

$$\cos(r_x) = r \sin x - 1 = 1 - r \sin^2 x \rightarrow r \sin^2 x + r \sin x - r = 0 \quad (1)$$

$$(4\sin x - 1)(\sin x + 1) = 0 \rightarrow \sin x = \frac{1}{4} \rightarrow x = 2k\pi + \frac{\pi}{2}, 2k\pi + \frac{9\pi}{2}$$

$$\sin x = -1$$

$$\cos(yx) + \cos x - y = 0 \Rightarrow \cancel{y \cos x} + \cos x - y = 0 = (\cos x - 1)(yx + y) = 0$$

$$\cos x = 1 \Rightarrow x = 2k\pi$$

$$\cos x = -\frac{1}{2} \cdot \times$$

$$\sin^k x - \cos^k x = (\sin^2 x + \cos^2 x)(\sin^2 x - \cos^2 x) = -\cos^2 x = \sin^2 x \quad (2) \text{ الف}$$

$$\Rightarrow Y \sin Yx \cos Yx = -\cos Yx \Rightarrow (Y \sin Yx) (\cos Yx) = - \rightarrow \sin Yx = -\frac{1}{Y}$$

$$\rightarrow yx = y | k\pi + \frac{v\pi}{9}, yk\pi + \frac{11\pi}{9} \rightarrow x = k\pi + \frac{v\pi}{19}, k\pi + \frac{11\pi}{19} \quad \cos yx = 0 \rightarrow yx = k\pi + \frac{\pi}{2}$$

$$Y \cos x + Y \sin x \cos x = 1 \Rightarrow \cos Yx = -\sin(Yx) = \frac{0}{1} \quad (c)$$

$\rightarrow \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{x}} \right) = \frac{\partial L}{\partial x}$

$$\tan(yx) = -1 \rightarrow yx = k\pi + \frac{\pi}{2} \rightarrow x = \frac{k\pi}{y} + \frac{\pi}{\lambda}$$

$$\cos(x)(Y \cos x + 1) = \frac{1}{\sin x} \Rightarrow \cos x(Y \cos x + 1) = 1 \quad (3) \text{ ان } \sin x \neq 0$$

$$Y \cos^2 x + \cos x - 1 = 0 \Rightarrow (Y \cos x - 1)(\cos x + 1) = 0$$

$\begin{cases} \cos x = -1 \rightarrow \sin x = 0 \\ \cos x = \frac{1}{Y} \rightarrow x = \arccos \frac{1}{Y} \end{cases}$

$$Y \sin^2 x - \sin x \cos x + \cos^2 x = Y \rightarrow \frac{1}{Y} \cos^2 x - \frac{1}{Y} \sin^2 x + \frac{1 + \cos^2 x}{Y} = Y$$

$$\rightarrow \frac{1}{Y} (\sin(Yx) + \cos(Yx)) = -\frac{1}{Y} \rightarrow \sqrt{Y} \sin(Yx + \frac{\pi}{4}) = -1 \rightarrow \sin(Yx + \frac{\pi}{4}) = -\frac{\sqrt{Y}}{Y}$$

$$\rightarrow Y_{x+\frac{\pi}{r}} = Y_{k\pi + \frac{\pi}{r}}, Y_{k\pi + \frac{\pi}{r}} \rightarrow x = k\pi + \frac{\pi}{r}, k\pi + \frac{\pi}{r}$$

$$\text{الف) } \cos\left(x + \frac{\pi}{4}\right) \cos\left(x - \frac{\pi}{4}\right) = \left(\frac{\sqrt{2}}{2}(\cos x - \sin x)\right) \left(\frac{\sqrt{2}}{2}(\cos x + \sin x)\right) \quad (1)$$

$$= \frac{1}{2} (\cos^2 x - \sin^2 x) = \frac{1}{2} \rightarrow \cos 2x = \frac{1}{2} \rightarrow 2x = 2k\pi \pm \frac{\pi}{3} \rightarrow x = k\pi \pm \frac{\pi}{6}$$

$$\text{ب) } \cos\left(2x - \frac{\pi}{4}\right) = -\sin 2x = \cos\left(2x + \frac{\pi}{4}\right) \Rightarrow \cos\left(-2x - \frac{\pi}{4}\right)$$

$$\Rightarrow 2x - \frac{\pi}{4} = 2k\pi + 2x + \frac{\pi}{4} \rightarrow 2x = 2k\pi + \frac{\pi}{2} \rightarrow x = k\pi + \frac{\pi}{4}$$

$$\frac{\sin(2x) + \sin(2x)}{\sin(2x)} = \cos^2 x + \sin^2 x = 1 \rightarrow \sin(2x) = 0$$

$$\sin(2x) = 0 \rightarrow 2x = k\pi \pm \frac{\pi}{2} \rightarrow x = k\pi \pm \frac{\pi}{4}$$

$$\frac{\sin\left(\frac{x}{2}\right)}{1 + \cos\left(\frac{x}{2}\right)} = \frac{1 + \cos\frac{x}{2}}{\sin\frac{x}{2}} \Rightarrow \tan\left(\frac{x}{4}\right) = \frac{1}{\tan\left(\frac{x}{4}\right)} \quad (2)$$

$$\tan\left(\frac{x}{4}\right) = \pm 1 \rightarrow \frac{x}{4} = k\pi \pm \frac{\pi}{4} \rightarrow x = 4k\pi \pm \pi \rightarrow x \in \left[-\pi, \frac{\pi}{4}\right] \rightarrow x = -\pi$$

$$\cos^2 x - \sin^2 x \cos^2 x = 1 \Rightarrow -\sin^2 x (\cos^2 x) = 0 \quad (3)$$

$$\sin^2 x = 0 \Rightarrow x = k\pi \quad \cos^2 x = 0 \Rightarrow x = \frac{\pi}{2} + k\pi$$

$$x = 0, \frac{\pi}{2}, \pi, \frac{3\pi}{2}, 2\pi$$

$$\sqrt{1 + \sin 2x} = \sqrt{2} \cos(x) \geq 0$$

$$\rightarrow 1 + \sin 2x = 2 \cos^2(x) = 2 - 2 \sin^2(x) \rightarrow \sin^2(x) = 0 \rightarrow x = k\pi$$

$$\rightarrow \sin 2x = -1 \rightarrow \cos(x) = 0 \rightarrow x = \frac{\pi}{2} + k\pi$$

$$\rightarrow \sin(2x) = \frac{1}{2} \rightarrow \cos 2x = \pm \frac{\sqrt{3}}{2} \rightarrow \cos(2x) = \frac{\sqrt{3}}{2} \rightarrow 2x = 2k\pi \pm \frac{\pi}{6} \rightarrow x = k\pi \pm \frac{\pi}{12}$$

$$\Rightarrow x = \frac{\pi}{12}, \frac{5\pi}{12}, \frac{7\pi}{12}, \frac{11\pi}{12}$$

$$\sin^r x - \cos^r x = -(\sin^r x + \cos^r x)(\cos^r x - \sin^r x) = -\cos^r x = 1 \quad (ج/١)$$

$$\cos^r x = -1 \rightarrow rx = rk\pi + \frac{\pi}{2}, \text{ where } r \rightarrow x = k\pi + \frac{\pi}{r} \rightarrow x = \frac{\pi}{r}, \frac{r\pi}{r}$$

$$\sin^r x - \cos^r x = -1 \rightarrow \cos^r x - \sin^r x = 1 \quad (ب)$$

$$\rightarrow (\cos x - \sin x)^r + r \sin x \cos x (\cos x - \sin x) = 1$$

$$-\sqrt{r} \leq \epsilon = \cos x - \sin x \rightarrow \epsilon^r = 1 + r \sin x \cos x \rightarrow \sin x \cos x = \frac{1 - \epsilon^r}{r}$$

$$\epsilon^r + r \left(\frac{1 - \epsilon^r}{r} \right) \epsilon = 1 \rightarrow \epsilon^r - \epsilon^r + r = 0 = (\epsilon - 1)^r (\epsilon + r) \quad \begin{cases} \rightarrow \epsilon = 1 \\ \rightarrow \epsilon = -r \end{cases}$$

$$\begin{aligned} \epsilon = 1 & \rightarrow \left. \begin{aligned} \sin x \cos x &= \frac{1 - \epsilon^r}{r} = 0 \\ \cos x - \sin x &= 1 \end{aligned} \right\} \rightarrow \begin{aligned} \sin x &= 0, \cos x = 1 \\ \cos x &= 0, \sin x = -1 \end{aligned} \quad \begin{cases} x = rk\pi \\ x = rk\pi + \frac{r\pi}{r} \end{cases} \\ x &= 0, \frac{r\pi}{r}, r\pi \end{aligned}$$

$$\frac{1 - \epsilon \tan x}{1 + \epsilon \tan x} = \epsilon \tan^r x \rightarrow r = (1 + \epsilon \tan x)(1 + \epsilon \tan^r x) \quad (أ)$$

$$1 - \epsilon \tan^r x \epsilon \tan x = \epsilon \tan(x) + \epsilon \tan(r x) \rightarrow \frac{\epsilon \tan x + \epsilon \tan^r x}{1 - \epsilon \tan x \epsilon \tan^r x} = \epsilon \tan(r x) = 1$$

$$rx = k\pi + \frac{\pi}{r} \rightarrow x = \frac{k\pi}{r} + \frac{\pi}{r}$$