

$$n+2 = t \Rightarrow n = t-2 \Rightarrow f(t) = \begin{cases} 3t-2+5 & t \geq 3 \\ 4t-1-1 & t < 3 \end{cases}$$

$$\Rightarrow f(3-n) = \begin{cases} 9-3n-1 & n \geq 3 \\ 12-4n-9 & n < 3 \end{cases} \Rightarrow \begin{cases} \sqrt{1-3n-3n-2} & n \geq 3 \\ -2n+6 & n < 3 \end{cases}$$

$$9 f(n+1) = \begin{cases} 3n+3-1 & n \geq 3 \\ 4n+4-9 & n < 3 \end{cases} \Rightarrow \begin{cases} \sqrt{3-4n-4n+5} & n \geq 3 \\ 1-1n & n < 3 \end{cases}$$

غیر قابل

$$1-1n \geq 0 \Rightarrow 1 \geq n \Rightarrow D_f = (-\infty, 1]$$

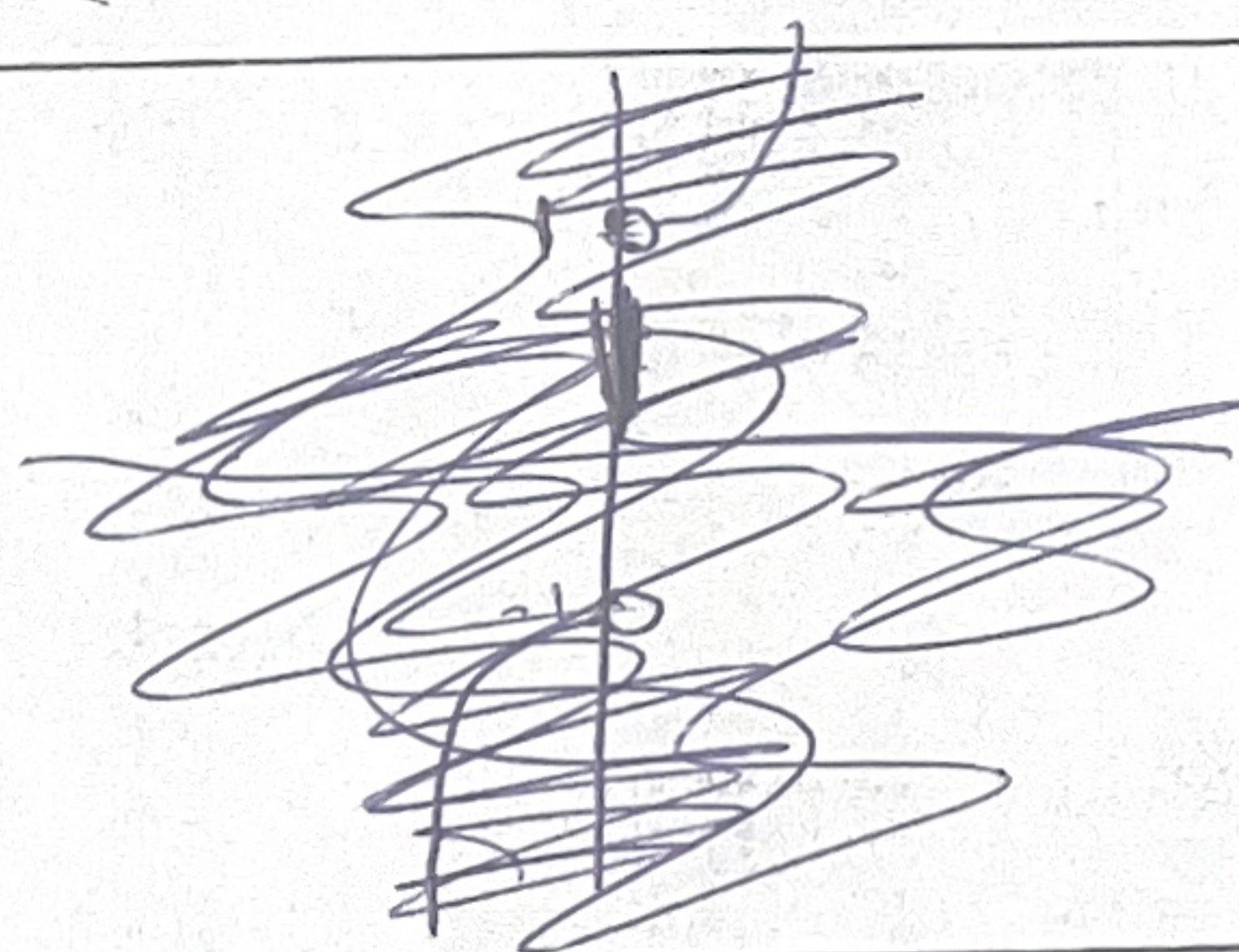
تابع $f(x)$ یک تابع صعودی است. پس:

$$f(x) < x^3 \Rightarrow (x^3+x)^2 < x^3 \Rightarrow x^3+x < x$$

$$\Rightarrow x^3 < 0 \Rightarrow x < 0$$

$$x \times \frac{x^3+1}{x} = x^2+1 : x > 0$$

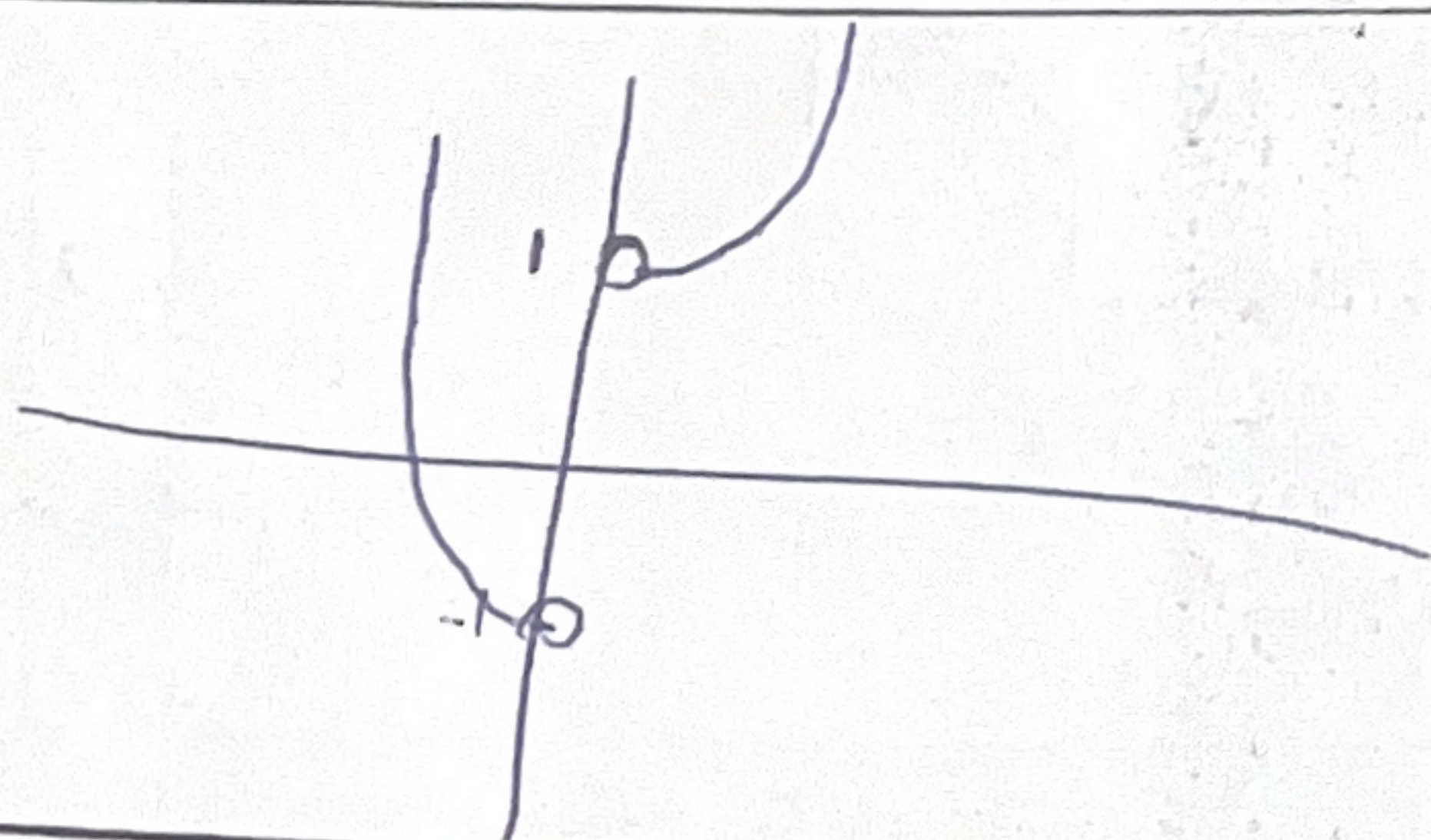
$$-x \times \frac{x^3+1}{x} = -x^2-1 : x < 0$$



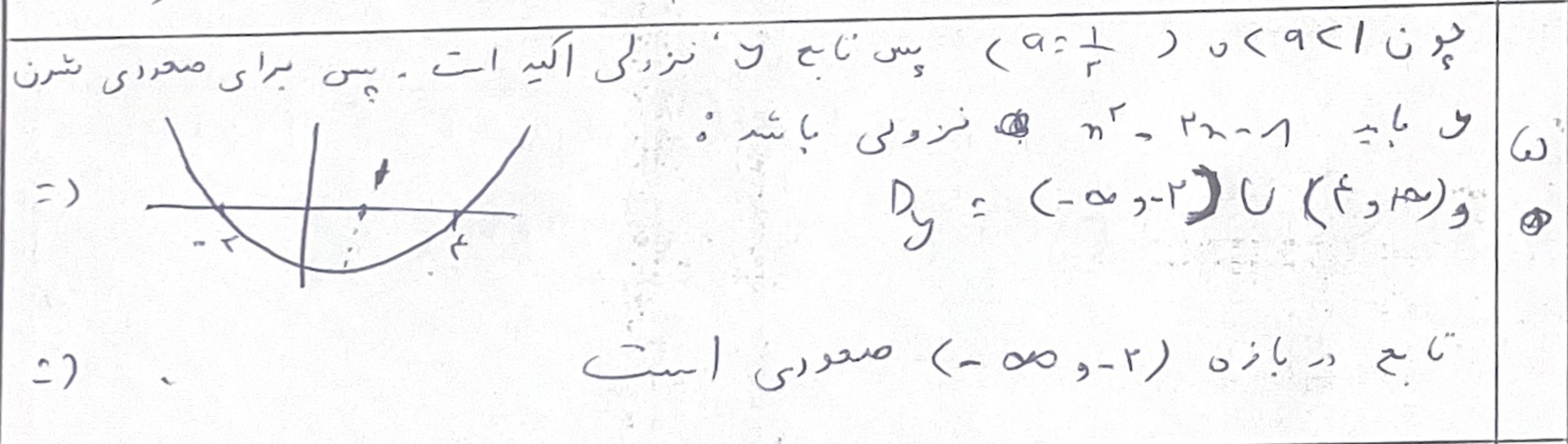
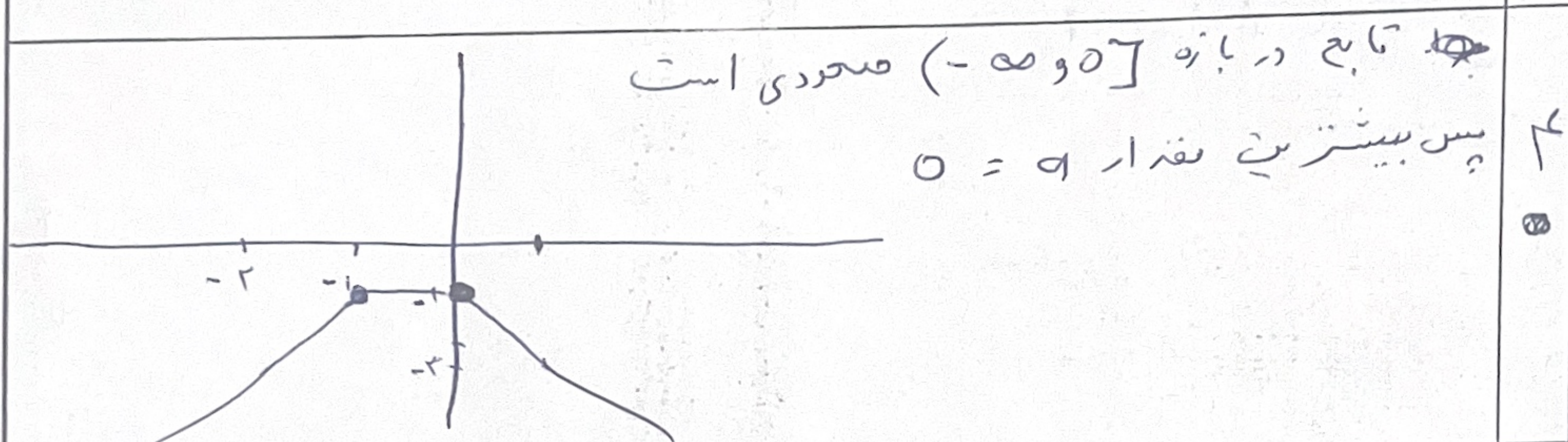
تابع نایکوندا است.

در بازه $(0, +\infty)$ صعودی است.

در بازه $(-\infty, 0)$ نزولی است.



$\frac{2n+1}{-n+n+1} = 2n+1$	$\frac{2n+1}{-n-n-1} = \frac{2n+1}{-2n-1}$ $= -1$	$\frac{2n+1}{n-n-1} = \frac{2n+1}{-1} = -2n-1$	✓
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$a^2 - 2 \geq 1$ $a^2 \geq 3$ $a \geq \sqrt{3}$ $a \leq -\sqrt{3}$	$a^2 - 2 > 1$ $a^2 > 3$ $a > \sqrt{3}$ $a < -\sqrt{3}$	اند	✓
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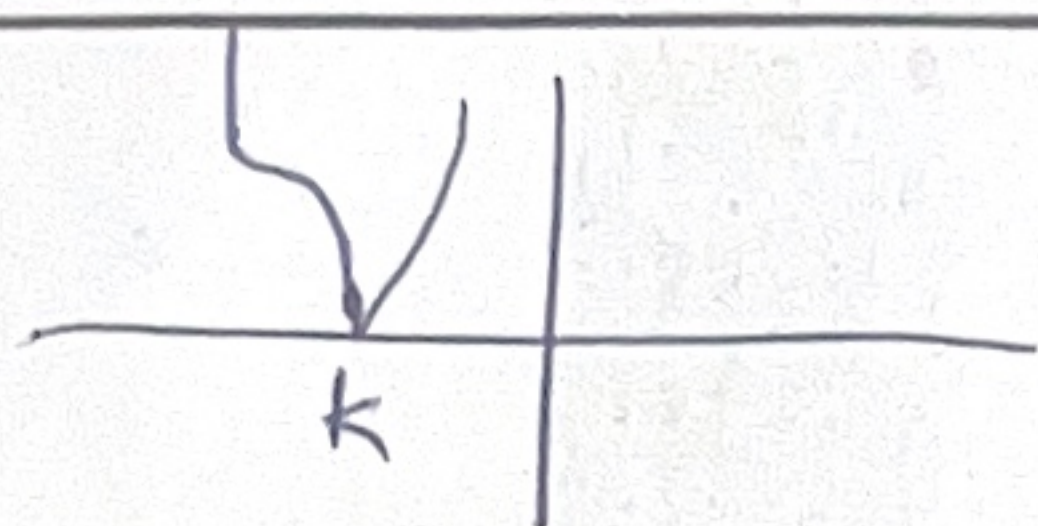
تابع:

$$(n+3)^3 - 1 = n^3 + 9n^2 + 27n + 27 - 1$$

$$= n^3 + 9n^2 + 27n + 26$$

$\Rightarrow a = 9, b = 27, c = 26$

$$|f(n)| :$$



$$\Rightarrow (n+r)^2 - 1 = 0 \Rightarrow (n+r)^2 = 1 \Rightarrow n+r = 1$$

$$\Rightarrow n = -r \Rightarrow k = -r$$

✓

$$f(n) \leq \sqrt{n} \Rightarrow n + \sqrt{n} - r \leq \sqrt{n}$$

$$\Rightarrow n - r \leq 0 \Rightarrow n \leq r$$

$$\Rightarrow \boxed{0 \leq n \leq r} \Rightarrow \text{محدوده صحیح}$$

$$D_{f(n)} = [0, r]$$

$$D_{f \circ f} = [\phi, +\infty)$$

✓

$$f(n) \geq 0 \Rightarrow n + \sqrt{n} - r \geq 0$$

$$\Rightarrow n + \sqrt{n} \geq r \Rightarrow n \geq 1$$

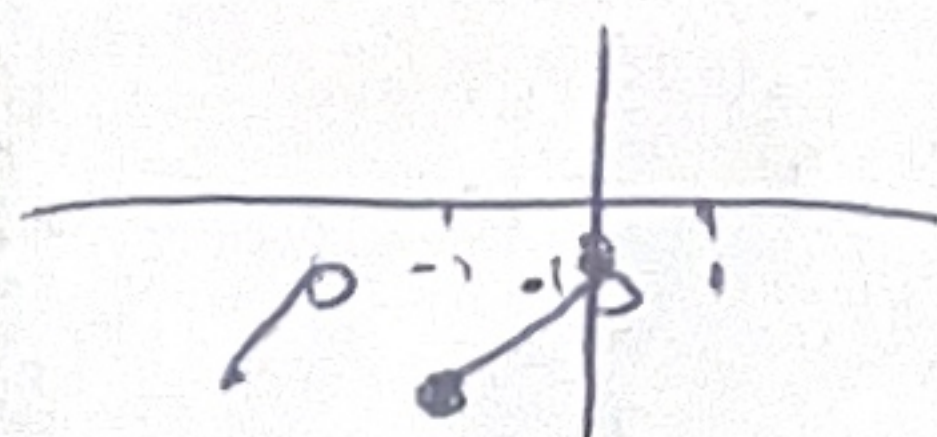
✓

$$\left. \begin{aligned} \cos n - 1 \geq 0 &\Rightarrow \cos n \geq \frac{1}{r} \Rightarrow \cos n \geq \frac{1}{r} \\ \cos n - 1 \leq 0 &\Rightarrow \cos n \leq 1 \Rightarrow \cos n \leq -\frac{1}{r} \end{aligned} \right\} \nexists$$

$$\text{I} \cap \text{II}: \cos n = \pm \frac{1}{r} \Rightarrow R_f = 0 \Rightarrow b-a = 0$$

9

$$f(n): n - [n] - r \Rightarrow$$



$$\Rightarrow R_f = [-r, -1)$$

$$g(-r) = \frac{\frac{1}{r} - r}{r} = \frac{1 - r^2}{r^2} = \frac{-10}{1}$$

$$g(-1) = \frac{\frac{1}{r} - r}{r} = \frac{1 - r^2}{r^2} = \frac{-r}{r} \Rightarrow R_{g \circ f} = \left[-\frac{10}{1}, -\frac{r}{r}\right)$$

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$\left(-\frac{r}{r}\right)$