

$1) n \in \mathbb{Z}, n^2 - an + b \quad a, b \in \mathbb{Z}$

$\Delta < 0$

$\hookrightarrow n > 3, n < 1 \rightarrow$ نیست $\begin{cases} n=1 \\ n=3 \end{cases}$ $\begin{cases} 3a+b=0 \\ a+b=0 \end{cases} \Rightarrow \begin{cases} 3a-b=9 \\ -a+b=-1 \end{cases} \Rightarrow \begin{matrix} 2a=8 \\ a=4 \end{matrix}$

$\Rightarrow a=4, b=3 \quad 4+3 = \boxed{7}$

$y = (k-2)(n+m-1)(n-3n)^2 \quad \frac{-4k}{+b} + \frac{4}{b-} \quad \frac{m}{n} + k = ?$

$3n = -1 \Rightarrow 2+n = -\frac{1}{3} \Rightarrow \frac{1-m}{n-2} = 4 \Rightarrow 4k-8 = 1-m \Rightarrow m = 9-4k$

$\Rightarrow y = (k-2)(n-4)(n+1)^2 \Rightarrow m=5, k=1, n=-\frac{1}{3} \Rightarrow (5, (-\frac{1}{3}), 1) = \boxed{19}$

$\boxed{-14}$

$y = -\frac{1}{2}n^2 + 2n + 6 \quad (a, b) \rightarrow \frac{7}{2}$

$-\frac{1}{2}n^2 + 2n + 6 > \frac{7}{2} \Rightarrow -n^2 + 4n + 7 > 7 \Rightarrow -n^2 + 4n + 5 > 0$

$\frac{-4 \pm \sqrt{16+20}}{-2} = \begin{cases} \frac{4-6}{-2} = 5 \rightarrow b \\ \frac{4+6}{-2} = -1 \rightarrow a \end{cases} \text{ max } b-a \rightarrow 5 - (-1) = \boxed{6}$

$f(n) = n^3 - 3n^2 + n + 3 = (n+1)(n-1)(n-3)$

$\Rightarrow (1, 3) \text{ نیست } \Rightarrow f(2) = 8 - 12 - 2 + 3 = \boxed{-3}$

$(a-1)n^2 + (a-1)n + 1 \rightarrow$ نیست $a-1 < 0 \Rightarrow a < 1$

$\Delta < 0 \Rightarrow a^2 - 2a + 1 - 4a + 4 < 0 \Rightarrow a^2 - 6a + 5 < 0 \Rightarrow (a-1)(a-5) < 0$

$\frac{1}{-} \frac{5}{+} \Rightarrow a \in (1, 5) \quad \frac{1}{-} \Rightarrow \emptyset$

$$\frac{m(m^3+m)}{m-2} > 0 \Rightarrow \frac{m(m^2+1)}{m-2} > 0 \Rightarrow \frac{m^2(m^2+1)}{m-2} > 0 \Rightarrow \frac{+}{-} \frac{+}{-} \frac{+}{+}$$

$$\Rightarrow m \in (2, +\infty)$$

9

$$\frac{(n^2-2n-6)(n-1)^2}{(n^2+n+1)(2-n)^3} \leq 0 \Rightarrow \frac{(n-3)(n-2)(n-1)^2}{(n^2+n+1)(2-n)^3}$$

$\Delta < 0$ (discriminant)

$$\Rightarrow \frac{+}{+} \frac{+}{+} \frac{+}{-} \frac{+}{-} = (-\infty, 2) \cup (3, +\infty)$$

10

for $f(x) = \frac{3x^2-2x}{x^2+4}$ (a, b) $y=2$

$3x^2-2x \geq 2(x^2+4) \Rightarrow x^2-2x-8 < 0 \Rightarrow \frac{2 \pm \sqrt{4+32}}{2} < \frac{8}{2} = 4 \rightarrow b$
 $\frac{-4}{2} = -2 \rightarrow a$

$b-a = 4 - (-2) = 6$

11

$$-1 < \frac{3n^2-4n}{n+1} < 0 \Rightarrow \frac{3n^2-4n}{n+1} + \frac{n+1}{n+1} > 0 \Rightarrow \frac{3n^2-3n+1}{n+1} > 0$$

$$\Rightarrow \frac{-1}{-} \frac{+}{+} \Rightarrow (-1, +\infty)$$

12

$$\frac{3n^2-4n}{n+1} < 0 \Rightarrow \frac{n(3n-4)}{n+1} < 0 \Rightarrow \frac{-1}{-} \frac{0}{+} \frac{4}{+} \Rightarrow (-\infty, -1) \cup (0, \frac{4}{3})$$

$$\text{①} \cap \text{②} \Rightarrow (0, \frac{4}{3})$$

$$\frac{n^2-10}{n} < 3 \Rightarrow \frac{n^2-10}{n} - 3 < 0 \Rightarrow \frac{n^2-10-3n}{n} < 0 \Rightarrow \frac{(n+2)(n-5)}{n} < 0$$

$$\Rightarrow \frac{-}{-} \frac{+}{+} \frac{-}{+} \Rightarrow (-\infty, -2] \cup (0, 5]$$

13