

4,0

الف) $\cos 2x = 3 \sin x - 1$
 $\Rightarrow 1 + 3 \sin^2 x + 3 \sin x - 1 = 0 \Rightarrow \sin^2 x + \sin x = 0$
 $\Rightarrow \sin x = -\frac{1}{3} \times \sin x = \frac{1}{3} \checkmark$
 $\Rightarrow x = 2k\pi + \frac{\pi}{3}$
 $x = 2k\pi + \pi - \frac{\pi}{3} = 2k\pi + \frac{2\pi}{3}$

$\cos 2x + \cos x - 1 = 0$
 $1 + \cos 2x + \cos x - 1 = 0 \Rightarrow \cos 2x + \cos x - 1 = 0$
 $\Rightarrow \cos 2x = 1 - \cos x = \frac{1}{3} \times 2 = \frac{2}{3} \checkmark$
 $\Rightarrow x = 2k\pi$

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الف) $\cos^2 x - \sin^2 x = -\sin^2 x$
 $\Rightarrow \cos^2 x = -\sin^2 x \Rightarrow \cos^2 x = -1 \sin^2 x \cdot \cos^2 x$
 $\Rightarrow \cos^2 x = 0 \Rightarrow x = k\pi + \frac{\pi}{2} \Rightarrow x = \frac{k\pi}{2} + \frac{\pi}{2}$
 $\sin^2 x = -1 \Rightarrow x = k\pi - \frac{\pi}{2} \Rightarrow x = k\pi - \frac{\pi}{2}$
 $\Rightarrow x = k\pi + \frac{\pi}{2} \Rightarrow x = k\pi + \frac{\pi}{2}$

$1) \cos^2 x + \sin^2 x \cdot \cos x = 1$
 $\Rightarrow \cos^2 x - 1 + \sin^2 x \cdot \cos x = 0 \Rightarrow \cos^2 x + \sin^2 x = 0$
 $\Rightarrow \cos^2 x = -\sin^2 x$
 $\Rightarrow x = k\pi + \frac{\pi}{2} \Rightarrow x = \frac{k\pi}{2} + \frac{\pi}{2}$

$\cos^2 x + \sin^2 x = 0$

$1 + \tan^2 x = 0 \Rightarrow x = \frac{k\pi}{2} - \frac{\pi}{2}$

1,0

الف) $\cos^2 x (1 + \cos x) = \frac{1}{\sin x}$
 $\Rightarrow \frac{\cos^2 x}{\sin x} (1 + \cos x) = \frac{1}{\sin x}$
 $\Rightarrow \cos^2 x + \cos^3 x - 1 = 0$
 $\cos x = -1 \Rightarrow x = k\pi + \pi$
 $\cos x = \frac{1}{2} \Rightarrow x = 2k\pi + \frac{\pi}{3}$

$\cos x + \sin x = 0$

$1 + \tan x = 0$

$x = k\pi - \frac{\pi}{4}$

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الف) $\cos(\frac{\pi}{2} + x) = \sin(\frac{\pi}{2} - x - \frac{\pi}{2})$
 $\Rightarrow -\sin(x - \frac{\pi}{2}) \cdot \cos(x - \frac{\pi}{2}) = \frac{1}{2}$
 $\Rightarrow -\frac{1}{2} \sin(x - \frac{\pi}{2}) = \frac{1}{2}$
 $\Rightarrow \sin(x - \frac{\pi}{2}) = -1 \Rightarrow x - \frac{\pi}{2} = k\pi - \frac{\pi}{2} \Rightarrow x = k\pi$
 $\Rightarrow x = k\pi + \frac{\pi}{2} \Rightarrow x = k\pi + \frac{\pi}{2}$

$\cos(x - \frac{\pi}{2}) = \sin(\frac{\pi}{2} - x + \frac{\pi}{2})$
 $\Rightarrow \sin(-x + \frac{\pi}{2}) = \sin(-x)$
 $\Rightarrow -x + \frac{\pi}{2} = k\pi - x \Rightarrow x = k\pi$

$\Rightarrow x = k\pi + \frac{\pi}{2} \Rightarrow x = k\pi + \frac{\pi}{2}$

$-x + \frac{\pi}{2} = k\pi + x \Rightarrow x = \frac{k\pi}{2} + \frac{\pi}{4}$

$\Rightarrow x = \frac{k\pi}{2} + \frac{\pi}{4}$

$x - \frac{\pi}{4} = k\pi - x - \frac{\pi}{4} \Rightarrow x = \frac{k\pi}{2} + \frac{\pi}{4}$

1,0

$\frac{\sin^2 x + \sin^2 x}{\sin^2 x} - \sin^2 x = \cos^2 x \Rightarrow \frac{\sin^2 x}{\sin^2 x} + 1 = 1 \Rightarrow \frac{\sin^2 x}{\sin^2 x} = 0$
 $\Rightarrow \sin^2 x = 0 \Rightarrow x = k\pi \Rightarrow x = \frac{k\pi}{2}$

$\sin^2 x + 1 = 1 \Rightarrow \sin^2 x = 0$

$\Rightarrow \sin^2 x = 0 \Rightarrow x = \frac{k\pi}{2} + \frac{\pi}{2}$

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k	0	1	2	3	4	5	6	7	8
x	0	$\frac{\pi}{2}$	$\frac{\pi}{2}$	$\frac{3\pi}{2}$	π	$\frac{5\pi}{2}$	$\frac{3\pi}{2}$	$\frac{7\pi}{2}$	2π

$$k=0 \rightarrow x=\pi \quad k=-1 \rightarrow x=-\pi \quad |-1-\pi| = k\pi$$

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$$\sin x = 0 \rightarrow x = 0, \pi, k\pi$$

$$\cos x = -1 \rightarrow x = \frac{\pi}{2}, \pi, \frac{3\pi}{2}$$

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$$\tan\left(\frac{\pi}{2} - x\right) = \frac{1 - \tan x}{1 + \tan x} = \tan \pi x$$

$$\Rightarrow \frac{\pi}{2} - x = \pi k + k\pi \Rightarrow \frac{\pi}{2} = x + k\pi \Rightarrow x = \frac{\pi}{2} - k\pi$$

$$\tan\left(\frac{\pi}{2} - x\right) = \tan \pi x \rightarrow \frac{\pi}{2} - x = k\pi + \pi x \rightarrow x = \frac{k\pi}{2} + \frac{\pi}{4}$$

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$$\sin x = -1 \rightarrow x = k\pi - \frac{\pi}{2} \rightarrow \frac{k\pi}{2}$$

$$x = k\pi + \frac{\pi}{2} \rightarrow \frac{\pi}{2}$$

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$$\text{a)} \quad \sin^2 x - \cos^2 x = 0$$

$$0 \rightarrow 0 - 1 = -1 \quad \times$$

$$\frac{\pi}{2} \rightarrow 1 - 0 = 1 \quad \checkmark$$

$$\pi \rightarrow 0 - 1 = -1 \quad \times$$

$$\frac{3\pi}{2} \rightarrow 1 - 0 = 1 \quad \checkmark$$

$$2\pi \rightarrow 0 - 1 = -1 \quad \times$$

$$\text{b)} \quad \sin^3 x - \cos^3 x = -1$$

$$0 \rightarrow 0 - (+1) = -1 \quad \checkmark$$

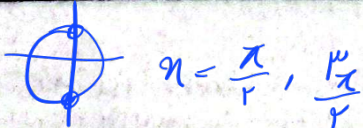
$$\frac{\pi}{2} \rightarrow 1 - 0 = +1 \quad \times$$

$$\pi \rightarrow 0 - (-1) = +1 \quad \times$$

$$\frac{3\pi}{2} \rightarrow -1 + 0 = -1 \quad \checkmark$$

$$2\pi \rightarrow 0 - (+1) = -1 \quad \checkmark$$

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$$x = \frac{\pi}{2}, \frac{3\pi}{2}$$



$$x = 0, 2\pi$$