



$$\frac{\frac{\sqrt{2}}{2} \times 1}{2} = \frac{\sqrt{2}}{4} \quad S_{ABC} = \frac{\pi}{4}$$

$$\frac{F}{2} = \frac{1}{2} \quad \therefore x^2 = \frac{F}{9} - \frac{16F}{9} = -\frac{15F}{9}$$

$$x^2 - \sin \alpha = -\frac{1}{9} \cos^2 \alpha \quad \leadsto \quad \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \rightarrow \frac{\sin \alpha \pm \sqrt{\sin^2 \alpha + \cos^2 \alpha}}{2} \rightarrow \frac{\sin \alpha \pm 1}{2}$$

$$\frac{\sin \alpha + 1}{2} = \frac{1}{3} \quad \leadsto \quad 3 \sin \alpha + 3 = 2 \rightarrow \sin \alpha = -\frac{1}{3} \rightarrow \cos \alpha = \pm \frac{\sqrt{8}}{3}$$

$$\left(\frac{\sin \alpha}{\cos \alpha} \right)^2 = \tan^2 \alpha \rightarrow \left(\frac{-\frac{1}{3}}{\pm \frac{\sqrt{8}}{3}} \right)^2 = \frac{1}{8}$$

$$1 + \frac{1}{\lambda} = \boxed{\frac{9}{\lambda}}$$

$$\log(\sin \alpha) - \log(\cos \alpha) = \log 3 \quad \leadsto \quad \log\left(\frac{\sin \alpha}{\cos \alpha}\right) = \log 3 \quad \leadsto \quad -\tan \alpha = 3 \rightarrow \tan \alpha = -3$$

$$\frac{\sin \alpha}{\cos \alpha} = -3 \rightarrow -3 \cos \alpha = \sin \alpha \quad \leadsto \quad \sin^2 \alpha + \cos^2 \alpha = 1 \rightarrow 9 \cos^2 \alpha + \cos^2 \alpha = 1 \rightarrow 10 \cos^2 \alpha = 1 \rightarrow \cos \alpha = \pm \frac{1}{\sqrt{10}}$$

$$\sin \alpha = \pm \frac{3}{\sqrt{10}} \quad \sin \alpha - \cos \alpha = \frac{3}{\sqrt{10}} + \frac{1}{\sqrt{10}} = \frac{4}{\sqrt{10}} = \frac{2\sqrt{10}}{5}$$

$$\cos \alpha = -\frac{1}{\sqrt{10}}$$

$$\sin^2 \alpha + \cos^2 \alpha = \frac{F}{\omega} \quad \leadsto \quad \sin^2 \alpha + 1 - \sin^2 \alpha = \frac{F}{\omega} \quad \leadsto \quad \sin^2 \alpha (\sin^2 \alpha - 1) = -\frac{1}{\omega} \quad \leadsto \quad \sin^2 \alpha x - \cos^2 \alpha = -\frac{1}{\omega} \rightarrow -(\sin^2 \alpha \cos^2 \alpha) = -\frac{1}{\omega}$$

$$\cos^2 \alpha + \sin^2 \alpha \rightarrow \cos^2 \alpha + 1 - \cos^2 \alpha = \leadsto \cos^2 \alpha (\cos^2 \alpha - 1) + 1 \rightarrow \cos^2 \alpha - \sin^2 \alpha + 1$$

$$\rightarrow \frac{-(\sin^2 \alpha \cos^2 \alpha) + 1}{-\frac{1}{\omega}} \rightarrow 1 - \frac{1}{\omega} = \boxed{\frac{F}{\omega}}$$

$$\sin \alpha \tanh x = \frac{1}{\cos \alpha} > 0 \rightarrow \frac{\sin \alpha - 1}{\cos \alpha} > 0 \rightarrow \boxed{\cos \alpha < 0}$$

$$\frac{3 \sin x + \sin x \cos x}{2(1 - \cos^2 x)} < 0 \rightarrow \frac{\sin x(3 + \cos x)}{2 \sin^2 x} < 0 \quad \leadsto \quad \frac{3 + \cos x}{2 \sin x} < 0 \rightarrow \boxed{\sin x < 0}$$

رابع کوم تلتای $\rightarrow$ ناصیه کوم

$$\frac{r \cos x + r \sin x}{\sin x \cos x} = 0 \rightarrow r \cos x = -r \sin x \rightarrow \cos x = -\frac{r}{r} \sin x$$

$$\rightarrow \sin^2 x + \cos^2 x = 1 \rightarrow \sin^2 x + \frac{r}{r} \sin^2 x = 1 \rightarrow \frac{1+r}{r} \sin^2 x = 1 \rightarrow \sin x = \pm \sqrt{\frac{r}{1+r}}$$

$$\rightarrow \sin x > 0 \rightarrow \cos x = -\frac{r}{r} \sqrt{\frac{r}{1+r}}$$

$$\tan x = \frac{\sqrt{\frac{r}{1+r}}}{-\frac{r}{r} \sqrt{\frac{r}{1+r}}} = -\frac{1}{r}$$

$$\tan x + \cot x \rightarrow -\frac{1}{r} - \frac{r}{r} \rightarrow -\frac{1}{r} - \frac{r}{r} = -\frac{1+r}{r}$$

$$\cot x = \frac{-\frac{1}{r}}{-\frac{1+r}{r}} = \frac{1}{1+r}$$

$$1 - r \sin^2 \theta \rightarrow \sin^2 \theta + \cos^2 \theta - r \sin^2 \theta = \cos^2 \theta - \sin^2 \theta = \cos 2\theta$$

$$\frac{1 - \tan^2 \theta}{1 + \tan^2 \theta} = \frac{\cos^2 \theta - \sin^2 \theta}{\cos^2 \theta + \sin^2 \theta} = \frac{\cos^2 \theta - \sin^2 \theta}{1} = \cos 2\theta$$

$$(1 - \tan^2 \theta) (\cos^2 \theta - \sin^2 \theta) = (\cos^2 \theta - \sin^2 \theta) (\cos^2 \theta + \sin^2 \theta) \rightarrow \cos^2 \theta - \sin^2 \theta = \cos^2 \theta + \sin^2 \theta$$

$$\sin \alpha + r \cos \alpha = r \rightarrow \sin \alpha = r - r \cos \alpha \rightarrow \sin^2 \alpha = r^2 + r^2 \cos^2 \alpha - 2r^2 \cos \alpha$$

$$\sin^2 \alpha + \cos^2 \alpha = 1 \rightarrow r^2 + r^2 \cos^2 \alpha - 2r^2 \cos \alpha + \cos^2 \alpha = 1 \rightarrow 1 + r^2 \cos^2 \alpha - 2r^2 \cos \alpha + r^2 = 1$$

$$r^2 \cos^2 \alpha - 2r^2 \cos \alpha + r^2 = 0 \rightarrow r^2 (\cos^2 \alpha - 2 \cos \alpha + 1) = 0 \rightarrow r^2 (\cos \alpha - 1)^2 = 0$$

$$\cos \alpha - 1 = 0 \rightarrow \cos \alpha = 1 \rightarrow \alpha = 0^\circ$$

$$\sin B \sin C = \cos^2 \frac{A}{2} \rightarrow \cos^2 \frac{A}{2} = \frac{1 + \cos A}{2} \rightarrow \cos A = 2 \cos^2 \frac{A}{2} - 1$$

$$\cos A = -(\cos B \cos C - \sin B \sin C) \rightarrow \cos A = \sin B \sin C - \cos B \cos C$$

$$\sin B \sin C = \frac{1 + \sin B \sin C - \cos B \cos C}{2} \rightarrow 0 = 1 + \sin B \sin C - \cos B \cos C - 2 \sin B \sin C$$

$$1 - (\sin B \sin C + \cos B \cos C) = 0 \rightarrow \sin B \sin C + \cos B \cos C = 1 \rightarrow \cos(B - C) = 1$$

$$\cos(0^\circ) = 1 \rightarrow B = C = 45^\circ \rightarrow \boxed{A = 90^\circ}$$