

جواب

$$\lim_{x \rightarrow 0} \frac{x^2 - 1}{x - 1} = \frac{0 - 1}{0 - 1} = 1 \Rightarrow x^2 + ax + b = (x - 1)^2 = x^2 - 2x + 1 \Rightarrow a + b = -2 + 1 = -1$$

$$\lim_{x \rightarrow \infty} \frac{x^2 - 1}{x - 1} = \frac{\infty - 1}{\infty - 1} = \frac{\infty}{\infty} \Rightarrow x^2 + ax + b = (x - \sqrt{x})^2 = x^2 - 2\sqrt{x} + x \Rightarrow \left[ \frac{b}{a} \right] = \left[ \frac{\sqrt{x}}{-\sqrt{x}} \right] = \left[ \frac{\sqrt{x}}{-\sqrt{x}} \right] = \left[ \frac{-1}{1} \right] = -1$$

$$\lim_{x \rightarrow \infty} \frac{\left[ \frac{-1}{1} \right] + a}{\left[ \frac{\sqrt{x}}{-\sqrt{x}} \right] + a} = -\infty \Rightarrow \frac{a - 1}{a + 1} = -\infty$$

$\Rightarrow \lim_{x \rightarrow \infty} \frac{a + 1}{a - 1} = 0 \Rightarrow a = -1 \Rightarrow [a] = -1$

$a < 0 \Rightarrow \frac{a - 1}{a + 1} = -\infty$   
 $a > 0 \Rightarrow \frac{a - 1}{a + 1} = \infty$

$$\Rightarrow \frac{14n + 1 \left[ \frac{1}{n^p} \right]}{18 + 1 \left[ \frac{1}{n^p} \right]} = \frac{1(14n + \left[ \frac{1}{n^p} \right])}{1(14n + \left[ \frac{1}{n^p} \right])} = \frac{1}{1}$$

-8

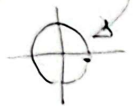
$$\lim_{n \rightarrow p^+} \frac{n^p - 8}{n^p - \left[ \frac{1}{n^p} \right]} = \frac{(n-1)(n+1)}{(n-1)(n^p + 1/n)} = \frac{1}{1+0+0} = \frac{1}{1} = \frac{1}{1} = \frac{1}{1}$$

-8

$$\Rightarrow \frac{14n+10}{9n^p} = \frac{14n+1}{9n^p} \Rightarrow \lim_{n \rightarrow -1} \frac{14n+1}{9n^p} = \frac{-9}{9 \sqrt[3]{9}} = \frac{-1}{\sqrt[3]{9}} = -\frac{1}{\sqrt[3]{9}}$$

-4

$$\lim_{\alpha \rightarrow 0^-} \frac{\sqrt{1+\alpha} - \sqrt{1-\alpha}}{\sqrt{1-\cos \alpha}}$$



$$\cos \alpha = 1 - \frac{\alpha^2}{2} \Rightarrow \frac{1}{2} \frac{\alpha^2}{1}$$

$$\lim_{\alpha \rightarrow 0^-} \frac{\sqrt{1+\alpha} - \sqrt{1-\alpha}}{\sqrt{1-\cos \alpha}} \rightarrow \frac{\sqrt{1+\alpha} - \sqrt{1-\alpha}}{\sqrt{1-\cos \alpha}} \rightarrow \frac{\sqrt{1+\alpha} - \sqrt{1-\alpha}}{\sqrt{1-\cos \alpha}}$$

$$\frac{\sqrt{1+\alpha}}{\alpha} \rightarrow \frac{1}{\sqrt{1+\alpha}} = \frac{1}{\sqrt{1}} = 1$$

$$f'(\alpha) = \frac{1}{\sqrt{1+\alpha}} - \frac{-1}{\sqrt{1-\alpha}} \Rightarrow \frac{1}{\sqrt{1}} = 1$$

$$\frac{\alpha \sqrt{1+\alpha}}{-\alpha \sqrt{1-\alpha}} = -1$$

-U

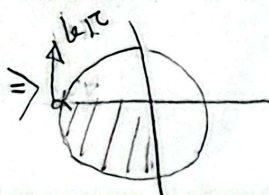
$$\lim_{n \rightarrow \infty} \frac{k + 1 - \frac{a n^p}{p}}{k n^p} = p \Rightarrow \frac{p k + p - a n^p}{p k n^p} = p \xrightarrow{\text{hoplim}} \frac{-p a n^p}{p k n^p} \Rightarrow \lim_{n \rightarrow \infty} \frac{-a}{k} = p - 1$$

$$\Rightarrow \frac{a}{k} = p(p-1) = -9$$

$$\lim_{n \rightarrow \infty} \frac{p \sqrt{n-1/a} + p \sqrt{n} - p \sqrt{1/a}}{\sqrt{(n-1/a)(n+1/a)}} \Rightarrow \frac{(\sqrt{n} - \sqrt{1/a})^p}{p \sqrt{n} - p \sqrt{1/a}} = \frac{\sqrt{n^p} + \sqrt{p} \sqrt{a} \sqrt{n} \sqrt{1/a} + 1/a \sqrt{n}}{(n-1/a)^{p/2} + 1/a \sqrt{n}}$$

$$\Rightarrow \frac{(n-1/a)^{p/2} + p \sqrt{n-1/a}}{\sqrt{1/a} + \sqrt{n}} \Rightarrow \frac{(\sqrt{n-1/a})^p}{\sqrt{1/a} + \sqrt{n}} \Rightarrow \frac{p}{\sqrt{1/a}}$$

$$\lim_{n \rightarrow -1} \frac{1 - k[n]}{n^p - 1} = -\infty$$



$$\begin{aligned} n \rightarrow -1^+ & \quad 1+k < -\infty \Rightarrow k+1 < 0 \Rightarrow k < -1 \\ n \rightarrow -1^- & \quad 1+k > -\infty \Rightarrow p k + 1 < 0 \Rightarrow p k < -1 \Rightarrow k < -1/p \end{aligned}$$

$\Rightarrow \frac{-1}{k} < -\frac{1}{p}$

Unit circle diagram for  $\cos R = -1$  at  $R = \pi$ .