

$$\lim_{x \rightarrow 0} \frac{f(x)}{g(x)} = \frac{0}{0} \Rightarrow \lim_{x \rightarrow 0} \frac{f'(x)}{g'(x)} = \lim_{x \rightarrow 0} \frac{-x \cos(x) + \sin(x) + \cos(x)}{1} = 1$$

$$\lim_{x \rightarrow 0} \frac{f'(x)}{g'(x)} = \frac{-x + \cos(x) + \sin(x)}{1} = 1 \Rightarrow a = 1$$

$$\cos(x) + \sin(x) + b = 1 \Rightarrow (1 + b = 0 \Rightarrow b = -1) \quad a + b = 0$$

1

$$f(x) = x^2 - 1 \Rightarrow f'(x) = 2x \quad \frac{x_0 - x}{a} = \frac{1}{a} \Rightarrow 2x = a \Rightarrow x = \frac{a}{2}$$

$$f(x_0) = f\left(\frac{1}{2}\right) = -\frac{3}{4} \quad f'(x_0) = f'\left(\frac{1}{2}\right) = 1$$

2

$$y = mx + b \Rightarrow m = \frac{\Delta y}{\Delta x} = \frac{1}{\frac{1}{4}} = 4 \quad y = 4x + b \Rightarrow b = -9 \quad y = 4x - 9$$

$$m = f'(x) \Rightarrow m = \frac{a}{(x-1)^2} \Rightarrow 4 = \frac{a}{(x-1)^2} \Rightarrow a = 4(x-1)^2$$

$$a = 4 \Rightarrow f(x) = \frac{4}{9} = \frac{1}{\frac{9}{4}}$$

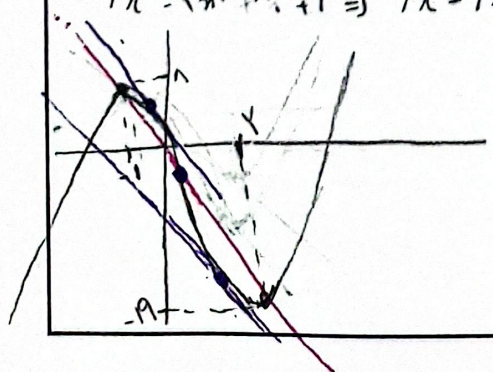
3

$$f(x) = \frac{a+1}{a+1} = 1 \quad y = x + b \Rightarrow x + b = 1 \Rightarrow b = 0 \quad f'(x) = \frac{(1-a^2)}{(a^2 x + 1)^2} = 2$$

$$\frac{1-a^2}{(a^2 x + 1)^2} = 2 \Rightarrow 1 - a^2 = 2(a^2 x + 1)^2 \Rightarrow 1 - a^2 = 2a^4 + 4a^2 x + 2$$

$$\Rightarrow a = -\frac{1}{\sqrt{2}} \quad b = 1 \Rightarrow a - b = -\frac{1}{\sqrt{2}} + 1$$

$$4x^2 - 4x - 1 = 0 \Rightarrow x^2 - x - \frac{1}{4} = 0 \quad (x-2)(x+1)$$



$$y = -9x + 1$$

$$4x^2 - 4x - 1 = -9x + 1$$

$$4x^2 - 9x + 3 = 0 \quad \Delta > 0 \Rightarrow \text{دو جواب}$$

دو نقطه قطع می‌شوند و در آنجا مماس می‌شود

4