

$$y = (a-1)x^2 + ax + 1 \quad , \quad a = 2$$

$$\frac{-b}{2a} = \frac{-1}{2(a-1)} \quad , \quad y \rightarrow f(a) = f(-1) \rightarrow f(a) = 1 \rightarrow a = \frac{1}{f} \rightarrow -\frac{1}{f}x^2 + ax + 1 = 0$$

$$ax^2 - x - 1 = 0 \rightarrow (a-1)(a+1) = 0 \rightarrow a = -1, 1 \rightarrow a = 1$$

1

$$f(x) = mx^2 - 2x + m \quad \begin{array}{c|c|c} x_1 & x_2 \\ \hline -1 & 1 \end{array} \rightarrow m < 0 \quad (1)$$

$$0 > 0 \rightarrow 1 - 4m > 0 \rightarrow -\frac{1}{4} < m < 0 \quad (2)$$

$$(1) \cap (2) = -\frac{1}{4} < m < 0$$

2

$$\frac{1-\sqrt{5}}{2} \quad , \quad \frac{1+\sqrt{5}}{2} \rightarrow s = \frac{1-\sqrt{5}}{2} \quad , \quad 1 \quad , \quad p = \frac{1+\sqrt{5}}{2} \rightarrow \frac{q-0}{q} = \frac{1}{q}$$

$$ax^2 - 5x + p = 0 \rightarrow (x^2 - 5x + \frac{1}{q} = 0) \times q \rightarrow qx^2 - 5qx + 1 = 0$$

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$$mx^2 - 11x + m + 1 = 0 \quad a < b \quad , \quad 2a^2 + b^2 = 12 \rightarrow 2a^2 + a^2 + 2b^2 - b^2 = 12$$

$$2(a^2 + b^2) + (a^2 - b^2) = 12 \rightarrow 2(s^2 - 2p) + (s(\frac{\sqrt{\Delta}}{|a|})) = 12$$

$$2(1 - 2m) + 2\sqrt{12 - 2m} = 12 \rightarrow (1 - m + \sqrt{12 - 2m})^2 = m^2 - 14m + 41 \rightarrow 1 - 11m + 14 = m^2 - 14m + 41 \rightarrow m = 4$$

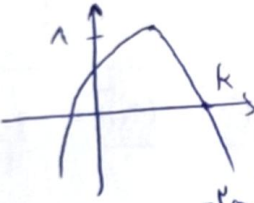
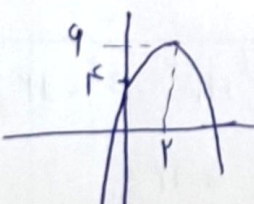
4

$$S(1, 9) \rightarrow C = 0 \quad \frac{-b}{2a} = 1 \rightarrow f_a = -b \rightarrow \frac{-0}{2a} = 9 \rightarrow a^2 + a = 0$$

$$a(a+1) = 0 \rightarrow a = 0, -1 \rightarrow a = -1 \rightarrow b = 1 \rightarrow -x^2 + 1x + 0 = 0$$

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$$(x-2)(x+1) = \frac{-1 \pm \sqrt{1+4}}{2} \rightarrow \text{ریشه ها } (-1, 0) \text{ و } (2, 0)$$

$a\alpha^2 - Va + a\beta = 0 \rightarrow \beta = \frac{V}{a} \rightarrow a + \beta = \frac{V}{a} \quad , \quad a\beta = \frac{a\beta}{a} \rightarrow a\beta = a$ $a \rightarrow \beta = \frac{V}{a} \quad \alpha \quad \left. \begin{array}{l} \frac{1}{a} + \frac{1}{\beta} = \frac{1}{V} + \frac{V}{V} = \frac{V}{V} \end{array} \right\}$ $\rightarrow \beta = \frac{V}{a} \quad \checkmark$	8
$a\beta + m\alpha - Vm = 0 \quad a^2 - m\beta = 1 \rightarrow a = a^2 + am - Vm = 0$ $m\beta + \lambda = Vm - am \rightarrow \underline{am + m\beta} = Vm - \lambda \rightarrow m(\alpha + \beta) = Vm - \lambda$ $-m^2 = Vm - \lambda \rightarrow m^2 + Vm - \lambda = 0 \rightarrow m = \frac{-V \pm \sqrt{V^2 + 4\lambda}}{2}$ $m = V \rightarrow \underline{S = -V}$	V
 $f(x) = mx^2 + kx + \frac{m}{V} + V \rightarrow \frac{-\Delta}{4a} \leq \lambda \rightarrow \frac{m^2 + (Vm - \lambda)^2}{4m} \leq \lambda$ $m^2 - Vm - \lambda \leq 0 \rightarrow m = V \rightarrow m < \lambda \quad \checkmark$ $-Vm^2 + k^2 + 4 \rightarrow a^2 - Vm - V = f(x) \rightarrow (x - V)(x + 1) \rightarrow \alpha = V, \alpha = -1$ $a = V \rightarrow k > 0 \rightarrow \underline{K \leq V}$	A
 $\rightarrow c < r \quad , \quad \frac{-b}{2a} < r \rightarrow r^2 - b = 0 \quad , \quad \frac{-\Delta}{4a} < r \rightarrow a < \frac{1}{r} \quad , \quad b < r$ $-\frac{1}{r} a^2 + k^2 + f = f(x) \rightarrow \frac{1}{a} + \frac{1}{\beta} = \frac{a + \beta}{a\beta} = \frac{-1}{r}$	9
$a^2 - (k + f)\alpha + (ka^2 + 4a + r) = 0 \rightarrow \lambda < r \rightarrow ka^2 - ka - 1 = 0 \rightarrow a < 1, \quad \frac{1}{a} > 1$ $a = 1 \rightarrow ka^2 - ka + r = 0 \rightarrow (a - r)(a - 4) \rightarrow a < 4, \quad r$ $a < \frac{1}{r} \rightarrow a^2 - \frac{1}{r} + \frac{r}{a} = 0 \rightarrow (a - r)(a - \frac{r}{a}) \rightarrow a < \frac{r}{a} > r$ $\Delta > 0 \rightarrow (k + f)^2 - 4(ka^2 + 4a + r) = (4a^2 + r^2ka + 4 - 4ka^2 - 4ka - 4r =$ $ka^2 - ka + r \rightarrow a^2 - kar + r = (a - 1)^2 = 0 \rightarrow a = 1 \quad \underline{a < 4, \quad \frac{r}{a} > r}$	1.