

$$\lim_{n \rightarrow 1} \frac{(n^2 - 2n + 1)^2}{(n^2 - 1)(n + 1)} = \frac{(n-1)^2(n-1)^2}{(n-1)(n+1)(n+1)} = \frac{(n-1)^3}{(n+1)^2} = \frac{1-1^3}{1+1} = \frac{1}{2}$$

$$\lim_{n \rightarrow \infty} \frac{|2n-1| - |2n+1|}{n} = \frac{1-2n-2n-1}{n} = \frac{-4n}{n} = -4$$

$$\lim_{n \rightarrow f} \frac{n-f}{\sqrt{n}-f} \cdot \frac{n-f}{n-f} \cdot \frac{\sqrt{n}+f}{1} = 1 \times f = f$$

$$\lim_{n \rightarrow 1} \frac{n - \sqrt{2n}}{2n^2 - n - 1} \cdot \frac{n^2 - 2n}{(n-1)(2n+1)} \cdot \frac{1}{n + \sqrt{2n}} = \frac{1-1}{(1-1)(2+1)} \cdot \frac{1}{1+\sqrt{2}} = \frac{1}{1 \cdot 1 \cdot (1+\sqrt{2})} = \frac{1}{1+\sqrt{2}}$$

$$\lim_{n \rightarrow 1} \frac{1 - \sqrt{n}}{1 - \sqrt{5-n}} \cdot \frac{1+\sqrt{n}}{1+\sqrt{n}} \cdot \frac{1-\sqrt{5-n}}{1-\sqrt{5-n}} \cdot \frac{1+\sqrt{5-n}}{1+\sqrt{5-n}} = -1 \times \frac{1}{1} = -1$$

$$\lim_{n \rightarrow f} \frac{\sqrt{2n+f} - f}{\sqrt{5n+5} - 5} \cdot \frac{1}{1} \cdot \frac{1}{1} \cdot \frac{1}{1} = \frac{1}{1} \cdot \frac{1}{1} \cdot \frac{1}{1} \cdot \frac{1}{1} = \frac{1}{1}$$

$$\lim_{n \rightarrow 1} \frac{\sqrt{2n+\sqrt{n}} - 1}{\sqrt[3]{n} - 1} = \frac{(\sqrt{2n+\sqrt{n}} - 1)^2}{(n-1)^2} = \frac{(\sqrt{2n-1})(\sqrt{2n+\sqrt{n}} + 1)^2}{\sqrt{2n-1}(\sqrt{2n+1} + 1)^2} = \frac{1}{1} \cdot \frac{1}{1} = \frac{1}{1}$$

$$\lim_{n \rightarrow \pi} \frac{1 + \cos n}{\sin n} = \frac{(1 + \cos n)(1 + \cos n)}{(1 + \cos n)(1 - \cos n)} = \frac{1 + 1}{1 + 1} = \frac{2}{2} = 1$$

$$\lim_{n \rightarrow \frac{\pi}{3}} \frac{1 - \tan n}{\sin n - \cos n} = \frac{\frac{\cos n - \sin n}{\cos n}}{\frac{\sin n - \cos n}{1}} = \frac{-1}{\cos n} = \frac{-1}{\frac{\sqrt{3}}{2}} = \boxed{\frac{-2}{\sqrt{3}}}$$

9

$$\lim_{n \rightarrow \frac{\pi}{4}} \frac{\tan n - 1}{\cos n} = \frac{\frac{\sin n - \cos n}{\cos n}}{\frac{\cos n - \sin n}{1}} = \frac{-1}{\cos n} = \frac{-1}{\frac{1}{\sqrt{2}}} = \boxed{-\sqrt{2}}$$

10