

$$\lim_{x \rightarrow r} \frac{rx - a}{x^2 + ax + b} \rightarrow \frac{ra - a}{r^2 + ar + b}$$

صورت و مخرج نامعادله است
در صورت نامعادله

$$x^2 + ax + b = (x-r)^2 = x^2 + (a-r)x + r^2$$

$$\left. \begin{array}{l} a = r \\ b = r^2 \end{array} \right\}$$

$$\underline{a+b=r}$$

$$\lim_{x \rightarrow r} \frac{x}{x^2 + ax + b} \rightarrow \frac{r}{r^2 + ar + b}$$

صورت نامعادله است پس باید مخرج نامعادله شود

$$x^2 + ax + b = (x-\sqrt{r})^2 = x^2 + 2\sqrt{r}x + r$$

$$\left. \begin{array}{l} b = r \\ a = 2\sqrt{r} \end{array} \right\}$$

$$\left[\frac{\sqrt{r}}{2\sqrt{r}} \right] = \left[-\frac{\sqrt{r}}{r} \right] = 0$$

$$\lim_{x \rightarrow \left(\frac{1}{r}\right)^+} \frac{[-x]}{\left| \frac{\sqrt{r}}{r}x + a \right| + a} \rightarrow \frac{a-1}{\left| \frac{\sqrt{r}}{r}x + a \right| + a} \rightarrow \frac{a-1}{\left| \frac{1}{r} + a \right| + a}$$

$$a + \frac{1}{r} > 0 \rightarrow a + \frac{1}{r} + a = \frac{a-1}{2a + \frac{1}{r}} \rightarrow -\infty \rightarrow \text{---} \rightarrow a = -\frac{1}{r} \rightarrow \left[-\frac{1}{r}\right] \cdot (-1)$$

$$a + \frac{1}{r} < 0 \rightarrow \frac{a-1}{-\frac{1}{r}} \rightarrow a = +\infty \rightarrow \text{---}$$

$$\lim_{x \rightarrow \left(-\frac{1}{r}\right)^+} \frac{rx - \left[\frac{r}{x^2}\right]}{rx + \left[\frac{r}{x^2}\right]} = \frac{rx + 9}{rx + 12} \rightarrow \frac{1}{0^+} = +\infty$$

صورت نامعادله

$$\lim_{x \rightarrow r^+} \frac{x^r - r}{x^r - [x^r]} \rightarrow \frac{x^r - r}{x^r - r} \rightarrow \frac{(x-r)(x+r)}{(x-r)(x^r + r + rx)} = \frac{x+r}{x^r + rx + r} = \frac{r}{r^2} = \frac{1}{r}$$

$$\lim_{x \rightarrow -1} \frac{x^r + 1}{x + 1} = \frac{(x+1)(x+1)}{x(x+1)} \cdot \frac{(x+\sqrt{x^r} - 1\sqrt{x})}{(x+\sqrt{x^r} - 1\sqrt{x})}$$

$$\lim_{x \rightarrow -1} \frac{(x+1)(x+\sqrt{x^r} - 1\sqrt{x})}{x} = \frac{-1 \times 1}{-1} = 1$$

$$\lim_{x \rightarrow 0} \frac{\sqrt{r+x} - \sqrt{r-x}}{\sqrt{1-\cos x}} = \frac{(\sqrt{r+x} - \sqrt{r-x})(\sqrt{r+x} + \sqrt{r-x})}{\sqrt{1-\cos x}(\sqrt{r+x} + \sqrt{r-x})}$$

$$\lim_{x \rightarrow 0} \frac{r+x - r+x}{x\sqrt{\frac{1}{r}}(\sqrt{r+x} + \sqrt{r-x})} = \frac{0}{0} \rightarrow \frac{1-x^r}{x\sqrt{\frac{1}{r}}} = \frac{r}{\sqrt{r} \times \sqrt{r}} = \frac{r}{r} = 1$$

$$\lim_{x \rightarrow 0} \frac{k + \cos(\sqrt{x})}{kx^r} = r \rightarrow \frac{k+1 - \frac{0x^r}{r}}{kx^r} = r$$

$$\rightarrow r k x^r = k+1 - \frac{0x^r}{r} \rightarrow \frac{k+1}{r} = r \rightarrow Q_1 = -4$$

$$\frac{Q_1}{k} = \frac{-4}{-1} = 4$$

$$\lim_{x \rightarrow -1} \frac{1-kx}{x^r-1} = -\infty \rightarrow \frac{1+k}{x^r-1} = -\infty \rightarrow \frac{1+k}{0^-} = -\infty$$

$$\rightarrow 1+k > 0 \rightarrow \boxed{k > -1}$$

$$k\pi \rightarrow \text{mod } \pi$$

$$x \rightarrow -1^- \rightarrow \frac{1+k}{x^r-1} = -\infty \rightarrow 1+k < 0$$

$$\boxed{-1 < k < -\frac{1}{r}}$$

$$\boxed{k < -\frac{1}{r}}$$

$$\cos(k\pi)$$