

$$f(x) \begin{cases} x^2 + 2x & ; x \geq a \\ a x - 2 & ; x \leq a \end{cases} \Rightarrow x=a \quad a^2 + 2a = a^2 - 2 \Rightarrow 2a = -2$$

$$\boxed{a = -2}$$

-2

$$g(x) = f(x) \Rightarrow f + b = \frac{f + a}{f - b} = 2 \Rightarrow f + b = 2 \Rightarrow b = -1$$

$$\Rightarrow \frac{f + a}{a} = 2 \Rightarrow f + a = 2a \Rightarrow a = 1 \Rightarrow f(1) = \frac{1^2}{2} = \boxed{2}$$

-3

$$f(x) = \frac{f(x+1)}{2x^2 + ax + b}$$

$$2x^2 + ax + b \Rightarrow 2 - a + b = 0$$

$$\Rightarrow 2 + a + b = 0$$

$$\Rightarrow 2 + a = 0 \Rightarrow a = -2$$

$$b = -1$$

$$f(1) = \frac{a}{2 + (-2) + (-1)} = \frac{a}{-1}$$

$$f(x) = \frac{x^2 - \sqrt{3}}{-f(x+1)^2}$$

$$-f(x+1)^2 \Rightarrow -f - a + b = 0$$

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$$f(x^2 + 2x + 1) = -f(x^2 - 1) = -f(x^2 + ax + b) \Rightarrow a = -1$$

$$(x^2 + mx + 1) \Rightarrow a + b = -12 \quad b = -1$$

$$m^2 - 1 < 0 \Rightarrow -1 < m < 1$$

$$m^2 - 1 = 0 \Rightarrow m = -1$$

$$\frac{-b \pm \sqrt{\Delta}}{2a} = \frac{-m}{2} = 1 \Rightarrow m = -2$$

$$\boxed{-2 \leq m < 1}$$

-6 چون زیر رادیکال هست

$$f(x) = \sqrt{f - \frac{1}{x^2}} \Rightarrow f - \frac{1}{x^2} \geq 0 \Rightarrow f \geq \frac{1}{x^2}$$

$$D(f) = (-\infty, -\frac{1}{\sqrt{f}}] \cup [\frac{1}{\sqrt{f}}, +\infty)$$

$\frac{1}{x^2} \leq x^2 \Rightarrow \frac{1}{x} \leq x$

$$m x^2 + r m x + 1 \geq 0 \Rightarrow a > 0 \Rightarrow m > 0$$

$$\Delta \leq 0 \Rightarrow f m^2 - f m \leq 0 \Rightarrow 0 < m \leq 1$$

$$\xrightarrow{x=1} \frac{1}{r} \quad 1 + 1 = r + k \Rightarrow k = 0 \quad a + k = \frac{1}{r}$$

$$\frac{f x^2 - 1}{r x - 1} \xrightarrow{x=1} \frac{0}{0} \Rightarrow x \neq a \Rightarrow x \neq \frac{1}{r}$$

$$\Rightarrow a = \frac{1}{r}$$

$$f(x) = \begin{cases} \frac{a x^2 - r}{r x + r} ; x \neq -\frac{r}{r} \Rightarrow \frac{a - r}{a} = 1 = r + b \Rightarrow = -r & -9 \\ r a x + r ; x = -\frac{r}{r} \end{cases} \quad g(x) = r x + b$$

$$r a x - \frac{r}{r} + r \Rightarrow r - a = -r + b \Rightarrow r a + b = r \Rightarrow r a = r$$

$$a = r$$

$$a - b = r - (-r) = 2r$$

$$f(x) = \begin{cases} \frac{x^2 - r}{x - r} ; x \neq r \\ r a^2 + a x ; x = r \end{cases} \quad g(x) = x + r \quad -10$$

$$\xrightarrow{x=r} r a^2 + r a = r$$

$$\Rightarrow a^2 + a = 1 \Rightarrow a = 1$$