

$$\frac{f(x) - f(x_0)}{x - x_0} \approx f'(x_0)$$

$$\frac{1 - \frac{a}{x} - 1 + a}{x} = \frac{a}{x^2}$$

$$\frac{a}{x} = \frac{a}{x^2} \rightarrow x = \pm \sqrt{a}$$

۱

$$f'(x) = 1 \rightarrow \tan^{-1} x = 1 \rightarrow x = \frac{1}{\tan 1} = \frac{1}{\tan 1}$$

$$\frac{1}{\tan 1} = \frac{1}{\frac{\sin 1}{\cos 1}} = \frac{\cos 1}{\sin 1} = \cot 1$$

۲

$$y = \frac{1}{x} \rightarrow y' = -\frac{1}{x^2}$$

x	$-\sqrt{1}$	$+\sqrt{1}$
y'	$+$	$-$
y	\nearrow	\searrow

$$\min_{x \in \mathbb{R}} \left| \frac{1}{x} - 1 \right| = \min_{x \in \mathbb{R}} \left| \frac{1-x}{x} \right|$$

۳

$$y' = \frac{1}{x^2} + \tan x - 1 = 0 \rightarrow \frac{1}{x^2} = 1 - \tan x \rightarrow 1 - \tan x > 0 \rightarrow \tan x < 1 \rightarrow x < \frac{\pi}{4}$$

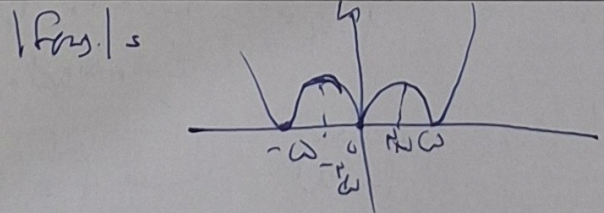
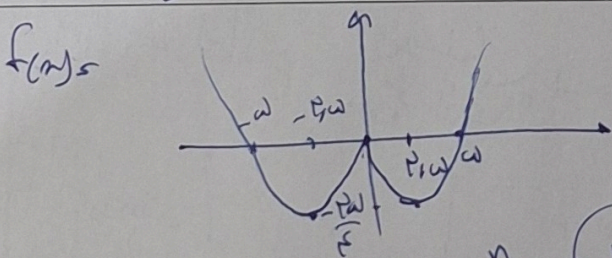
x	$-\frac{\pi}{4}$	0
y'	$+$	$-$
y	\nearrow	\searrow

$$A \begin{vmatrix} -1 \\ 0 \end{vmatrix}$$

$$B \begin{vmatrix} 0 \\ -1 \end{vmatrix}$$

$$\sqrt{(0-0)^2 + (-1-0)^2} = \sqrt{1} = 1$$

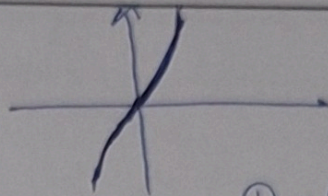
۴



$$\frac{n}{m} = \frac{1}{1}$$

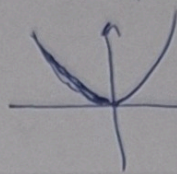
۵

f_{ms} $\begin{cases} \rightarrow n \neq 0 & n^2 + 1 & 1/2 \\ \rightarrow n = 0 & -n^2 + 1 & 1/2 \end{cases}$



نقطه بحرانی: $n=0$

$|f_{ms}|$ $\begin{cases} \rightarrow n \neq 0 & n^2 + 1 & 1 \\ \rightarrow n = 0 & n^2 - 1 & 1 \end{cases}$



① $\rightarrow f'_{s0} \rightarrow$ $\frac{d}{dx}(x^2+1) = 2x$
 ② $\rightarrow f'_{s0} \rightarrow$ $\frac{d}{dx}(-x^2+1) = -2x$
 $n=0 \rightarrow f'_{s0} = 0$ \rightarrow $f'_{s0} = -2x$ \rightarrow $x=0$

$[0, a] \rightarrow f_{ms} = (a-n)^m \sqrt[n]{n} \rightarrow 0 \text{ و } 1 \rightarrow$ f'_{s0} \rightarrow $\frac{d}{dx} f_{ms}$ \rightarrow $\frac{d}{dx} (a-n)^m \sqrt[n]{n}$

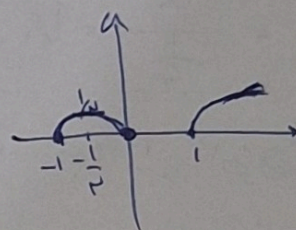
$f'_{s0} = \sqrt[n]{n} + (a-n) \frac{1}{n^2} \sqrt[n]{n} \rightarrow$ $\frac{d}{dx} (a-n)^m \sqrt[n]{n} \rightarrow$ $\frac{d}{dx} (a-n)^m \cdot \frac{1}{n^2} \sqrt[n]{n} + (a-n)^m \cdot \frac{1}{n^2} \sqrt[n]{n}$

$n \frac{1}{\omega} a \rightarrow \frac{1}{\omega} a \sqrt[n]{\frac{1}{\omega}} \cdot a \frac{1}{\omega} = \frac{1}{\omega} \rightarrow \sqrt[n]{\frac{1}{\omega}} \cdot a \frac{1}{\omega} = a \frac{1}{\omega} \cdot \frac{1}{\omega} = \frac{1}{\omega^2} \cdot a$

$f_{ms} \begin{cases} \rightarrow n \neq 0 & \sqrt[n]{n^2 - n} \\ \rightarrow n = 0 & \sqrt[n]{-n^2 - n} \end{cases}$

$\frac{d}{dx} \sqrt[n]{n^2 - n} = \frac{1}{n^2} \sqrt[n]{n^2 - n}$

$\frac{d}{dx} \sqrt[n]{-n^2 - n} = \frac{1}{n^2} \sqrt[n]{-n^2 - n}$



$m \rightarrow 1$
 $n = 0$ $R = F$ $\frac{R_{m+n}}{R-n} = 1$

$ad - bc < 0 \rightarrow m^2 - m - 1 < 0 \rightarrow \frac{1}{2} \pm \sqrt{\frac{1}{4} + 1} = \frac{1}{2} \pm \frac{\sqrt{5}}{2} \rightarrow -1 < m < 2$

$m = 0 \text{ و } 1 \rightarrow$ $\frac{d}{dx} f_{ms}$

$f_{ms} \rightarrow n \neq 0 \rightarrow \frac{n}{1-n^2} \rightarrow [0, +\infty) \rightarrow f'_{s0} = \frac{n^2 + 1}{(1-n^2)^2} \rightarrow \begin{vmatrix} 0 & 1 & 0 \\ -1 & 0 & 1 \end{vmatrix}$

$n = 0 \rightarrow \frac{n}{1+n^2}$

$f'_{s0} = \frac{n^2 + 1}{(1+n^2)^2} \rightarrow \begin{vmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \end{vmatrix}$

$n = 0 \rightarrow f'_{s0} = \frac{1}{1}$
 $f'_{s-} = 1$

$n = 1 \rightarrow \frac{1+1}{(1+1)^2} = \frac{2}{4} = \frac{1}{2}$