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$2x^2 - ax + 1 = 0$
 $\alpha = 2\beta \Rightarrow S = \frac{a}{2} = 2\beta$
 $P = 2\beta^2 = \frac{1}{2} \quad \beta^2 = \frac{1}{4} \quad \beta = \pm \frac{1}{2}$
 $\beta = \frac{1}{2} \rightarrow \frac{a}{2} = \frac{1}{2} \quad \boxed{a = 1}$
 $\beta = -\frac{1}{2} \quad \frac{a}{2} = -\frac{1}{2} \quad \boxed{a = -1}$

$\Delta = 1 = (1)$

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$2x^2 - (m+1)x + 1 = 0 \quad S = \frac{m+1}{2} \quad P = \frac{1}{2}$
 $\frac{1}{\sqrt{a}} + \frac{1}{\sqrt{b}} = \omega \quad \frac{\sqrt{a} + \sqrt{b}}{\sqrt{ab}} = \frac{\sqrt{a} + \sqrt{b}}{\frac{1}{4}} = \omega \quad \sqrt{a} + \sqrt{b} = \frac{\omega}{4} \Rightarrow \alpha + \beta + \frac{1}{4} = \frac{10}{4}$

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$\alpha + \beta = \frac{10 - 1}{4} = \frac{9}{4} \quad \frac{m+1}{2} = \frac{9}{4} \quad \boxed{m = -1} \rightarrow -x^2 + 2x + 1 = \frac{c}{a} = -1$

$2x^2 + kx - 9x - 1 = 0 \quad \alpha\beta = -1 \quad \alpha = 1$
 $(\alpha + \beta)^2 = 1 = \alpha^2 + \beta^2 - 1 \quad \alpha + \beta = 1 \Rightarrow \beta = -1$
 $\Rightarrow k + 1 + 1 - 1 - 1 = 0 \quad \boxed{k = -2}$

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$x^2 + 4x + a = 0 \quad \alpha < \beta < 0 \quad S = -4 \quad P = a \quad |\alpha - \beta| = \frac{\sqrt{\Delta}}{a} = \frac{\sqrt{16 - 4a}}{1}$
 $\alpha - \beta = -2\sqrt{4 - a}$
 $2\alpha^2 + 2\beta^2 = 12\sqrt{4 - a} + 16$
 $2(\alpha^2 + \beta^2) + 2\alpha\beta = 4 \cdot -4a + 4\sqrt{4 - a} = 16 + 12\sqrt{4 - a}$
 $\frac{4 - 4a}{2\sqrt{4 - a}} = \frac{16 + 12\sqrt{4 - a}}{2\sqrt{4 - a}} \quad \boxed{a = 1}$

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$x^2 - 7x^2 - \omega = 0$
 $x^2 = t \quad t^2 - 7t - \omega = 0 \quad t = \frac{7 \pm \sqrt{49 + 4\omega}}{2} \quad S = 0$
 $\Delta = 49 + 4\omega = 49$
 $\omega = \pm \sqrt{\frac{49 + 49}{4}} \quad P = -\frac{7 - \sqrt{49}}{2}$
 $2P^2 = 2\left(\frac{49 + 49 + 14\sqrt{49}}{4}\right) = \frac{118 + 14\sqrt{49}}{2} = 59 + 7\sqrt{49}$

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$$\begin{aligned}
 & \gamma x^2 - ax + b = 0 & \gamma ax^2 + ax - 4 = 0 \\
 & S: \alpha + \frac{1}{\gamma} + \beta + \frac{1}{\gamma} = \frac{a}{\gamma} & S: \alpha + \beta = -\frac{1}{\gamma} \quad p = -\gamma \\
 & \alpha + \beta = \frac{a}{\gamma} - 1 & -\frac{1}{\gamma} = \frac{a}{\gamma} - 1 \quad \boxed{a=1} \\
 & P = (\alpha + \frac{1}{\gamma})(\beta + \frac{1}{\gamma}) = \alpha\beta + \frac{1}{\gamma}(\alpha + \beta) + \frac{1}{\gamma^2} = \frac{b}{\gamma} \\
 & -\gamma - \frac{1}{\gamma} + \frac{1}{\gamma} = \frac{b}{\gamma} \quad \boxed{b = -4}
 \end{aligned}$$

$$\left[\frac{ab}{c}\right] = \left[\frac{-4}{-1}\right] = -4$$

$$\begin{aligned}
 & ax^2 - ax - b = 0 & \gamma \cdot \beta^2 + \gamma \cdot \alpha^2 - \gamma \cdot \beta = 14 \\
 & \alpha + \beta = 1 & \gamma \cdot (\beta^2 + \alpha^2) + \gamma \cdot (\beta^2 + \alpha^2) = 14 \\
 & \alpha\beta = -\frac{b}{a} & \gamma \cdot \left(\frac{b}{a}\right) + \gamma \cdot \left(\frac{1}{\gamma} - \frac{1}{\gamma}\right) = 14 \\
 & \gamma(\beta^2 - \beta) = b & \frac{\gamma \cdot b}{a} + \gamma \cdot \frac{1}{\gamma} = 14 \quad \frac{b}{a} = -\frac{1}{\gamma} \\
 & |\alpha - \beta| = \frac{\sqrt{\Delta}}{|\alpha|} = \sqrt{1 - \frac{4b}{a}} = \sqrt{\frac{14}{\gamma}} = \frac{\sqrt{14}}{\sqrt{\gamma}}
 \end{aligned}$$

$$P_k^r - (a+1)x + a = 0 \quad r_{k+1}, r_{k-1}$$

$$P_k^r - (a+1)x + b = 0 \quad r_{k'}, r_{k'+r}$$

$$\begin{aligned}
 & P_1 = a = (r_{k+1})(r_{k-1}) = r_{k-1}, S = r_k = a+1 \quad a = r_{k-1} \quad \begin{matrix} w^r = k \\ k=0,1 \end{matrix} \quad \boxed{a=r} \\
 & P_r = b = r_{k'} r_{k'+r} \quad S = r_{k'} + r_{k'+r} = 10 \quad k' = r \quad P_r = b = 14 = \boxed{r \cdot 7} \\
 & r \cdot 7 = 14 \quad \boxed{r=2}
 \end{aligned}$$

$$\begin{aligned}
 & x^2 + x - 1 - m^2 = 0 & \alpha^r + \beta^r = S^r - r p = 1 + -r(-1) = r \\
 & S = -1 \\
 & P: \alpha\beta = -(1+m^2) \xrightarrow{m=0}
 \end{aligned}$$

$$\begin{aligned}
 & y = a(x+1)^r + 1 & \alpha^r + \beta^r = a \\
 & 0 = ax^2 + 2ax + a + 1 & r - \frac{r(r+1)}{a} = a \\
 & S = \frac{-2a}{a} = -2 \quad p = \frac{a+1}{a} & -\frac{ra-r}{a} = 1 \quad -ra - r = a \\
 & & a = \boxed{-\frac{r}{r+1}}
 \end{aligned}$$

$$\begin{aligned}
 & y = -\frac{r}{r+1}(x+1)^r + 1 \\
 & y = -\frac{r}{r+1} + 1 = \boxed{\frac{1}{r+1}}
 \end{aligned}$$