

$\frac{\sin \frac{\pi}{r}}{1 + \cos \frac{\pi}{r}} = \frac{1}{\sin \frac{\pi}{r}} + \cot \frac{\pi}{r} = \frac{1}{\sin \frac{\pi}{r}} + \frac{\cos \frac{\pi}{r}}{\sin \frac{\pi}{r}} = \frac{1 + \cos \frac{\pi}{r}}{\sin \frac{\pi}{r}}$ $\hookrightarrow \frac{\sin \frac{\pi}{r}}{1 + \cos \frac{\pi}{r}} = \frac{1 + \cos \frac{\pi}{r}}{\sin \frac{\pi}{r}} \Rightarrow \tan \frac{\pi}{r} = \frac{1}{\tan \frac{\pi}{r}} \Rightarrow \tan^2 \frac{\pi}{r} = 1 \Rightarrow \tan \frac{\pi}{r} = \pm 1$ $\Rightarrow \frac{\pi}{r} = \frac{K\pi}{r} + \frac{\pi}{r} \Rightarrow \frac{\pi}{r} = K\pi + \frac{\pi}{r} \cdot \overline{00} \Rightarrow x = 2K\pi + \pi \rightarrow x = -\pi, \pi$ $\Rightarrow \frac{\pi}{r} = \frac{K\pi}{r} + \frac{\pi}{r} \Rightarrow \frac{\pi}{r} = K\pi + \frac{\pi}{r} \cdot \overline{00} \Rightarrow x = 2K\pi + \pi \rightarrow x = -\pi, \pi$ $\Rightarrow \frac{\pi}{r} = \frac{K\pi}{r} + \frac{\pi}{r} \Rightarrow \frac{\pi}{r} = K\pi + \frac{\pi}{r} \cdot \overline{00} \Rightarrow x = 2K\pi + \pi \rightarrow x = -\pi, \pi$	9
$\cos^2 x - \sin^2 x \cos^2 x = 1 \Rightarrow \cos^2 x - 1 - \sin^2 x \cos^2 x = 0$ $-\sin^2 x (1 + \cos^2 x) = 0$ $\Rightarrow \sin x = 0 \Rightarrow x = K\pi \Rightarrow x = 0, \pi, 2\pi$ $\Rightarrow 1 + \cos^2 x = 0 \Rightarrow \cos^2 x = -1 \Rightarrow x = 2K\pi + \pi \Rightarrow x = \frac{\pi}{r}, \frac{3\pi}{r}$	7
$\frac{1 - \tan x}{1 + \tan x} = \tan \pi x \Rightarrow \tan\left(\frac{\pi}{2} - x\right) = \tan \pi x \Rightarrow \pi x = K\pi + \frac{\pi}{2} - x$ $\frac{1 - \tan x}{1 + \tan x} = \frac{\tan \frac{\pi}{2} - \tan x}{1 + \tan \frac{\pi}{2} \tan x}$ $x = K\pi + \frac{\pi}{2}$ $x = K\pi + \frac{\pi}{2} \rightarrow \overline{00}$	1
$\sqrt{1 + \sin^2 x} = \sqrt{r} \cos^2 x \rightarrow \sqrt{1 + \sin^2 x} \cos x = \sqrt{r} (\cos^2 x - \sin^2 x) \Rightarrow \cos x + \sin x = \sqrt{r} (\cos^2 x - \sin^2 x)$ $ \cos x + \sin x \neq 0 \Rightarrow \sqrt{r} \cos x - \sin x = 1 \Rightarrow \sqrt{r} \sin x - \cos x = 1$ $\sin x - \cos x = \sqrt{r} \sin\left(x - \frac{\pi}{4}\right) \hookrightarrow \sqrt{r} \left \sqrt{r} \sin\left(x - \frac{\pi}{4}\right) \right = 1 \Rightarrow \left \sin\left(x - \frac{\pi}{4}\right) \right = \frac{1}{r}$ $\left \sin\left(x - \frac{\pi}{4}\right) \right = \frac{1}{r} \Rightarrow \sin\left(x - \frac{\pi}{4}\right) = \pm \frac{1}{r} \Rightarrow x - \frac{\pi}{4} = K\pi \pm \frac{\pi}{4} \Rightarrow x = K\pi \pm \frac{\pi}{2}$	9
الف) $\sin^2 x - \cos^2 x = 1$ $(\sin^2 x - \cos^2 x)(\sin^2 x + \cos^2 x) = 1$ $\hookrightarrow \sin^2 x - \cos^2 x = 1$ $-\cos^2 x = 1 \Rightarrow \cos^2 x = -1$ $x = 2K\pi + \pi$ $x = K\pi + \frac{\pi}{2}$ ب) $\sin^2 x - \cos^2 x = -1$ $x = 0 \Rightarrow 0 - 1 = -1 \checkmark$ $x = \frac{\pi}{2} \Rightarrow 1 - 0 = 1 \times$ $x = \pi \Rightarrow 0 - (-1) = 1 \times$ $x = \frac{3\pi}{2} \Rightarrow -1 - 0 = -1 \checkmark$ $x = 2\pi \Rightarrow 0 - 1 = -1 \checkmark$ $x = \pi, \frac{3\pi}{2}, 0$	10