$\Delta = b^2 - 4ac \Rightarrow 16 - 4(-9)(-2) = -76$

(الف)  $y = x^2 - 9x + 1$

ext  $\left| \begin{array}{l} -\frac{b}{2a} = \frac{9}{2} = 4.5 \\ -\frac{\Delta}{4a} = \frac{-81}{4} = -20.25 \end{array} \right.$

Table with x values 1, 2, 3, 4, 5 and y values -7, -1, 1, -7



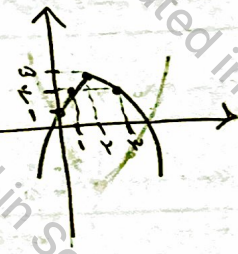
$\Delta = b^2 - 4ac \Rightarrow 81 - 4 = 77$

$19 - 2 \times 1$

(ب)  $y = -x^2 + 4x + 1$

ext  $\left| \begin{array}{l} -\frac{b}{2a} = \frac{-4}{-2} = 2 \\ -\frac{\Delta}{4a} = \frac{-16}{-4} = 4 \end{array} \right.$

Table with x values 1, 2, 3, 4 and y values 5, 5, 1, -3



$\Delta = b^2 - 4ac \Rightarrow 16 - 4(1)(1) = 12$

$x^3 + 11x^2 - 9x - 15 = 0 \rightarrow \alpha(x-\alpha)(x-\beta)(x-\gamma)$

$= \alpha x^3 - \alpha(\alpha+\beta+\gamma)x^2 + \alpha(\alpha\beta+\alpha\gamma+\beta\gamma) - \alpha\alpha\beta\gamma = 0$

$S = \frac{\alpha+\beta+\gamma}{-1} = -\frac{11}{1} \rightarrow 1 - \frac{1}{\alpha} = \frac{-11}{\alpha} \rightarrow \alpha = -1$

$P = \frac{\alpha\beta\gamma}{1} = \frac{15}{1} = 15 \rightarrow \alpha\beta = -15 \quad \gamma = -\frac{1}{\alpha}$

$x^2 - 10x + 15 = 0$

$x = \alpha \rightarrow \alpha^2 - 10\alpha + 15 = 0$

$x = \beta \rightarrow \beta^2 - 10\beta + 15 = 0$

$S = 15$

$P = 15$

$2x^2 - 10x - 15 = 0$

$2x^2 - x - 15 = 0$

$P = \frac{-1}{2}$

$P = \frac{15}{2}$

$\sqrt{x} - \sqrt{y} = 1$

$\frac{x+y - 2\sqrt{xy}}{2} = 1$

$\frac{x+y}{2} - \sqrt{xy} = 1$

$\sqrt{x} = 1 + \sqrt{y} \rightarrow \sqrt{m} = 1 + \sqrt{1-m} \rightarrow m = 1$

$$y = 2x^2 - (m+2)x + m$$

$$\Delta = \frac{1}{4} \times \frac{|m+2|}{4} \times |m| = \frac{|m(m+2)|}{16}$$

$$\alpha + \beta = \frac{m+2}{2} \quad \alpha\beta = \frac{m}{2}$$

$$\Delta = (m+2)^2 - 4m \rightarrow m^2 + 4m + 4 - 4m = m^2 + 4 = (m+2)^2$$

$$\frac{m}{2} = \frac{2}{2}, \frac{1}{2}$$

$$y = ax^2 + 2x + a$$

$$\Delta = 4 + 4a^2 = 4(1+a^2)$$

$$a > 0 \text{ min } \Delta = 4 - 4a^2 \quad a = \frac{2 \pm 2\sqrt{0}}{2} \rightarrow a = 1, a = -1 \rightarrow a = 1$$

$$\text{ext } \left\{ \begin{aligned} \frac{-b}{2a} &= \frac{-2}{2a} = -\frac{1}{a} \\ \frac{-\Delta}{4a} &= \frac{-(4-4a^2)}{4a} = \frac{a^2-1}{a} \end{aligned} \right. \rightarrow \text{ext } \left\{ \begin{aligned} x &= x \\ x &= \beta \end{aligned} \right. \rightarrow x^2 - (a+1)x + a = 0$$

$$\frac{\sqrt{\Delta}}{|a|} = \frac{\sqrt{(a+1)^2}}{|a|} = \frac{a+1}{a} = 1 + \frac{1}{a}$$

$$\Delta = b^2 - 4ac \rightarrow (a+1)^2 - 4a \rightarrow a^2 + 2a + 1 - 4a = a^2 - 2a + 1 = (a-1)^2$$

$$x^2 - (a+1)x + b = 0 \quad x = \alpha \rightarrow \alpha^2 - (a+1)\alpha + b = 0$$

$$\frac{\sqrt{\Delta}}{|a|} = \sqrt{1 - \frac{4b}{a}} = 1 \rightarrow 1 - \frac{4b}{a} = 1 \rightarrow -\frac{4b}{a} = 0 \rightarrow b = 0$$

$$\Delta = b^2 - 4ac \rightarrow (a+1)^2 - 4b \rightarrow 1 - 4b$$

$$4a = 4b \rightarrow b = a = 1$$

$$\textcircled{1} y = -ax^2 + ax + 2 \rightarrow \text{ext } \left\{ \begin{aligned} \frac{-b}{2a} &= \frac{-a}{-2a} = \frac{1}{2} \\ \frac{-\Delta}{4a} &= \frac{-(a^2 + 4a)}{4a} = -\frac{a+4}{4} \end{aligned} \right. \rightarrow a = 12, b = -4$$

$$\textcircled{2} y = 2bx^2 - bx - 1 \rightarrow \text{ext } \left\{ \begin{aligned} \frac{-b}{2a} &= \frac{-1}{4b} = -\frac{1}{4b} \\ \frac{-\Delta}{4a} &= \frac{-(b^2 + 4b)}{8b} = -\frac{b+4}{2b} \end{aligned} \right. \rightarrow b = 4, b = 12$$

$$b - a = -4 - (-12) = 8$$

$$y = \gamma \omega \alpha x^2 + \epsilon x + \beta \quad \xrightarrow{\alpha=\alpha} \quad \gamma \omega \alpha^2 + \alpha + \beta = 0$$

$$\xrightarrow{\alpha=\beta} \quad \gamma \omega \alpha \beta^2 + \beta + \beta = 0 \quad \gamma \omega \alpha \beta^2 + \omega \beta = 0$$

$$\omega \beta (\omega \alpha \beta + 1) = 0$$

$$S = \frac{\gamma \omega \alpha^2}{\gamma \omega \alpha} = \alpha + \beta$$

$$P = \frac{\gamma \omega \alpha}{\gamma \omega \alpha} = \alpha \beta \rightarrow \gamma \omega \alpha^2 = 1 \rightarrow \alpha = \pm \frac{1}{\sqrt{\gamma \omega}}$$

$$\alpha < \beta \rightarrow \alpha = -\frac{1}{\sqrt{\gamma \omega}}, \beta = 1$$

$$y = -\omega x^2 + \epsilon x + 1 \rightarrow \text{mat} \begin{vmatrix} \frac{1}{\sqrt{\gamma \omega}} & \epsilon \\ 1 & \gamma \omega \end{vmatrix} \rightarrow \begin{vmatrix} \frac{1}{\sqrt{\gamma \omega}} & \epsilon \\ 1 & \gamma \omega \end{vmatrix} \rightarrow \begin{vmatrix} \frac{1}{\sqrt{\gamma \omega}} & \epsilon \\ 1 & \gamma \omega \end{vmatrix} \rightarrow \begin{vmatrix} \frac{1}{\sqrt{\gamma \omega}} & \epsilon \\ 1 & \gamma \omega \end{vmatrix}$$

$$\alpha^2 - (a^2 + b^2 - 1)x + a^2 - 1 = 0 \quad S = a + b \quad P = ab$$

$$a^2 + b^2 - 1 = a + b \rightarrow S^2 - 2P - 1 = S \rightarrow S^2 - 2(S-1) - 1 = S$$

$$ab = a + b - 1 \rightarrow P = S - 1 \quad S^2 - 2S - 1 = 0$$

$$(S-5)(S+2) = 0$$

$$\boxed{S = 5}$$

دون اطمینان

$$S = -2$$

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