

۱- $2 \left[\frac{x}{x} \right] + a \left[\frac{0}{x} \right] = 2$
 $2 \left[\frac{x}{x} \right] + a \left[\frac{0}{x} \right] = 2 \Rightarrow 2 - a \cdot 2 = 2 \Rightarrow a = 2$
 $\Rightarrow \left[\frac{x}{x} \right] = 0$

۲- $\sin \frac{\pi}{4} = \frac{1}{2} \Rightarrow \left[2 \times \frac{1}{2} - 1 \right] = \left[1 - 1 \right] = \left[0 \right] = -1$
 $\Rightarrow \lim_{n \rightarrow (\frac{\pi}{4})^-} [2 \sin n - 1] = -1$

۳- $-\frac{1}{x} = -\frac{1}{x} \Rightarrow \left[1 \times -\frac{1}{x} + \frac{1}{x} \right] = \left[-\frac{1}{x} \right] = -1$

۴- $x < -\frac{1}{x} \Rightarrow x^2 > \frac{1}{x} \Rightarrow \frac{1}{x^2} < x \Rightarrow \frac{x}{x^2} < 1 \Rightarrow \left[\frac{x}{x^2} \right] = 1$
 $\frac{1}{x^2} < x \Rightarrow \frac{x}{x^2} < 1 \Rightarrow -\frac{x}{x^2} > -1 \Rightarrow \left[-\frac{x}{x^2} \right] = -1$
 $x < -\frac{1}{x} \Rightarrow 14x < -1$
 $\Rightarrow \frac{-14 + 14}{-1 + 1} = \frac{0}{0} = \infty$

۵- $\frac{\sin^2 \pi x}{1 + \cos \pi x} = \frac{1 - \cos^2 \pi x}{1 + \cos \pi x} = \frac{(1 - \cos \pi x)(1 + \cos \pi x)}{1 + \cos \pi x} = 1 - \cos \pi x$
 $\lim_{x \rightarrow 1^+} 1 - \cos \pi x = 2$

۶- $\lim_{n \rightarrow -1} \frac{\sqrt{2n+3} - \sqrt{2n+4}}{1 + \sqrt{n}} = \frac{0}{0}$ Hop
 $\lim_{n \rightarrow -1} \frac{\frac{2}{2\sqrt{2n+3}} - \frac{2}{2\sqrt{2n+4}}}{\frac{1}{2\sqrt{n}}} = \frac{\frac{2}{2} - \frac{2}{2}}{\frac{1}{2}} = \frac{-\frac{1}{2}}{\frac{1}{2}} = -\frac{1}{2}$

۷- $\lim_{x \rightarrow 1} \frac{0}{0} = \frac{0}{0}$ Hop $\lim_{x \rightarrow 1} \frac{2 - \frac{1}{\sqrt{x}}}{2 - \frac{1}{\sqrt{x}}} = \frac{2 - \frac{1}{\sqrt{1}}}{2 - \frac{1}{\sqrt{1}}} = \frac{2 - 1}{2 - 1} = 1$

$$\lim_{n \rightarrow 0} \frac{0}{0} \stackrel{\text{H\ddot{o}p}}{=} \lim_{n \rightarrow 0} \frac{b}{\sqrt{bn+c}} = \frac{b}{\sqrt{c}} = \frac{1}{\sqrt{c}} \Rightarrow \sqrt{c} = \sqrt{c} \quad -1$$

$$(c > 0, b > 0 \Rightarrow) \sqrt{bn+c} = c \quad I$$

$$a + \sqrt{bn+c} = 0 \Rightarrow a = -\sqrt{bn+c} \Rightarrow a = -\sqrt{cn} \Rightarrow a = -\sqrt{c} \Rightarrow a = -\sqrt{c}$$

$$\Rightarrow \frac{ab}{c} = \frac{-\sqrt{c} \cdot \sqrt{c}}{\sqrt{c} \cdot \sqrt{c}} = -\frac{1}{\sqrt{c}} \quad \checkmark \quad (4)$$

$$n > -2\pi \Rightarrow \frac{n}{\pi} > -2 \Rightarrow \left[\frac{n}{\pi} \right] \geq -2 \Rightarrow \frac{c-2k}{0^+} = +\infty \quad -9$$

$$n < -2\pi \Rightarrow \frac{n}{\pi} < -2 \Rightarrow \left[\frac{n}{\pi} \right] = -3 \Rightarrow \frac{c-3k}{0^-} = +\infty \quad (5)$$

$$\Rightarrow c-2k > 0 \Rightarrow c > 2k, \quad c-3k < 0 \Rightarrow \frac{c}{3} < k$$

$$\Rightarrow \frac{c}{3} < k < \frac{c}{2} \Rightarrow -\frac{c}{2} > -k > -\frac{c}{3} \Rightarrow [-k] = -\frac{c}{3} \quad \checkmark$$

$$\lim_{n \rightarrow 1} \frac{0}{0} \stackrel{\text{H\ddot{o}p}}{=} \lim_{n \rightarrow 1} \frac{b \times \frac{1}{\sqrt{2n+1}}}{\sqrt{2n+1}} = \frac{b}{2} \quad I$$

$$1a - b = 0 \Rightarrow 1a = b = a = \frac{b}{1} \quad II$$

$$I \cap II : \lim_{n \rightarrow 1} \frac{b \times \frac{1}{\sqrt{2n+1}}}{\frac{bn}{1}} = \frac{1}{\sqrt{2} \times \sqrt{2+1}} = \frac{1}{4} \quad \checkmark \quad (6)$$