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$$f(x) = (1+m)x^2 + (-p+n)x + m+n+2 \rightarrow m = -10, n = 4$$

$$\rightarrow f(x) = -2x$$

$$p+1 = -10 \rightarrow p = -11$$

$$p+1 < -1 \rightarrow -11+1 < -1 \rightarrow -10 < -1$$

$$\rightarrow k = 10$$

$$m+n+p+k = -10+4-11+10 = -7$$

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الف) $\sqrt{\frac{x-2}{x^2-2x-8}}$ $\xrightarrow{x=t}$ $\frac{t^2-2t-8}{t^2-2t-8} = \frac{t^2-2t-8}{t^2-2t-8} = 1$ $\xrightarrow{t=4}$ $x=2$ $\rightarrow D_f = (-\infty, -2) \cup (2, \infty)$

ب) $\frac{2x^2+1}{x^2-2x}$ $\rightarrow f-2[-x] \neq 0 \rightarrow 2[-x] = f \rightarrow x \in (-\infty, -2)$

$\rightarrow D_f = \mathbb{R} - (-\infty, -2]$ واضح نبودن

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الف) $\sqrt{x(x-1)}$ $\xrightarrow{\text{بین صفت صحت}}$ $\frac{x}{x+1} \rightarrow x \geq 0 = 2x \rightarrow x \leq 0 = 0$ $\rightarrow D_f = [1, \infty) \cup [1, \infty)$

ب) $\sqrt{|x+1|-x^2}$ $\rightarrow |x-2| \geq 0 \rightarrow D_f = [-2, 1] - \{0\}$

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$|x-2|-1 \neq k$ $\rightarrow$ تابع در کمترین و بیشترین و خطی و در هر دو سمت و نقطه قطع کند

$\rightarrow y = k \rightarrow k = 1$

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مرتب بنویس!

$y = 2x$ $\rightarrow$ بین صفر تا یک

$x > 1 \rightarrow y = 2x - 1$

$x = 2 \rightarrow y = 2$

$-1 \leq x < 0 \rightarrow y = 2x + 1$

$-2 \leq x < -1 \rightarrow y = 2x + 3$

$$f(x) = g(x) \rightarrow f(0) = g(0) \rightarrow \left. \begin{aligned} f(0) &= 2 \\ g(0) &= c \end{aligned} \right\} \rightarrow \boxed{c=2}$$

$$\left. \begin{aligned} f(1) &= g(1) \rightarrow \frac{a+2}{b+1} = 2 \\ f(-1) &= g(-1) \rightarrow \frac{-a+2}{-1+b} = 1 \end{aligned} \right\} \rightarrow \begin{aligned} a+2 &= 2b+2 \\ -a+2 &= -1+b \end{aligned} \rightarrow \begin{aligned} a &= 2b \\ -2b+2 &= -1+b \end{aligned} \rightarrow \begin{aligned} 0 &= 3b-3 \\ b &= 1 \end{aligned} \rightarrow \boxed{b=1}$$

جواب سوال
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$$\frac{x^2 - 2x + 3}{x+2} = x - b \rightarrow \frac{x^2 - 2x + 3}{x+2} = x - b$$

$$\rightarrow x^2 - 2x + 3 = x^2 + (a-b)x - ab \rightarrow \begin{aligned} a-b &= -2 \\ ab &= 3 \end{aligned} \rightarrow \boxed{a-b = -2}$$

$$\rightarrow \left. \begin{aligned} a &= 3 \\ b &= 1 \end{aligned} \right\} \rightarrow \boxed{a+b = -2, 2}$$

خوابه سوال نیست

جواب
سوال
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$$\sqrt{b-2} + 2k \rightarrow \boxed{b=2}$$

$$\sqrt{2-2a} + k - 1 \rightarrow \boxed{a = \frac{2}{r}}$$

$$2a - \frac{b}{r} - k = 2 - 2 + 1 = \boxed{1}$$

$$2f(1) - g(1) = k \rightarrow 2k - 2 - 2k = k \rightarrow \boxed{k = -1}$$

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$$D_{f \circ g} = D_f \cap D_g \rightarrow D_g = [-1, +\infty)$$

$$\max D_f = \{v\} \rightarrow \sqrt{m-v} = 0 \rightarrow \boxed{m=v}$$

$$f(r) - g(r) = 5\sqrt{r}$$

$$m+n = 5 + 8\sqrt{r}$$

$$\rightarrow r+n - 2\sqrt{r} = 5\sqrt{r} \rightarrow r+n = 7\sqrt{r} \rightarrow \boxed{n = -r + 7\sqrt{r}}$$

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$$y = x - [x] = \frac{1}{2}$$

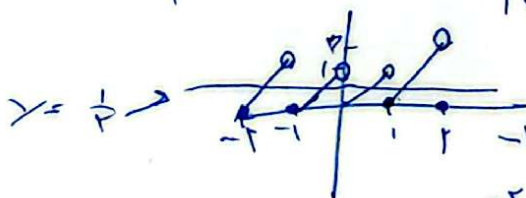
$$0.5x < 1 \rightarrow y = 0$$

$$1.5x < 2 \rightarrow y = x - 1$$

$$x = 2 \rightarrow y = 0$$

$$-1.5x < 0 \rightarrow y = x + 1$$

$$-2.5x < -1 \rightarrow y = x + 2$$



جواب دارد

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