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$x=1 \rightarrow f(1) + f(1) = 3 + f(1) \quad f(x) = ax+b \xrightarrow{\text{جای ندری}} \begin{matrix} a=1 \\ b=0 \end{matrix} \quad f(x) = x$
 $f(1) = 3$

$f(1x+1) + f(x+1) = 3x + 3$

$g(x) = \sqrt{x - x^2} \rightarrow D_g = [0, 1]$
 $R_g = [0, \frac{1}{2}]$

$\frac{x^3 - 4x}{x+2} = \frac{(x+2)(x^2 - 2x)}{x+2} = x^2 - 2x \xrightarrow{x=-2} f - (2)(-2) = 1$
 $x^2 - 2x - 1 = 0 \rightarrow x = -2 < a$

$D: \mathbb{R} - \{ -2 \}$
 $D: \mathbb{R} - \{ a, b \} \rightarrow a, b \rightarrow \mathbb{R} - \{ -2, -1 \}$
 $\frac{-b}{2a} = \frac{-1}{2} = -\frac{1}{2} \rightarrow c$

$f\left(\frac{-1}{-2}\right) = f\left(\frac{1}{2}\right) = 0$
 $f(-1) = 3$

$\sqrt[3]{(x-2)^3} = \sqrt[3]{x^3 - 4x^2 + 12x - 8} = x - 2$

$a = -4 \quad b = 12$

$f(x) = x - 2$
 $f(-4) = -6$
 $f(12) = 10$

$R: [-6, 10]$

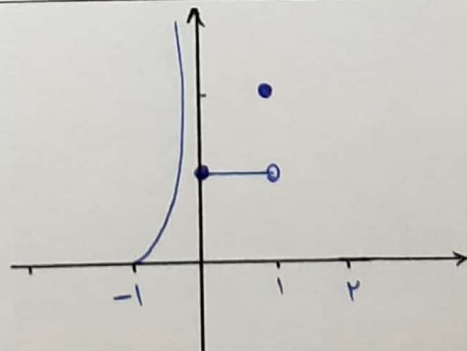
$\frac{x+1}{1-x} \geq 0$
 $\left\{ \begin{matrix} -1 & 1 \\ - & + \\ + & - \end{matrix} \right\} \quad [-1, 1)$

$\frac{ax^2 - 1}{x^2 + b} = y$

$x^2 \begin{cases} \text{max} \rightarrow \infty \rightarrow a \rightarrow a=1 \\ \text{min} \rightarrow 0 \rightarrow \frac{-1}{b} \rightarrow \frac{-1}{b} = -1 \end{cases}$
 $b = 1$

$a+b = 1+1 = 2$

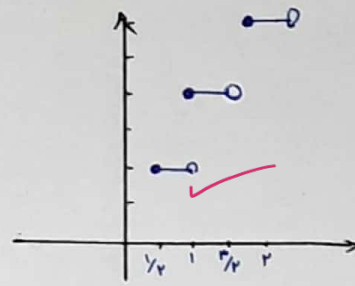
$\frac{[x]}{x} \quad \frac{|x|}{x}$
 $-1 \leq x < 0 \rightarrow \frac{-1}{x} - 1 = \frac{-1-x}{x}$
 $0 \leq x < 1 \rightarrow 0 + 1 = 1$
 $x = 1 \rightarrow 1 + 1 = 2$



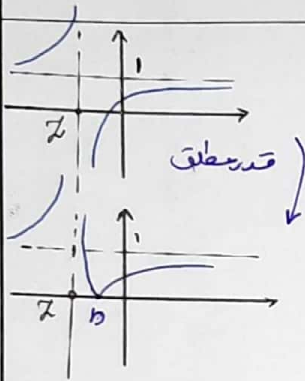
$$\frac{1}{4} < x < 1 \rightarrow 0 + 1 = 1$$

$$1 < x < \frac{3}{4} \rightarrow 1 + 1 = 2$$

$$\frac{3}{4} < x < 2 \rightarrow 1 + 2 = 3$$



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$$y = \left| \frac{1+x}{ax+3} \right| \quad \left| \frac{1+x}{x+3} \right| < 1 \rightarrow x+1 = -x-3$$

$$\frac{1}{a} = 1 \rightarrow a = 1$$

$$x+1 = -x-3 \rightarrow x = -2$$

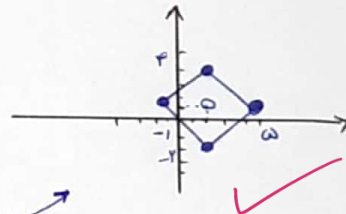
$$b = -1$$

$$a+b = 1+(-1) = 0$$

$$a-b = 2$$

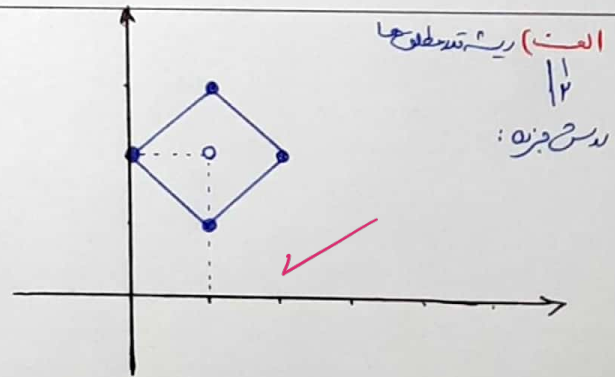
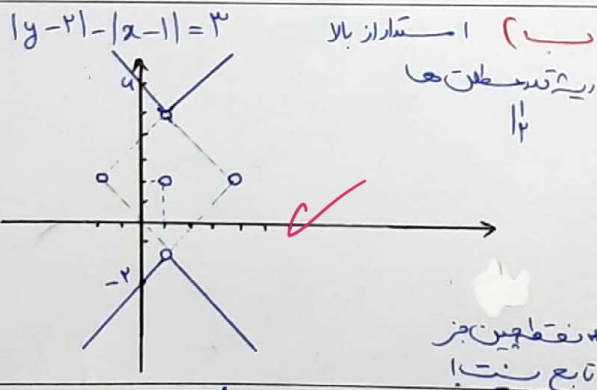
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$$\begin{aligned} x-x+y-1 &= 3 \\ y &= x+4 \\ x-2+y-1 &= 3 \\ y &= -x+4 \end{aligned}$$



نقطه هم درم
ضایحه صریح است

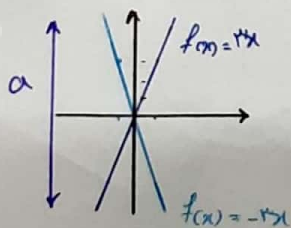
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$$x < 0 \rightarrow f(x) = 3x - ax = (3-a)x \rightarrow 3-a > 0$$

$$x > 0 \rightarrow f(x) = 3x + ax \rightarrow 3+a > 0$$



$$x < 0 \rightarrow 3-a > 0 \rightarrow a < 3$$

$$x > 0 \rightarrow 3+a > 0 \rightarrow a > -3$$

$$-3 < a < 3$$

* b نایزگی نخواهد داشت!

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