

$$\alpha + \beta = 5 \quad \alpha\beta = 2 \quad \beta^2 = 5\beta - 2 \quad \text{۱-}$$

ی نسبت بده

$$\beta^3 = \beta \times \beta^2 = \beta(5\beta - 2) = 5\beta^2 - 2\beta = 5(5\beta - 2) - 2\beta = 25\beta - 10 - 2\beta = 23\beta - 10$$

$$\beta^4 = \beta \times \beta^3 = \beta(23\beta - 10) = 23\beta^2 - 10\beta = 23(5\beta - 2) - 10\beta = 115\beta - 46 - 10\beta = 105\beta - 46$$

$$f(\alpha + \beta^4) = f(\alpha) + f(105\beta - 46) = 5 + 105f(\beta) - 46f(1) = 5 + 105(5) - 46(1) = 545 - 41 = 504$$

$$f(\alpha + \beta^4) = f(5 - \beta) + f(105\beta - 46) = 5 + 105f(\beta) - 46f(1) = 5 + 105(5) - 46(1) = 545 - 41 = 504$$

$$f(105\beta - 46) = 105f(\beta) - 46f(1) = 105(5) - 46(1) = 545 - 46 = 504$$

$$5\beta^2 = 5(5\beta - 2) = 25\beta - 10$$

$$\frac{19}{5} = \frac{545 - 190}{25 - 10} = \frac{5(95 - 38)}{5(5 - 2)} = \frac{95 - 38}{5 - 2} = 19$$

مخرج

$$y = -\frac{4}{5} \quad x = \frac{2 + (-15)}{2} = \frac{2 - 15}{2} = \frac{-13}{2} = -\frac{13}{2}$$

$$f(x) = ax^2 + bx + c = \frac{x^2 - r_1 + r_2}{2} = \frac{1}{2} \Rightarrow$$

$$r_1 + r_2 = 2 \cdot \frac{1}{2} = 1$$

$$r_1 + r_2 = -2k \quad r_1 \times r_2 = 5$$

$$r_1 - r_2 = \frac{4k}{3} \quad (r_1 - r_2)^2 = (r_1 + r_2)^2 - 4r_1 r_2$$

$$\left(\frac{4k}{3}\right)^2 = (-2k)^2 - 4(5) \quad \frac{16k^2}{9} = 4k^2 - 20 \quad 16k^2 = 36k^2 - 180 \quad 20k^2 = 180 \quad k^2 = 9 \quad k = 3 \quad \frac{k^2}{9} = \frac{9}{9} = 1$$

$$x = \frac{3 + (-5)}{2} = -1 \quad f(x) = a(x^2 + 2x + 1) + 1 = a(x+1)^2 + 1$$

$$2a(x+1) + a + 1 = 5 \quad \alpha + \beta = 2a \quad \alpha\beta = a + 1$$

$$(-2a)^2 - 2(a+1) = 5 \quad 4a^2 - 2a - 7 = 0$$

$$a = \frac{2 \pm \sqrt{4 + 112}}{8} = \frac{2 \pm \sqrt{116}}{8} = \frac{1 \pm \sqrt{29}}{4} \quad x=0 \Rightarrow f(0) = a(0+1)^2 + 1$$

$$+1 = a + 1 \quad f(0) = \frac{1 + \sqrt{29}}{4} + 1 = \frac{5 + \sqrt{29}}{4} \quad 5 + \sqrt{29} = 29$$

$$f(0) = \frac{5 + \sqrt{29}}{4} = \frac{10 + \sqrt{29}}{8} = 2,5$$

$$f(0) = \frac{1 - \sqrt{29}}{4} + 1 = \frac{5 - \sqrt{29}}{4}$$

$$f(0) = \frac{5 - \sqrt{29}}{4} = \frac{-0,29}{4} = -0,1$$

Genobar

نقطه: (0, 2,5) و (0, -0,1)  
مخرج: 4

$$0 = \omega - \frac{1}{\omega} (-1) m = 2\omega + \frac{1}{\omega} m \quad m - \frac{2\omega}{\omega} = -2\omega \quad \Delta \geq 0 \quad \omega \geq 0$$

$$x = \frac{-\omega}{-2\omega} = \frac{1}{2} = \frac{1}{2}, \omega \quad f\left(\frac{1}{2}\right) = -\left(\frac{1}{2}\right)^2 + 0\left(\frac{1}{2}\right) + m \leq 0$$

$$-\frac{1}{4} + \frac{1}{2} + m \leq 0 \quad \frac{1}{4} + m \leq 0 \quad m \leq -\frac{1}{4} = -0.25$$

$$-0.25 \leq m \leq -0.25 \quad m = \{-0.25, -0.25, -0.25\} = \{-0.25\}$$

$$x = \frac{-b}{2a} = \frac{-(-12)}{2m} = \frac{6}{m} \quad \text{بزرگترین } x = \frac{6}{\omega} \quad f\left(\frac{6}{m}\right) = 2$$

$$m\left(\frac{6}{m}\right)^2 - 12\left(\frac{6}{m}\right) + 0m - 1 = 2 \Rightarrow -\frac{36}{m} + 0m - 1 = 2$$

$$-\frac{36}{m} + 0m - 1 = 2 \quad m \text{ منفی} \quad -36 + 0m^2 = 3m \quad m = \frac{3\sqrt{9+120}}{10} = \frac{3\sqrt{129}}{10}$$

$$am^2 - 12m - 1 = 0 \quad m = \frac{12 \pm \sqrt{144+4}}{2} = \frac{12 \pm \sqrt{148}}{2} = \frac{12 \pm 2\sqrt{37}}{2} = 6 \pm \sqrt{37}$$

$$m_1 = \frac{12}{10} = 1.2 \quad m_2 = \frac{12}{10} = 1.2 \quad m > 0 \Rightarrow m = 1.2$$

$$x = \frac{6}{m} = \frac{6}{1.2} = 5 = 5$$

$$0x + 1 = -2(a+1) = -2a-2 \quad \alpha\beta = 2a-1 \quad \checkmark$$

$$a^2 = \alpha \times \beta \quad a^2 = 2a-1 \quad a^2 - 2a + 1 = 0 \quad a = 1$$

$$x^2 + 2(1+1)x + 2(1) - 1 = 0 \quad x^2 + 4x + 1 = 0$$

$$x = \frac{-4 \pm \sqrt{16-4}}{2} = \frac{-4 \pm \sqrt{12}}{2} = \frac{-4 \pm 2\sqrt{3}}{2} = -2 \pm \sqrt{3}$$

$$\alpha = -2 - \sqrt{3} \quad \beta = -2 + \sqrt{3}$$

$$q = a \quad \alpha = 1 \quad (-2 - \sqrt{3}) = (-2 + \sqrt{3}) = -2 + \sqrt{3}$$

$$q = -2 + \sqrt{3} \quad \beta = -2 + \sqrt{3} \quad \alpha = -2 - \sqrt{3} \quad \alpha = 1$$

$$y^2 - 4y + 0 = 0 \quad y = \frac{4 \pm \sqrt{16+0}}{2} = \frac{4 \pm 4}{2} = 0, 4$$

$$\frac{(4 \pm \sqrt{16})}{2} \quad \text{بزرگترین } y = \frac{4 + \sqrt{16}}{2} = \frac{4 + 4}{2} = 4 \quad y_1 > 0$$

$$x_1 = \frac{(V + \sqrt{V^2 + 9})}{2} \quad x_2 = \frac{(V - \sqrt{V^2 + 9})}{2} \quad S = x_1 + x_2 =$$

$$\frac{\sqrt{V^2 + 9}}{2} + \left(-\frac{\sqrt{V^2 + 9}}{2}\right) \quad S = 0 \quad P = x_1 \times x_2 =$$

$$\frac{\sqrt{V^2 + 9}}{2} \times \left(-\frac{\sqrt{V^2 + 9}}{2}\right) \Rightarrow P = -\frac{(V^2 + 9)}{4}$$

$$x^2 - 4x + 0 = 0 \Rightarrow x^2 - 4x = 0 \Rightarrow x(x-4) = 0 \Rightarrow x = 0, 4$$

$$x = \frac{-b}{2a} = \frac{-(-1)}{2k} = \frac{1}{2k} \quad x = \frac{1}{k} \Rightarrow y = k\left(\frac{1}{k}\right)^2 - \frac{1}{k} = \frac{1}{k} - \frac{1}{k} = 0$$

$$= \frac{1}{k} - \frac{1}{k} - 1 = -\frac{1}{k} - 1 \quad y = -\frac{1}{k} - 1 \quad -\frac{1}{k} - 1 = -\frac{1}{k} - 1 \quad -\frac{1}{k} - 1 = -\frac{1}{k} - 1$$

$$-\frac{1}{k} - 1 = -\frac{1}{k} - 1 \Rightarrow \frac{1}{k} = 2 \quad k = 2 \quad y = \frac{1}{2} - 1 = -\frac{1}{2}$$

$$= -2 - 1 = -3 \quad -\frac{1}{k} + \frac{1}{k} = -1 + 1 = 0$$

$$-m\alpha^2 + m\alpha + 1 = -m - \alpha \quad -m\alpha^2 + (m+1)\alpha + (1+m) = 0$$

$$m = 0 \Rightarrow \alpha + 1 = 0 \quad \alpha = -1 \quad m \neq 0 \quad \Delta < 0$$

$$= (m+1)^2 - 4(-m)(1+m) < 0 \quad = (m+1)^2 + 4m(1+m) < 0$$

$$= (m+1)(m+1+4m) < 0 \quad m = \frac{-1}{5} = -0.2 \quad m = -1$$

$$-0.2 < m < -1 \quad \text{مورد دوم}$$