

1

$$\begin{cases} x \geq 0 \\ a - 2x \geq 0 \end{cases} \xrightarrow{\text{دامنه}} [0, \frac{a}{2}]$$

$$A \mid \begin{matrix} 0 \\ a \end{matrix} \quad B \mid \begin{matrix} a \\ 0 \end{matrix}$$

$$f'(x) = \frac{1}{\sqrt{x}} + \frac{-2}{\sqrt{a-2x}} = 0 \rightarrow \frac{1}{\sqrt{x}} = \frac{2}{\sqrt{a-2x}}$$

$$\rightarrow \sqrt{a-2x} = 2\sqrt{x} \rightarrow a - 2x = 4x \rightarrow a = 6x \rightarrow x = \frac{a}{6} \Rightarrow C \mid \frac{a}{6}$$

$$\rightarrow y_{max} \times y_{min} = \sqrt{12} \Rightarrow \sqrt{\frac{12a}{6}} \times \sqrt{\frac{a}{6}} = \sqrt{12} \rightarrow a = 6 \Rightarrow [a] = 6$$

2

3

$$y = ax^3 + bx^2 + cx + d \xrightarrow{(0,0)} d = 0$$

$$\xrightarrow{(1,1)} a + b = 1$$

$$y' = 3ax^2 + 2bx + c \xrightarrow{(0,0)} c = 0$$

$$\xrightarrow{(1,1)} 3a + 2b + 0 = 0 \rightarrow 3a + 2b = 0$$

$$\ominus \begin{cases} 3a + 2b = 0 \\ a + b = 1 \end{cases} \Rightarrow \begin{cases} 2a = -2 \Rightarrow a = -1 \\ b = 2 \end{cases}$$

$$ab = -2$$

4

تابع در دامنه داده شده بگنجد است پس نقاط سرج و ته را به
 مابرسی می‌کنیم

$$A \mid \begin{matrix} -1 \\ a \end{matrix} \quad B \mid \begin{matrix} \sqrt{3} \\ 0 \end{matrix}$$

$$y = -x^3 + 3x \rightarrow y' = -3x^2 + 3 = 0 \rightarrow \begin{cases} C \mid \frac{1}{\sqrt{3}} \\ D \mid -\frac{1}{\sqrt{3}} \end{cases} \Rightarrow y_{min} = -2$$

در دامنه داده شده داخل قدر مطلق است \oplus

5

$$\begin{cases} x^3 + 3ax^2 + b & x \geq 0 \end{cases}$$

$$\begin{cases} -x^3 + 3ax^2 + b & x < 0 \end{cases} \rightarrow y' = -3x^2 + 6ax = 0 \xrightarrow{(-1,0)} -3 - 6a = 0 \rightarrow a = \frac{-3}{6}$$

$$-x^3 + 3ax^2 + b \xrightarrow{(-1,0)} -x^3 - \frac{3}{2}x^2 + b \rightarrow 1 - \frac{3}{2} + b = 0 \rightarrow b = \frac{1}{2} \Rightarrow \frac{b}{a} = \frac{\frac{1}{2}}{\frac{-3}{6}} = \boxed{-2}$$

6

$$y = \frac{3}{2}x^2 + x + \frac{1}{2} \rightarrow y' = 3x + 1 = 0 \rightarrow x = -\frac{1}{3} \xrightarrow{f, \rightarrow} y_{\min} = \frac{1}{3}$$

$$y = \frac{ax+3}{(a+1)x+(a-1)} \quad \text{مجانِب افقی} = \frac{a}{a+1} \quad \text{مجانِب قائم} = \frac{-d}{c} = \frac{-a+1}{a+1}$$

7

$$\frac{a}{a+1} = \frac{1}{3} \rightarrow a = 2 \rightarrow y = \frac{2x+3}{3x+1} \rightarrow \frac{2x+3}{3x+1} = 0 \rightarrow 2x+3=0 \rightarrow x = -\frac{3}{2}$$

$$\text{مجانِب افقی} = \frac{b}{c} \quad \text{مجانِب قائم} = -(ax+1)$$

$$A(-\frac{1}{3}, 3) \rightarrow \frac{b}{c} = 3 \rightarrow b = 12$$

$$\frac{-ax-1}{c} = -\frac{1}{3} \rightarrow ax+1 = 2$$

$$\rightarrow ax=1 \rightarrow a = -2$$

8

$$\frac{b}{a} = \frac{12}{-2} = \boxed{-6}$$

$\frac{x^6}{x^3-1}$ منبسط طول بازه اکیدا نزولی آن (0,2) است

9

10