

المسألة الأولى: إيجاد القيمة القصوى والدنيا لـ $f(x) = 1 - \frac{a}{x}$ في الفترة $[1, 4]$

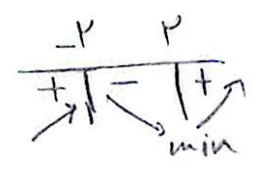
$$① \frac{f(4) - f(1)}{4 - 1} = \frac{(1 - \frac{a}{4}) - (1 - a)}{3} = \frac{\frac{3}{4}a}{3} = \frac{a}{4}$$

$$f(x) = 1 - \frac{a}{x} \Rightarrow f' = \frac{a}{x^2} \rightarrow \frac{a}{x^2} = \frac{a}{x^2} \rightarrow x = \pm \sqrt{x} \xrightarrow{x \in [1, 4]} \boxed{x = \sqrt{4}}$$

$$② y = -x \Rightarrow \lambda a x^r - \Delta x + \lambda a = -x \rightarrow \lambda a x^r - \lambda x + \lambda a = 0$$

$$\Delta = 0 \rightarrow 14 - 144a^2 \rightarrow 14 = 144a^2 \rightarrow a^2 = \frac{1}{9} \rightarrow a = \pm \frac{1}{3} \rightarrow \boxed{a = -\frac{1}{3}}$$

$$③ y = x^r - 11x + 1 \rightarrow r x^{r-1} - 11 = 0 \rightarrow x = \pm r$$



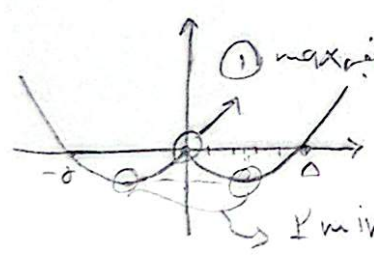
④ القيمة الدنيا

$$④ y = x^r + a x^r - r b x - c \rightarrow r x^{r-1} + r a x - r b \stackrel{=0}{\rightarrow} \boxed{b=0}$$

$$\downarrow x^r - r x^{r-1} - c / -A = -r - c = \boxed{x = -r} \quad r - c a = \rightarrow \boxed{x = r}$$

$$(0, -c) \quad (-r, -r-c) \rightarrow \sqrt{r^2 + 4r-c} = \sqrt{4r-c} = r \sqrt{4r-c}$$

$$⑤ f(x) = x^r - a|x| \xrightarrow{a=b} ① x=0, ② x^r - \Delta x \rightarrow \boxed{x = \Delta}, \boxed{x = 0}$$



$$① \max_{x \in \mathbb{R}} = \frac{-b}{2a} = \frac{\Delta}{r} = \frac{r}{r} = 1 \quad + \frac{r}{c} - \frac{0}{c} = -\frac{r}{c} = -\frac{r}{c}$$

$$\rightarrow \frac{a}{m} = \frac{r}{c}$$

⑥

(v) $0 \leq x \leq a \xrightarrow{-a} -a \leq x-a \leq 0 \rightarrow |x-a| = a-x$

$f(x) = \sqrt[p]{x^r} (a-x) = ax^{\frac{r}{p}} - x^{\frac{r+p}{p}} \rightarrow f'(x) = \frac{r}{p} ax^{\frac{r}{p}-1} - \frac{r+p}{p} x^{\frac{r+p}{p}-1} = \frac{r}{p} x^{\frac{r}{p}-1} (a - \frac{r+p}{r} x)$

$f'(x) = \frac{r(a - \frac{r+p}{r}x)}{p \sqrt[p]{x^{r+p}}}$ *نقطه بحر:* $a=x, x=0, x = \frac{r}{r+p}a$ $f(a), f(0) = 0$

$f(\frac{r}{r+p}a) = 1/\Delta \rightarrow \sqrt[p]{(\frac{r}{r+p}a)^r} (a - \frac{r}{r+p}a) = \frac{r}{p} \xrightarrow{p \cdot \Delta} \frac{r}{r+p} a^r \times \frac{r}{r+p} a^p = \frac{r^2}{\Delta}$

$\frac{\Sigma a^p}{r \Delta \times 1/\Delta} = \frac{1}{\Delta} \rightarrow a^p = \frac{r \Delta \times 1/\Delta}{\Sigma \times 1} = \frac{\Delta^p}{r \Delta} \rightarrow \boxed{a = \frac{\Delta}{r} = r/\Delta}$

(^)

(9) $y = \frac{mx+r}{x-1+m} \rightarrow y' = \frac{m(m-1)-r}{(x-1+m)^2} = \frac{m^2-m-r}{(x-1+m)^2} \ll 0 \rightarrow m^2-m-r \ll 0 \rightarrow -1 \ll m \ll r$

$1-m \ll 1 \rightarrow 0 \ll m \Rightarrow 0 \ll m \ll r \rightarrow \boxed{m=1}, \boxed{m=0}$

(10)