

$$\frac{0}{0} \rightarrow \text{hop} = \lim_{u \rightarrow 1} \frac{u+1}{\frac{1}{\frac{1}{u} + 1}} = \frac{u+1}{\frac{u}{u+1}} = \frac{(u+1)^2}{u} = \frac{1}{-1} = -1$$

$$\cos \alpha \sim 1 - \frac{\alpha^2}{2} \rightarrow 1 - \cos \alpha = \frac{\alpha^2}{2} \rightarrow \lim_{u \rightarrow 0} \frac{\sqrt{1+u} - \sqrt{1-u}}{u}$$

$$\lim_{u \rightarrow 0} \frac{\sqrt{1+u} - \sqrt{1-u}}{u} \times \frac{1}{1} \times \frac{1}{1} = \frac{1}{2} \times \frac{1}{1} = \frac{1}{2}$$

$$\cos \alpha \sim 1 - \frac{\alpha^2}{2} \rightarrow \lim_{u \rightarrow 0} \frac{k+1 - \frac{au^2}{2}}{ku^2} = \frac{k+1 - \frac{au^2}{2}}{ku^2} = \frac{k+1}{0} \times$$

$$\rightarrow \frac{0}{0} \text{ (1) } k+1=0 \rightarrow k=-1, \text{ (2) } \frac{-au^2}{ku^2} = \frac{-a}{k} = -1 \rightarrow a=k \rightarrow \frac{a}{k} = -1$$

$$\lim_{u \rightarrow 0} \frac{u\sqrt{u-a} + u(\sqrt{u-a} - \sqrt{a})}{\sqrt{u-a} \sqrt{a}} = \frac{u\sqrt{u-a} + u(\frac{u-a}{\sqrt{u-a} + \sqrt{a}})}{\sqrt{u-a} \sqrt{a}}$$

$$\rightarrow \frac{u + \frac{u^2}{\sqrt{u-a} + \sqrt{a}}}{\sqrt{u-a} \sqrt{a}} = \frac{u}{\sqrt{a}} = \sqrt{\frac{u}{a}} = \sqrt{\frac{1}{a}}$$

$$\lim_{u \rightarrow 1} \frac{1+k}{0} = -\infty$$

$$1+k > 0 \rightarrow k > -1 \rightarrow \pi k \in (-1, 9 - \frac{1}{\pi})$$

$$1+k < 0 \rightarrow k < -1$$

$$\rightarrow \cos \pi k \in (-1, 0) \quad \left(\cos \pi k, \sin \pi k \right) \sim \cos \pi k$$