

$$f(x) \Rightarrow \text{graph}, \sqrt{-(x+r)f(x+1)} \quad \begin{matrix} -r & 0 & 1 & r \\ - & + & - & + \end{matrix} \quad (9)$$

$$-(x+r)f(x+1) \geq 0$$

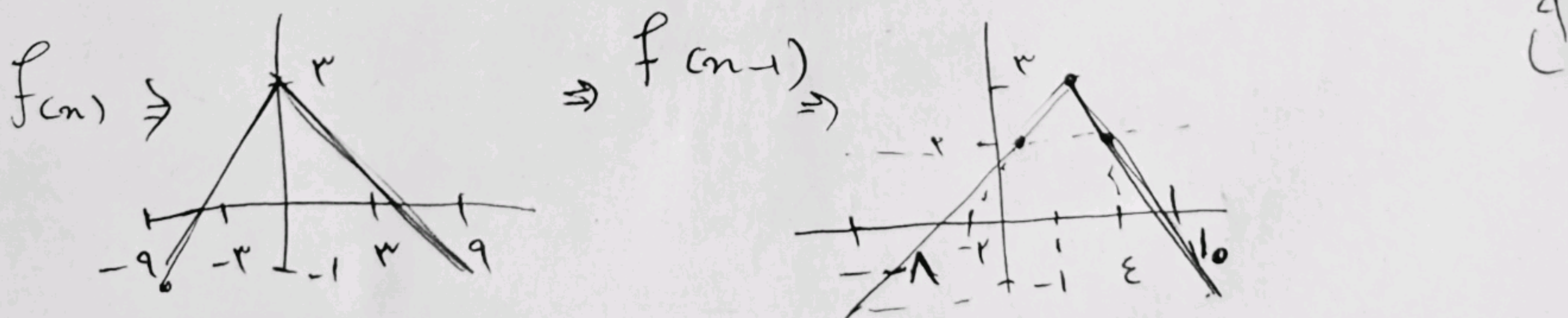
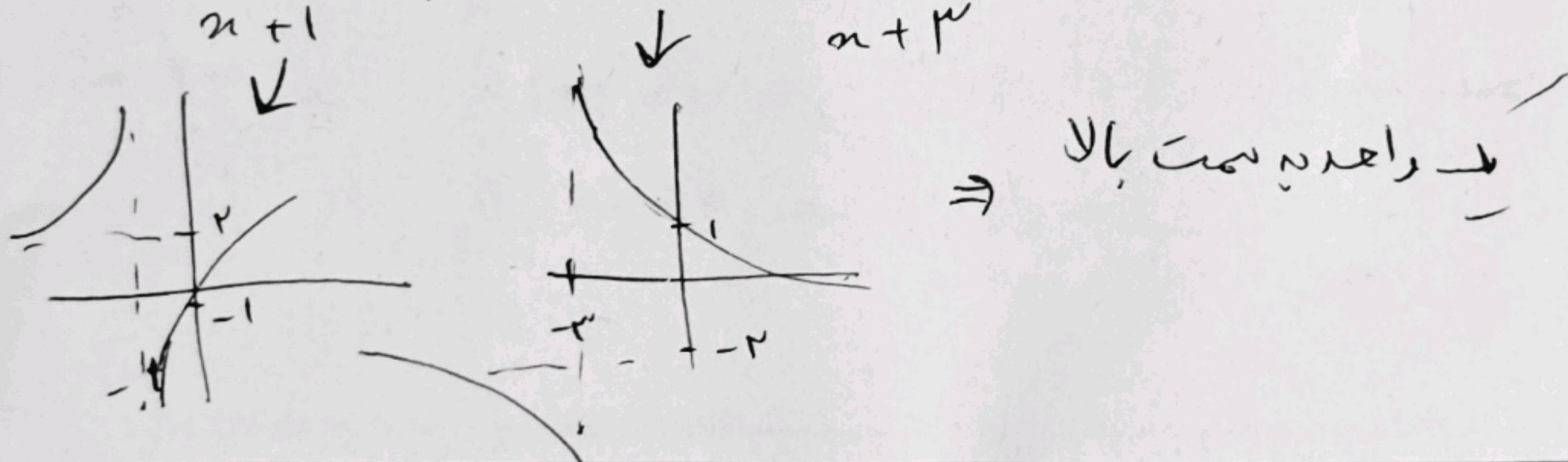
$$\Rightarrow (x+r)f(x+1) \leq 0 \Rightarrow D_f = (-\infty, -r] \cup [0, 1]$$

$$f(x) = |x-r|+1 \rightarrow g(x) = |x(r+k)-r|+1-r \quad (10)$$

$$x=0 \rightarrow |r|+1 = |rk-r|-r \Rightarrow r+r = |rk-r| \Rightarrow r = |rk-r|$$

$$\Rightarrow \begin{matrix} r = rk-r & \rightarrow k = r/a & k > 0 \\ -r = rk-r & k = -1/a \end{matrix} \rightarrow \boxed{k = r/a}$$

$$f(x) = \frac{x-1}{x+1}, \quad f'(x) = \frac{x-r}{x+r} \quad (11)$$



$$\varepsilon - (-r) = r \quad \frac{r \times 1}{r} = \boxed{r = S}$$

$$S = \frac{(a-r)^r}{r} + \frac{(a-r-(a+r)) \times \frac{r}{a}}{r} = r/a \quad (12)$$

$$\left(\frac{a-r}{r}\right)^r = \frac{1}{r} \Rightarrow a-r = 1 \Rightarrow a=r$$

$$f\left(\frac{1}{a}\right) = \left|\frac{1}{r}-r\right|-r = \boxed{\frac{r}{r}}$$

الف) $-1 \leq x \leq 1 \Rightarrow -1 \leq 2x - 1 \leq 1 \Rightarrow D' = [-1, 1]$

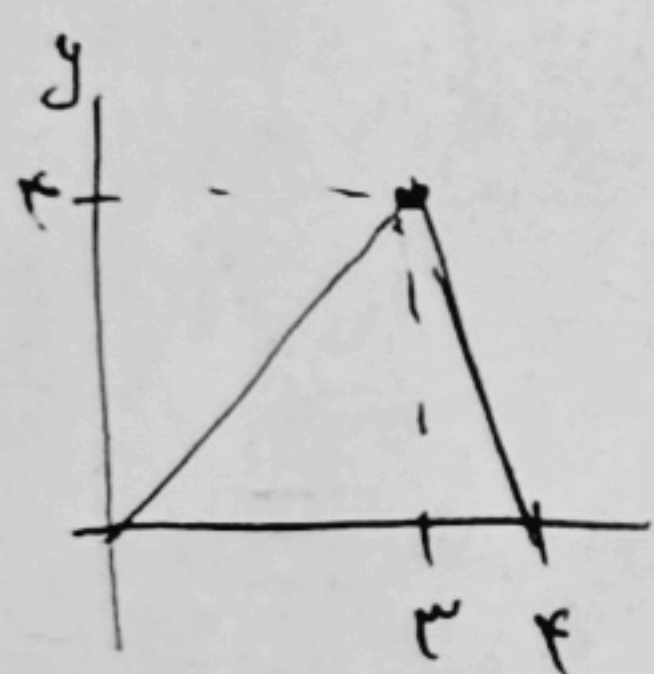
ب) $-1 \leq 2x - 1 \leq -1 \Rightarrow -1 \leq 2x \leq 0 \Rightarrow -\frac{1}{2} \leq x \leq 0 \Rightarrow D' = [-\frac{1}{2}, 0]$

$f(x) = x + \sqrt{x-1} \rightarrow f'(x) = 1 + \frac{1}{2\sqrt{x-1}}$

نقطه بحر در $x=1$ است

$1 + \frac{1}{2\sqrt{x-1}} = 0 \Rightarrow \frac{1}{2\sqrt{x-1}} = -1 \Rightarrow \sqrt{x-1} = -\frac{1}{2} \Rightarrow x-1 = \frac{1}{4} \Rightarrow x = \frac{5}{4}$

$A \mid \wedge \Rightarrow y' = 1$

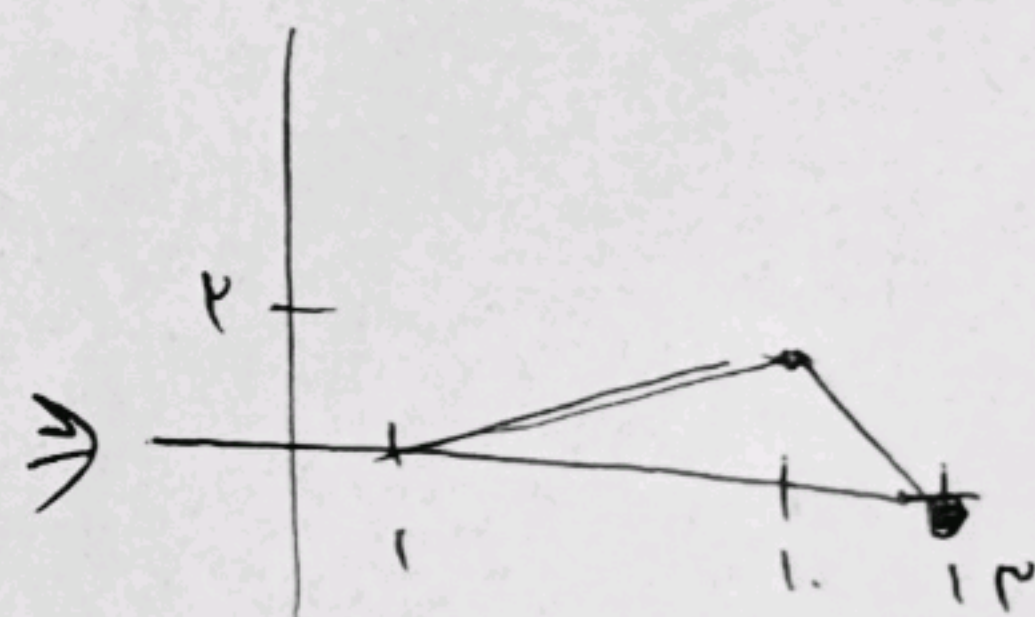


$g(x) = 2f(2x+1)$

$g(2) = 2 \Rightarrow f(1.5) = 1$

$g(1) = 0 \Rightarrow f(1) = 0$

$g(0) = 0 \Rightarrow f(1) = 0$



$\Rightarrow S = \frac{1 \times 1 \times 1}{2} = \frac{1}{2}$

$A \mid \begin{matrix} 2 \\ -2 \end{matrix} y = a + 2f\left(\frac{x-a}{2}\right) \Rightarrow \frac{y-a}{2} = f\left(\frac{x-a}{2}\right) \Rightarrow x-a = 2$

$\Rightarrow x = 2+a$

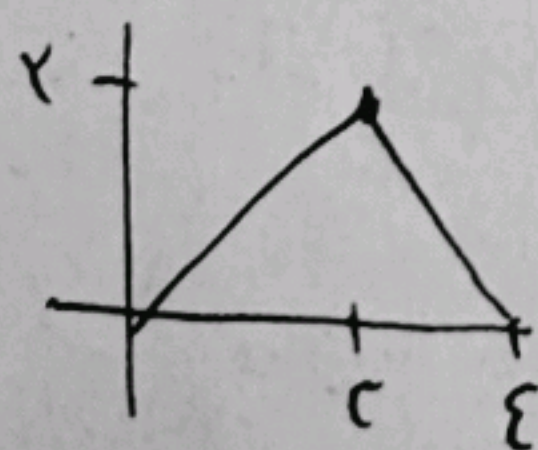
$y = a-2$

$y = 2x-1$

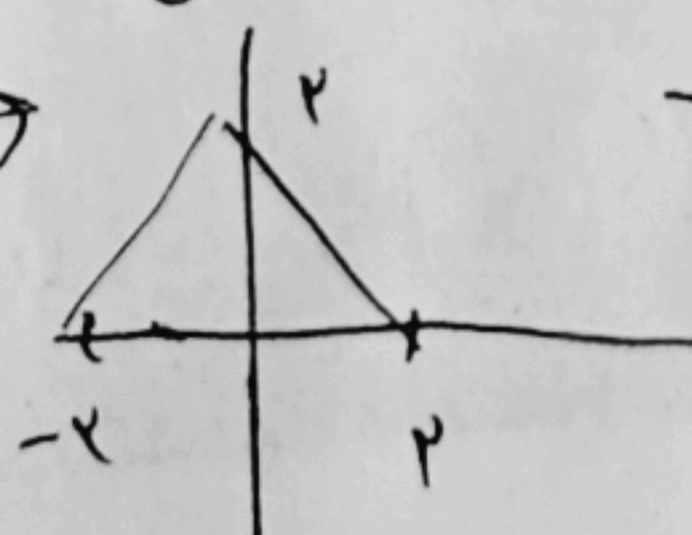
$a-2 = 2(2+a)-1 \Rightarrow a-2 = 4+2a-1 \Rightarrow a-2 = 3+2a \Rightarrow -a = 5 \Rightarrow a = -5$

$\Rightarrow \boxed{a = -5}$

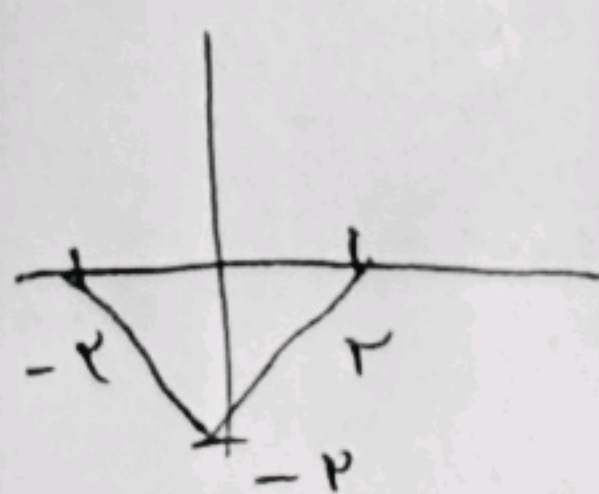
$y = -f(x-1)$



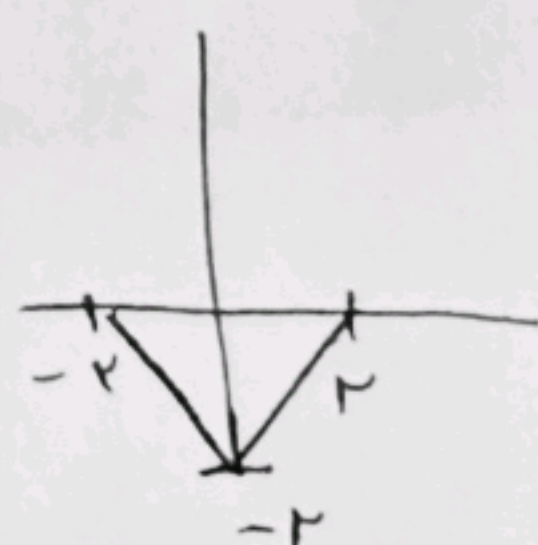
$y = f(x)$



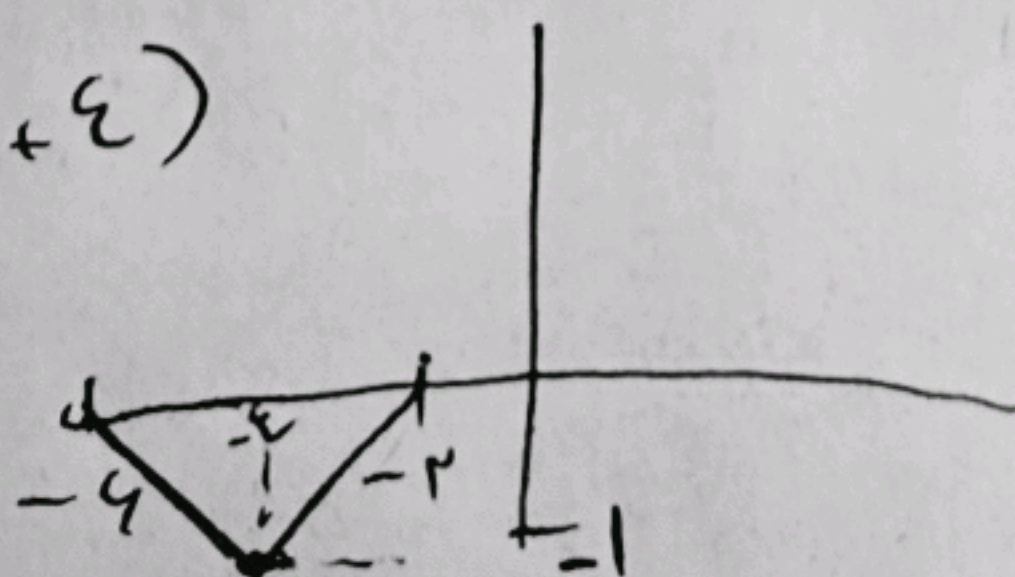
$y = f(x)$



$y = f(-x)$



$y = \frac{1}{2}f(-x+1)$



نقطه بحر در $x=1.5$ است