

رحمہ پھن مرد (۱۳۲۱ھ - ۱۳۲۲ھ) (۱۳۲۱ھ - ۱۳۲۲ھ)

$$\begin{aligned} 1! &\rightarrow 1 \\ 2! &\rightarrow 2 \\ 3! &\rightarrow 6 \\ 4! &\rightarrow 24 \\ 5! &\rightarrow 120 \\ \vdots &\vdots \\ n! &\rightarrow n! \end{aligned}$$

$$\} \rightarrow (1+q)(r+e) = V \times G = \underline{15r} \rightarrow \boxed{r}$$

$$\text{الف) } \sqrt{(4+\sqrt{3})^{-1}} \sqrt{1+\sqrt{3}} = \sqrt{\left(\frac{1+\sqrt{3}}{4}\right)^{-1}} \sqrt{1+\sqrt{3}} = \sqrt{\frac{4}{1+\sqrt{3}}} \cdot \frac{1+\sqrt{3}}{1} = \sqrt{4} = 2$$

$$\rightarrow \frac{\sqrt{r} + \sqrt{d}}{(\sqrt{r} + \sqrt{d})\sqrt{r}} \times \left(\sqrt{\frac{(\sqrt{c} + \sqrt{d} - \sqrt{c} + \sqrt{d})^2}{r - \sqrt{d} + c + \sqrt{d} - c = r}} \right) = \frac{1}{\sqrt{r}} \times (-\sqrt{r}) = \boxed{-1}$$

$$\text{الف) } \frac{(\sqrt{r} + \sqrt{r})(\sqrt{r} - \sqrt{r})}{\cancel{\sqrt{r}}} = \frac{r}{\sqrt{r} - 1} = \frac{r + \sqrt{r} - \sqrt{r} - r}{\sqrt{r} - 1} = \frac{(1 - \sqrt{r}) + (\sqrt{r} - r)}{\sqrt{r} - 1}$$

$$= \frac{(\sqrt{r} - 1)(\sqrt{r} - 1)}{\cancel{\sqrt{r} - 1}} = \boxed{\sqrt{r} - 1}$$

$$\therefore \frac{(\sqrt{c}-1)(\sqrt{c}+1+\sqrt{c})}{\cancel{c+\sqrt{c}}} + \frac{\sqrt{c}+1}{\cancel{(\sqrt{c}+1)}} = \sqrt{c} - 1 + \sqrt{c} = \boxed{1+2\sqrt{c}}$$

الف) $\sqrt{\frac{1+\sqrt{e}+\sqrt{e}-1+\sqrt{r}}{\sqrt{e}-\sqrt{r}}} - r = \sqrt{\frac{r(\sqrt{e}+\sqrt{r})}{(\sqrt{e}-\sqrt{r})} \times \frac{\sqrt{e}+\sqrt{r}}{\sqrt{e}+\sqrt{r}}} - r = \sqrt{\frac{r(\sqrt{e}+\sqrt{r})}{1}} - r$
 $= (\sqrt{e}+\sqrt{r})(\sqrt{r}) - r = \sqrt{e} + r - r = \boxed{\sqrt{e}}$

$$\rightarrow \sqrt[10]{r^{10}} \times \sqrt{r} \times \sqrt[12]{r^{12}} = r^{\frac{1}{10}} \times r^{\frac{1}{2}} \times r^{\frac{1}{6}} = r^{\frac{1+3+5}{6}} = r^{\frac{9}{6}} = r^{\frac{3}{2}}$$

$$\frac{r^n (1+r+q+rV+1+rEc)}{r^{n-r} (1+r+E+1+q+Cr)} = \cancel{dr} \rightarrow r^{n-r} \times \cancel{qV} \times \cancel{dr} = r^n \times r \times \cancel{qV}$$

$$r^{n-r} \times Cr = r^n \times V$$

$$r^{n-r} \times r^r = r^n$$

$$r^{n-r} \times r^r = r^n$$

$$\boxed{r = n}$$

$$\begin{aligned}
 (a^r + b^r - r ab)^r (a^r + b^r + r ab)^r &= ((a-b)^r (a+b)^r)^r = (a^r - b^r)^2 \left((a^r - b^r)^r \right)^r \\
 &= (a^r + b^r - r ab)^r = (\sqrt{9} + \sqrt{5} - r - r\sqrt{5})^r = (r\sqrt{5} - r\sqrt{5})^r \\
 &= (r(\sqrt{5} - \sqrt{5}))^r = r^r \times (2 + r - r^2\sqrt{10}) = 19 \times (r - \sqrt{5}) \\
 &= 19(r - \sqrt{5}) = 19(r - \sqrt{5}) \rightarrow \boxed{r = 19} \quad \left(\begin{smallmatrix} \infty \\ 1 \end{smallmatrix} \right)
 \end{aligned}$$

$$\begin{aligned}
 \left(a + \frac{1}{a} - \sqrt{r}\right)^r \left(a + \frac{1}{a} + \sqrt{r}\right)^r &= \left(\left(a + \frac{1}{a}\right)^r - r\right)^r \\
 \left(a^r + \frac{1}{a^r} + r - r\right)^r &= \left(a^r + \frac{1}{a^r}\right)^r = a^r \left(\frac{1}{a^r} + r - r \right) = \sqrt{r-5} + \frac{1}{\sqrt{r-5}} + r \\
 \sqrt{r-5} + \frac{\sqrt{r-5}}{r-5} + r &= \sqrt{r-5} + r = 19 = r \rightarrow \boxed{r = 19} \quad \left(\begin{smallmatrix} \infty \\ 1 \end{smallmatrix} \right)
 \end{aligned}$$

$$\begin{aligned}
 (rA)^{-\frac{1}{r}} &= \left(r^{\frac{1}{10}} \times r^{\frac{2}{10}} \times r^{\frac{3}{10}} \times r^{\frac{4}{10}}\right)^{-\frac{1}{r}} = \left(r^{\frac{10}{10}}\right)^{-\frac{1}{r}} = (r)^{-\frac{1}{r}-1} \\
 &= \boxed{\frac{1}{r}} \quad \left(\begin{smallmatrix} \infty \\ 1 \end{smallmatrix} \right)
 \end{aligned}$$

$$\begin{aligned}
 \sqrt[r]{a} &= a^{\frac{1}{r}} \rightarrow a^{\frac{1}{r}} = r^r \times a^{\frac{1}{r}} \rightarrow 1 = r^r \times a^{\frac{1}{r}} \rightarrow r^{-r} = a^{\frac{1}{r}} \rightarrow a = r^r \\
 \frac{\left(\frac{1}{a} - r\right)}{1 + \sqrt{r}} &= \frac{r\sqrt{r} - r}{1 + \sqrt{r}} = \frac{r(\sqrt{r} - 1)}{\sqrt{r} + 1} \times \frac{\sqrt{r} - 1}{\sqrt{r} - 1} = \frac{r(r+1 - r\sqrt{r})}{r-1} = \frac{r(r-\sqrt{r})}{r-1} \\
 &= \boxed{9 - 3\sqrt{5}} \quad \left(\begin{smallmatrix} \infty \\ 1 \end{smallmatrix} \right)
 \end{aligned}$$

$$\begin{aligned}
 (\sqrt{n+a} - \sqrt{n-a}) (\sqrt{n+a} + \sqrt{n-a}) &= n+a - n+a = a \\
 a + r &= r(\sqrt{n+a} + \sqrt{n-a}) \rightarrow \sqrt{n+a} + \sqrt{n-a} = \frac{a+r}{r} \\
 \rightarrow \sqrt{n+a} + \sqrt{n-a} - r &= \frac{a}{r} + r - r = \boxed{\frac{a}{r}} \quad \left(\begin{smallmatrix} \infty \\ 1 \end{smallmatrix} \right)
 \end{aligned}$$