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$$a^{m+n} = a^m \cdot a^n \Rightarrow \log_r a^{m+n} = \log_r a^m + \log_r a^n \Rightarrow (m+n) \log_r a = m \log_r a + n \log_r a \Rightarrow \log_r a = \log_r a$$

$$f(x) = x^{n-1} \Rightarrow f'(x) = \frac{1}{x}$$

به عدد با محدود و با بهر آید

$$\log_r (r^x + 10) = x + r \Rightarrow (r^x)^r - 10(r^x) + 10^r = 0$$

$$t^r - 10t + 10^r = 0 \Rightarrow \begin{cases} t = r \Rightarrow r^r - 10r + 10^r = 0 \\ t = 10 \Rightarrow 10^r - 100 + 10^r = 0 \end{cases}$$

$$(\log_r r_1)^r + \log_r r_1 \Rightarrow (\log_r r_1)^r - (\log_r r_1)^r + r = r$$

$$\log_r r_1 = \log_r r_1 + \log_r r_1 = 1 + \log_r r_1 = 1 + \log_r \frac{r_1}{r} = 1 + \log_r r_1 - \log_r r = 2 - \log_r r$$

$$\log_r r_1 = r + \log_r r_1 \Rightarrow r = 0$$

$$\log (x^{r-m+1}) + r \log (1-x) = 0 \Rightarrow (1-x) \log (1-x) = 0 \Rightarrow \log (1-x) = 0 \Rightarrow 1-x = 1 \Rightarrow x = 0$$

$$\log_r (1-x)^r = r \log_r (1-x) \Rightarrow \log_r (1-x) = \log_r (1-x)$$

$$\log_r (x^r + r^m + r) + \log_r (x-r) = r \Rightarrow \log_r \frac{x^r + r^m + r}{x-r} = r$$

$$\log_r (x-r) = \log_r (x-r)$$

$$\log (r-x) - \log \frac{1}{(r-x)^r} = r \Rightarrow \log (r-x) + r \log (r-x) = r \Rightarrow (r+1) \log (r-x) = r \Rightarrow \log (r-x) = \frac{r}{r+1}$$

$$\log \frac{1}{r-x} = \log \frac{1}{(r-x)^r} = \log \frac{1}{(r-x)^r} = -r \log (r-x) = -r \log (r-x)$$

$$r^m \cdot r^n = r^{m+n} \Rightarrow \log_r r^m + \log_r r^n = \log_r r^{m+n} \Rightarrow m + n = m+n$$

$$\log_r (r-x) = \log_r (r-x)$$

$$\log_r a = r \log_r a^{\frac{1}{r}} = r \log_r a^{\frac{1}{r}} = \log_r a$$

$$\log_r r = \frac{\log_r r}{\log_r r} = \frac{\log_r r + \log_r r}{\log_r r + \log_r r} = \frac{1 + 1}{1 + 1} = \frac{2}{2} = 1$$

$$(a \log_r) x^r + a + b \log_r = 0 \Rightarrow a \log_r + b \log_r = a$$

$$(a+b) \log_r = a \Rightarrow \log_r = \frac{a}{a+b} \Rightarrow \frac{1}{\log_r} = \frac{a+b}{a} \Rightarrow \frac{1}{\log_r} - 1 = \frac{b}{a}$$

$$\log_r = \frac{b}{a} \Rightarrow (r^{\frac{1}{a}})^{\log_r} = r^{\frac{1}{a}} = \frac{1}{r^{\frac{1}{a}}}$$