

$y = x^{A+B}$, $y = x^A$ → $x=1, y=1$, $y = x^B$ → $x=1, y=1$

$x=1, y=1 \xrightarrow{A+B} 1 = 1^A \Rightarrow A+B=0, A=-B$ / $x=1, y=1 \xrightarrow{A-B} 1 = 1^{A+B} \Rightarrow A+B=0, -B+B=0, -B=0$
 $B=0 \Rightarrow A=1 \rightarrow y = x^{-1} \Rightarrow \text{if } x=0 \rightarrow y = x^{-1} = \frac{1}{x} \rightarrow \text{بجز } x=0$

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$x^2 + y^2 = x^2 + \omega \rightarrow y^2 = \omega \rightarrow (x^2)^2 - 1 = \omega \rightarrow x^4 - 1 = \omega$ $x^2 = t$

$t^2 - 1t + 1 = \omega \Rightarrow \Delta = 1 - 4\omega, x = \frac{1 \pm \sqrt{1-4\omega}}{2}, \omega = \frac{x^2 + 1}{2}$

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$(\log_{11}^3)^2 + \log_{11}^{(11^2)} \times \log_{11}^{(11^2)} / 1 < v < 3 \times v^2, 1 \times v^2 < 3 \times v^2 \times v^2 / \log_{11}^3 = t$

$\log_{11}^{11^2} = \log_{11}^3 + 2 \log_{11}^v \rightarrow \log_{11}^{11} = 1 \Rightarrow \log_{11}^3 + \log_{11}^v = 1, \log_{11}^v = 1 - a$
 $\log_{11}^{11^2} = \log_{11}^3 + 2 \log_{11}^v = 3 - a$ / $\log_{11}^{11^2} = 2 \log_{11}^3 + 2 \log_{11}^v = 2a + 2(1-a) = 2$

$\Rightarrow a^2 + (a+2)(1-a) = 2 \Rightarrow a^2 + 1 - a^2 = 2 \Rightarrow 1 = 2$

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$\log(1-x)^2 + 3 \log(1-x) = \omega \rightarrow \omega \log(1-x) = \omega \Rightarrow \log(1-x) = 1$

$10 = 1-x \Rightarrow x = 9 \Rightarrow \log_{10}^9 = 1$

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$\log_{14}^{x^2+2x+1} + \log_{14}^{x-2} = \log_{14}^1 \rightarrow (x^2+2x+1)(x-2) = 1 \Rightarrow x^2 + 2x^2 + 2x - 2x^2 - 4x - 1 = 1$

$\Rightarrow x^2 - 1 = 1 \Rightarrow x^2 = 14, x = \sqrt{14}$

$\log_{14}^{\sqrt{14}} = \frac{1}{2}$

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$$\log(x-y) - \log\left(\frac{1}{(x-y)^2}\right) = 3 \rightarrow \log(x-y)(x-y)^2 = 3 \quad D_f, x-y > 0 \Rightarrow x < y$$

$$\text{if } x < y \Rightarrow (x-y)^2 = (y-x)^2 \Rightarrow \log(x-y)^2 = 3 \rightarrow (x-y)^2 = 10^3$$

$$\Rightarrow y-x=10, x=1 \quad , \log_{\sqrt{y}}(x) = ? \rightarrow \log_{\sqrt{y}}^{\wedge} = 4$$

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$$x^2 - y = 1 \rightarrow x^2 - y = x^2 \Rightarrow x^2 - y = x^2, x^2 - x^2 - y = 0 \Rightarrow \Delta = 4$$

$$x = \frac{1 \pm \sqrt{4}}{2} \Rightarrow x = 1 + \sqrt{4}, \underbrace{1 - \sqrt{4}}_{\text{قبح}}$$

$$\log_4(x-y) = \log_4^{y+\sqrt{y}-y} \Rightarrow \log_4^{\sqrt{y}} = -1$$

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$$\log_{\frac{y}{x}} = \frac{\Delta}{\Lambda}$$

$$\log_{\frac{\Lambda}{\Delta}} = \frac{\log_{\frac{\Lambda}{\Delta}}^{\wedge}}{\log_{\frac{\Lambda}{\Delta}}^{\Delta}} = \frac{3 \log_{\frac{\Lambda}{\Delta}}^{\Delta}}{\log_{\frac{\Lambda}{\Delta}}^{\Delta} + \log_{\frac{\Lambda}{\Delta}}^{\Delta}} = \frac{3 \times \frac{\Delta}{\Lambda}}{2 + \frac{\Delta}{\Lambda}} = \frac{\frac{3\Delta}{\Lambda}}{\frac{2\Lambda + \Delta}{\Lambda}} = \frac{3\Delta}{2\Lambda + \Delta} = \frac{3\Delta}{\Lambda}$$

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$$\log_{\frac{y}{x}} = 0,18$$

$$\log_{\frac{y}{x}} = \frac{\log_{\frac{y}{x}}^{\Delta}}{\log_{\frac{y}{x}}^{\Delta} + \log_{\frac{y}{x}}^{\Delta}} = \frac{0,18 + 0,18}{0,18 + 1} = \frac{0,36}{1,18} = \frac{18}{118}$$

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$$(a \log y)(-1)^b - a + b \log y = 0 \rightarrow a \log y + b \log y = a \rightarrow (a+b) \log y = a$$

$$\left(\frac{a+b}{a}\right) \log y = \frac{a}{a} \rightarrow \left(1 + \frac{b}{a}\right) \log y = 1, \quad 1 + \frac{b}{a} = \frac{1}{\log y} \Rightarrow \frac{b}{a} = \frac{1}{\log y} - 1 = \log_{\frac{y}{y}}^{\log y} - 1$$

$$\left(\sqrt{y}\right)^{\frac{b}{a}} = y^{\frac{b}{2a}} \rightarrow y^{\frac{1}{2}} \left(\log_{\frac{y}{y}}^{\log y} - 1\right) = y^{\frac{\log y}{2}} \times y^{-\frac{1}{2}} = 10^{-\frac{1}{2}} \times \frac{1}{\sqrt{y}} = \sqrt{10} \times \frac{1}{\sqrt{y}} = \sqrt{10}$$

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