

$R_f = \mathbb{Z}^2 \times \mathbb{Z}$

$$f(n) = \frac{n^2 - n + \frac{1}{2}}{n^2 - n + 1}$$

$$n^2 - n + 1 \neq 0 \quad D_f = \mathbb{R}$$

$$R_f = (0, 1) \cup \dots$$

$$-y^2 + y \geq 0 \Rightarrow y \in [0, 1]$$

$$y n^2 - y n + y = n^2 - n + \frac{1}{2} \Rightarrow (1-y) n^2 + (y-1) n + \frac{1}{2} - y = 0$$

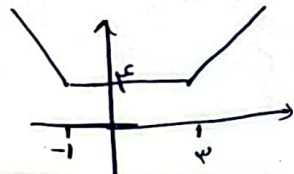
$$\Delta = (y-1)^2 - 4(1-y)\left(\frac{1}{2} - y\right) = -4y^2 + 4y \quad n = \frac{-(y-1) \pm \sqrt{4y^2 - 4y}}{2(1-y)} \rightarrow y \neq 1$$

الف)
$$\begin{cases} n+1 & n \geq 3 \\ 3n-4 & 1 < n < 3 \\ -n-1 & n \leq 1 \end{cases}$$

$$R_f = [-2, +\infty)$$



ب)
$$\begin{cases} 2n-2 & n \geq 3 \\ 2 & 1 < n < 3 \\ -2n+2 & n \leq 1 \end{cases}$$

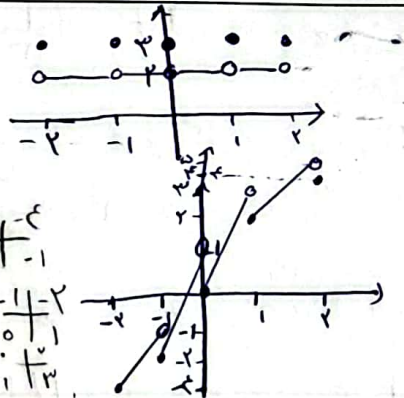


$$R_f = [2, +\infty)$$

$n+2$	$-2n$	$-n-2$
$n+2 \leq 1$	$-2n \leq 1$	$-n-2 \leq 1$
$n \leq -3$	$-2n \geq \frac{1}{2}$	$-4 \leq n$
	$\frac{1}{2} \leq n \leq 3$	$2 \leq n$

$$(-\infty, -3] \cup [\frac{1}{2}, +\infty)$$

الف) $f(n) = \lfloor n \rfloor + \lfloor -n \rfloor + 2$



$$R_f = \{2\}$$

ب) $f(n) = \lfloor n \rfloor$

$$-2 \leq n < -1 \Rightarrow y = 2n + 2$$

$$-1 \leq n < 0 \Rightarrow y = 2n + 1$$

$$0 \leq n < 1 \Rightarrow y = 2n$$

$$1 \leq n < 2 \Rightarrow y = 2n - 1$$

$$n = 2 \Rightarrow y = 2$$

$$R_f = (-\infty, 2)$$

الف)
$$\sin \begin{cases} 1 & 0 \leq x < \frac{\pi}{2} \\ -1 & \frac{\pi}{2} \leq x < \pi \end{cases}$$

$$R_f = [-1, 1]$$

ب)
$$\sin^2 \begin{cases} 1 & 0 \leq x < \frac{\pi}{2} \\ 0 & \frac{\pi}{2} \leq x < \pi \end{cases}$$

$$R_f = [0, 1]$$