

$$y = \frac{x^2 + x + 1}{x - 1} \Rightarrow yx - y = x^2 + x + 1 \Rightarrow x^2 + x(1 - y) + (1 + y) = 0 \Rightarrow x = \frac{-b \pm \sqrt{\Delta}}{2a}$$

$$x = \frac{-(1-y) \pm \sqrt{(1-y)^2 - 4(1+y)}}{2} \Rightarrow 1 - y + y^2 - 4 - 4y > 0 \Rightarrow y^2 - 5y - 3 > 0 \Rightarrow \frac{-1}{2} < y < \frac{1}{2}$$

$$R_f(-\infty, -1] \cup \{1, +\infty\} \quad (y-1)(y+1)$$

$$\text{ج) } y = \frac{x^2 - 2x + 1}{x - 1} \quad x_s = \frac{2}{1}, \quad y_s = \frac{x^2 - 2x + 1}{x - 1} \Rightarrow \frac{x^2 - 2x + 1}{x - 1} = 1 \Rightarrow x^2 - 2x = 0 \Rightarrow x(x-2) = 0 \Rightarrow x = 0, 2$$

$$R_f\left[-\frac{1}{2}, +\infty\right) \quad \frac{1}{x} = \frac{2}{1} \Rightarrow x = \frac{1}{2}$$

$$\rightarrow y = \sqrt{-x^2 + 4x - 4} \quad x_s = \frac{-4}{-1} = 4, \quad y_s = -4 + 16 - 4 = 8 \quad R_f\left[\sqrt{-4}, 4\right] = [0, 4]$$

$$\text{ج) } y = \sqrt{x^2 - 2x + 1} \Rightarrow R_f\left[\sqrt{R} = \{0, +\infty\}\right]$$

10

$$\rightarrow \log(x^2 - 4x + 1) \Rightarrow R_f(-\infty, +\infty)$$

$$\text{الف) } y = \frac{x^2 + 1}{x - 1} \Rightarrow R_f: R - \left\{\frac{1}{1}\right\} \quad (1^2)$$

15

$$\rightarrow y = \sqrt{\frac{x^2 + 1}{x - 1}} \Rightarrow R_f: \sqrt{R - \{1\}} = [0, +\infty) - \{1\}$$

$$\text{ج) } y = \frac{x^2 + 1}{\sqrt{x^2 + 1}} \Rightarrow \frac{x^2 + 1}{\sqrt{x^2 + 1}} = \frac{x^2 + 1}{\sqrt{x^2 + 1}} + \frac{1}{\sqrt{x^2 + 1}} \Rightarrow \sqrt{x^2 + 1} + \frac{1}{\sqrt{x^2 + 1}} \Rightarrow R_f\left[\frac{1}{\sqrt{2}}, +\infty\right)$$

$$\rightarrow y = \frac{x^2 + 1}{x^2 + 1} \Rightarrow \frac{x^2 + 1}{x^2 + 1} = 1 \Rightarrow x^2 + 1 = x^2 + 1 \Rightarrow 1 = 1 \Rightarrow R_f\left[\frac{1}{2}, +\infty\right)$$

$$y = \frac{x^2 + 1}{x^2 - 1} \Rightarrow \textcircled{1} \quad yx^2 - y = x^2 + 1 \Rightarrow x^2(y - 1) = 1 + y \Rightarrow x = \sqrt{\frac{1+y}{y-1}} \quad \left(\frac{1}{y-1} > 0\right)$$

$$\textcircled{2} \quad \lim_{x \rightarrow -1} \frac{1}{x^2 - 1} = -\frac{1}{2}, \quad \lim_{x \rightarrow 0} \frac{1}{x^2 - 1} = -1 \Rightarrow R_f(-\infty, -\frac{1}{2}] \cup (1, +\infty)$$

25

$$y = \frac{x \sin x - 1}{\sin x + 1} \Rightarrow \textcircled{1} \quad y \sin x + y = x \sin x - 1 \Rightarrow \sin x (x - y) = y + 1$$

(a)

$$\sin x = \frac{y+1}{x-y} \Rightarrow -1 \leq \frac{y+1}{x-y} \leq 1 \Rightarrow I = \frac{y+1+x-y}{x-y} \geq 0 \Rightarrow \frac{y+1}{x-y} \geq 0 \Rightarrow \frac{-1}{x-y} \geq 0$$

$$\textcircled{II} \quad \frac{y+1-x+y}{x-y} = \frac{y-1}{x-y} \leq 0 \Rightarrow \frac{1}{x-y} \leq 0 \Rightarrow R_f\left[-\frac{1}{1}, \frac{1}{1}\right]$$

30

$$\text{PAYCO} \quad \textcircled{P} \quad \sin x = 1 \Rightarrow y = \frac{1}{2} \quad \left(\frac{1}{2}\right)$$

$$\sin x = -1 \Rightarrow y = -\frac{1}{2} \quad \left(-\frac{1}{2}\right)$$

Subject:

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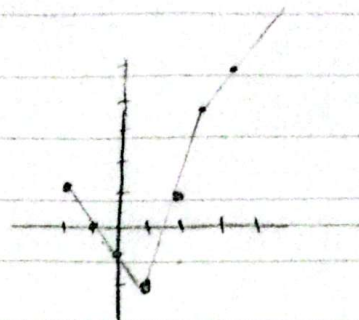
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$$f(x) = \frac{x^2 - x + \frac{1}{x}}{x^2 - x + 1} \quad R_f: yx^2 - yx + y = x^2 - x + \frac{1}{x} \rightarrow (y-1)x^2 - (y-1)x + y + \frac{1}{x} \quad (*)$$

$$x_1 = \frac{y-1}{1(y-1)} = \frac{1}{y} \quad y_1 = \frac{1}{y} \rightarrow \left\{ \frac{1}{y}, +\infty \right\}$$

5

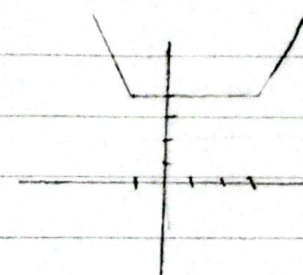
$$y = |2x-1| - |x-2| \quad \begin{cases} -x-1 & x < 1 \\ 3x-3 & 1 \leq x \leq 2 \\ x+1 & x > 2 \end{cases}$$



(V)

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$$y = |x-2| + |x+1| \quad \begin{cases} -2x+3 & x < -1 \\ 2 & -1 \leq x \leq 2 \\ 2x-1 & x > 2 \end{cases}$$



$$|x-2| - |x+1| \leq 1$$

$$\begin{aligned} -x+3 & \leq x+1 & -x+3-2x-1 & \leq 1 & x-2-2x-1 & \leq 1 \\ x+2 & \leq 1 & -3x & \leq 1 & -x-3 & \leq 1 \\ x & \leq -3 & x & \geq -\frac{1}{3} & x & \geq -2 \end{aligned}$$

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$$\left(-\infty, -3 \right] \cup \left[-\frac{1}{3}, +\infty \right)$$

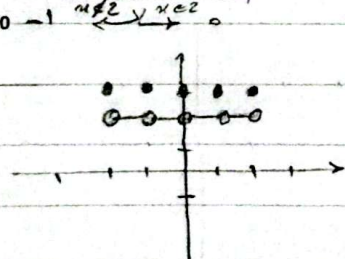
(A)

$$y = \{x\} + \{2-x\}$$

$$y = \{x\} - \{x\}$$

$$y = \{x\} + \{-x\} + 1$$

20



$$\begin{aligned} -2x & < -1 \Rightarrow 2x+1 \\ -1 & \leq x < 0 \Rightarrow 2x+1 \\ 0 & \leq x < 1 \Rightarrow 2x \\ 1 & \leq x < 2 \Rightarrow 2x-1 \\ x & \geq 2 \Rightarrow 2x-2 \end{aligned}$$



(A)

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$$y = \sin^2 x - \sin x + 1 \quad \begin{cases} \sin x = 1 & y = 1 \\ \sin x = -1 & y = 3 \\ \sin x = \frac{1}{2} & y = \frac{3}{4} \end{cases} \quad R_f = \left\{ \frac{3}{4}, 1, 3 \right\}$$

$$y = \sin^2 x + \sin x + 1 \quad \begin{cases} \sin^2 x = 1 & y = 3 \\ \sin^2 x = 0 & y = 1 \\ \sin^2 x = \frac{1}{4} & y = \frac{5}{4} \end{cases}$$

30

$$R_f = [1, 3]$$

PAYCO

