

$$\frac{1}{x-1} = |x-1|$$

$$\frac{1}{x-1} = x-1 \Rightarrow x^2 - 2x + 1 = 1 \Rightarrow x^2 - 2x = 0 \Rightarrow x(x-2) = 0 \Rightarrow x=0 \text{ یا } x=2$$

$$\frac{1}{x-1} = -x+1 \Rightarrow -x^2 + 2x - 1 = 1 \Rightarrow -x^2 + 2x - 2 = 0 \Rightarrow \Delta < 0 \rightarrow \text{ریشه ندارد}$$

if $x=0 \Rightarrow \frac{1}{-1} = |-1| \Rightarrow 1 = -1$ غلط
if $x=2 \Rightarrow \frac{1}{2-1} = |2-1| \Rightarrow 1 = 1$ صحیح ✓

$$x=2$$

الف) $\left| \frac{x-1}{x} \right| < 2$

$$-2 < \frac{x-1}{x} < 2 \Rightarrow \frac{x-1}{x} < 2 \Rightarrow \frac{x-1-2x}{x} < 0 \Rightarrow \frac{-x-1}{x} < 0$$

$$\frac{-x-1}{x} < 0 \Rightarrow \frac{x+1}{x} > 0 \Rightarrow x < -1 \text{ یا } x > 0$$

$$\frac{x-1}{x} > -2 \Rightarrow \frac{x-1+2x}{x} > 0 \Rightarrow \frac{3x-1}{x} > 0 \Rightarrow x < \frac{1}{3} \text{ یا } x > 0$$

$$x < -1 \text{ یا } x > 0 \text{ و } x < \frac{1}{3} \text{ یا } x > 0 \Rightarrow (-\infty, -1) \cup (0, \frac{1}{3})$$

ب) $\left| \frac{x-2}{x+1} \right| > 1$

$$\frac{x-2}{x+1} > 1 \Rightarrow \frac{x-2-x-1}{x+1} > 0 \Rightarrow \frac{-2x-3}{x+1} > 0$$

$$\frac{-2x-3}{x+1} > 0 \Rightarrow \frac{2x+3}{x+1} < 0 \Rightarrow x < -\frac{3}{2} \text{ یا } x > -1$$

$$\frac{x-2}{x+1} < -1 \Rightarrow \frac{x-2+x+1}{x+1} < 0 \Rightarrow \frac{2x-1}{x+1} < 0$$

$$\frac{2x-1}{x+1} < 0 \Rightarrow x < -\frac{1}{2} \text{ یا } x > \frac{1}{2}$$

$$(-\frac{3}{2}, -1) \cup (-\frac{1}{2}, \frac{1}{2})$$

۱) $x^2 < |x+4| \rightarrow |x-\alpha| < \beta$

$$x^2 - x - 4 < 0 \Rightarrow (x-3)(x+2) < 0 \Rightarrow -2 < x < 3$$

$$|x - \frac{1}{2}| < \frac{5}{2} \Rightarrow x - \frac{1}{2} < \frac{5}{2} \text{ و } x - \frac{1}{2} > -\frac{5}{2} \Rightarrow x < 3 \text{ و } x > -2$$

۲) $x^2 + x + 4 < 0 \rightarrow \Delta < 0 \Rightarrow \mathbb{R}$
خارج

$$f = |x+1| - |x| + |x-1|$$

max $\rightarrow 2$
min $\rightarrow -1$
 $J^+ = 2$

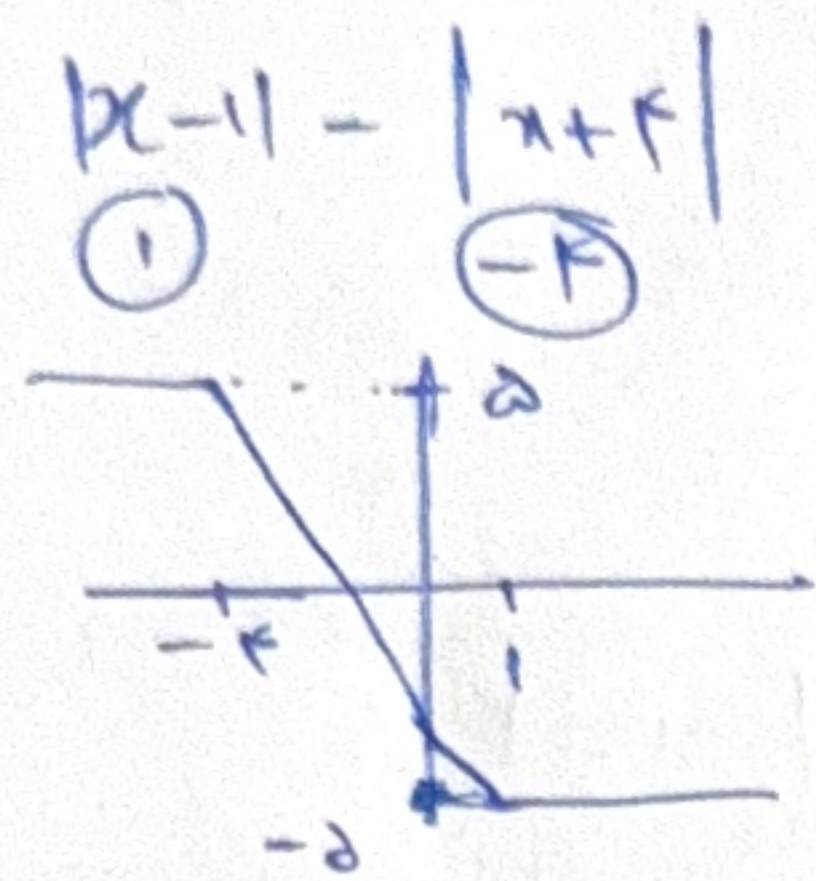
$$\begin{array}{ccccccc} & -1 & & 0 & & 1 & \\ x & -1 & 0 & 1 & 2 & 3 & 4 \\ f & 1 & 1 & 1 & 2 & 3 & 4 \end{array}$$

$$f = \left| \frac{1}{x} \right| - 2 \rightarrow g = \left| \frac{1}{x} + 1 \right| - 1$$

$$\left| \frac{x+1}{x} \right| - 1 = \left| \frac{1}{x} \right| - 2 \rightarrow \frac{x+1}{x} + 1 = \frac{x}{x} - 2 \rightarrow \frac{x+1}{x} = -1$$

$$\frac{x+1}{x} = -1 \Rightarrow x+1 = -x \Rightarrow x = -1$$

الف) $f(x) = [1-x] - [x+4]$



در بازه $R_f = \{-5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5\}$

ب) $f(x) = \frac{1}{x} - \left[\frac{x+1}{x} \right]$

$\frac{1}{x} - \left[\frac{x+1}{x} \right]$

$f(x) = \frac{1}{x} - 1 - \left[\frac{1}{x} \right] \rightarrow \frac{1}{x} - \left[\frac{1}{x} \right] - 1$
نیل $\frac{x - [x]}{[0, 1)}$

$R_f = [-1, 0)$

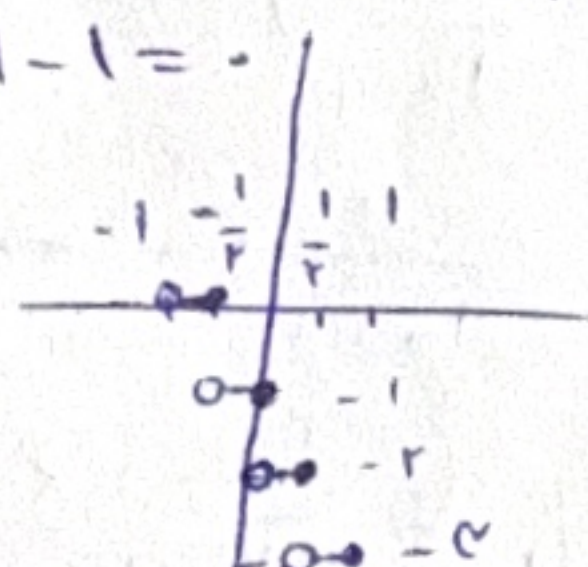
الف) $y = [-2x] - 1$ $x \in (-1, 1)$

$-1 < x < 0 \Rightarrow -2 < -2x < 0 \Rightarrow y = -1 - 1 = -2$

$0 < x < 1 \Rightarrow -2 < -2x < 0 \Rightarrow y = 0 - 1 = -1$

$-1 < x < 0 \Rightarrow -2 < -2x < 0 \Rightarrow y = -1 - 1 = -2$

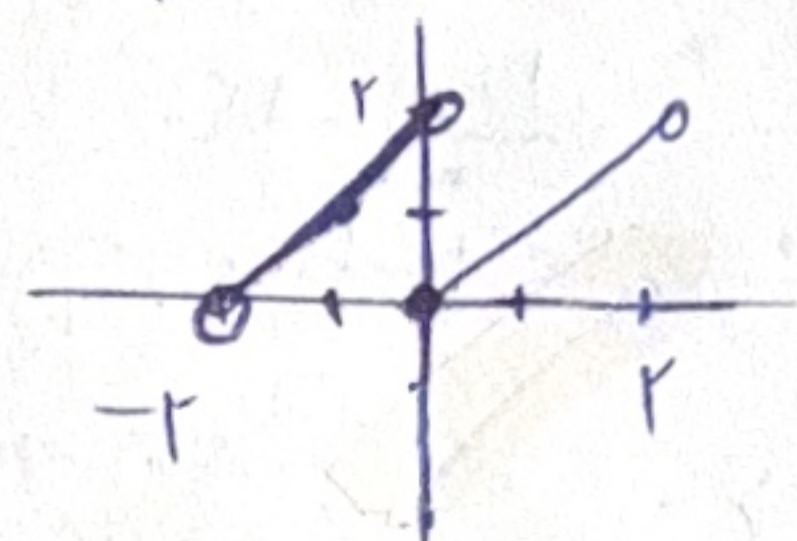
$0 < x < 1 \Rightarrow -2 < -2x < 0 \Rightarrow y = 0 - 1 = -1$



ب) $y = x - r \left[\frac{x}{r} \right]$ $x \in (-r, r)$

$-r < x < 0 \Rightarrow -r < x - r \left[\frac{x}{r} \right] < 0$

$0 < x < r \Rightarrow 0 < x - r \left[\frac{x}{r} \right] < r$



الف) $y = [|x| - 1]$ $x \in [-r, r]$

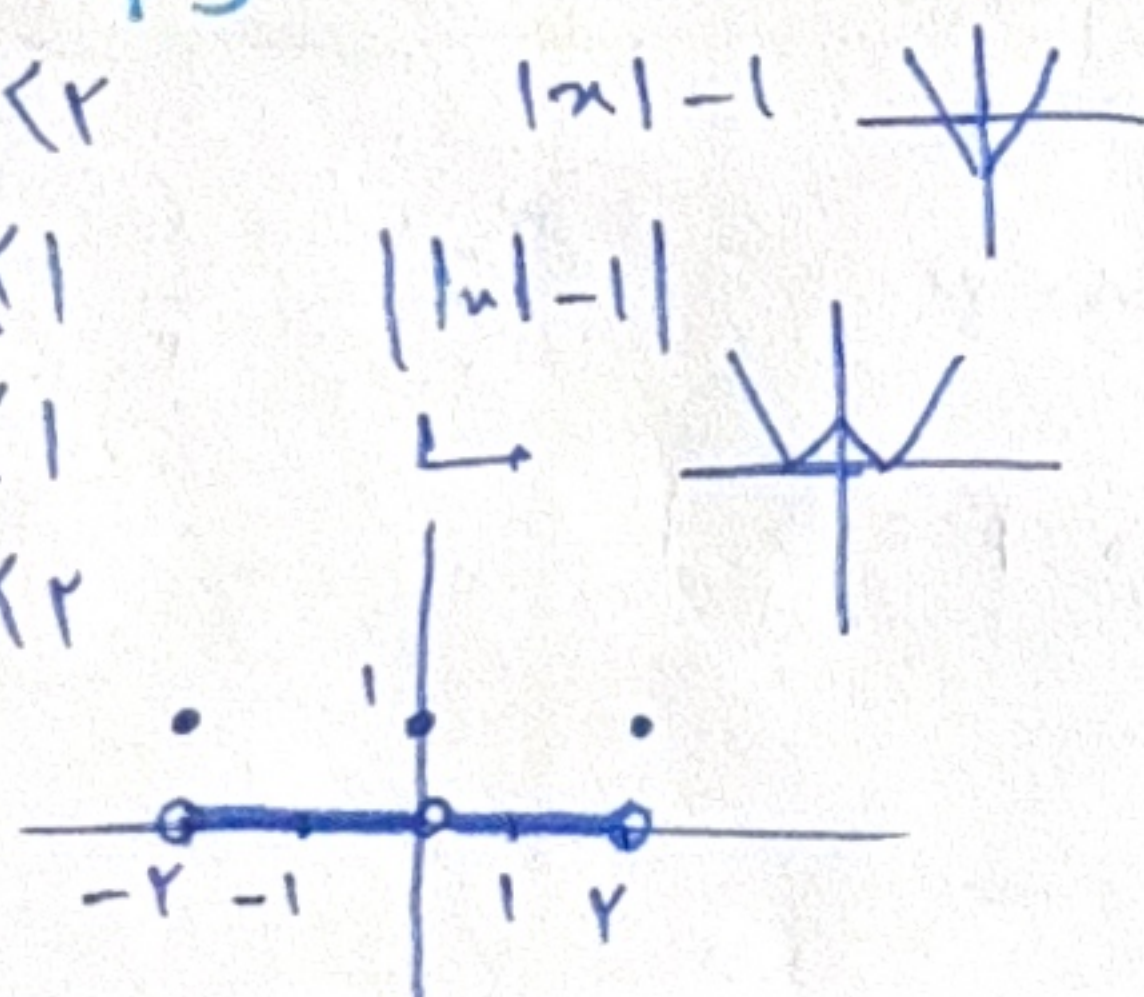
$-r < x < -1 \Rightarrow -r < |x| < -1$

$-1 < x < 0 \Rightarrow -1 < |x| < 0$

$0 < x < 1 \Rightarrow 0 < |x| < 1$

$1 < x < r \Rightarrow 1 < |x| < r$

$x = r$

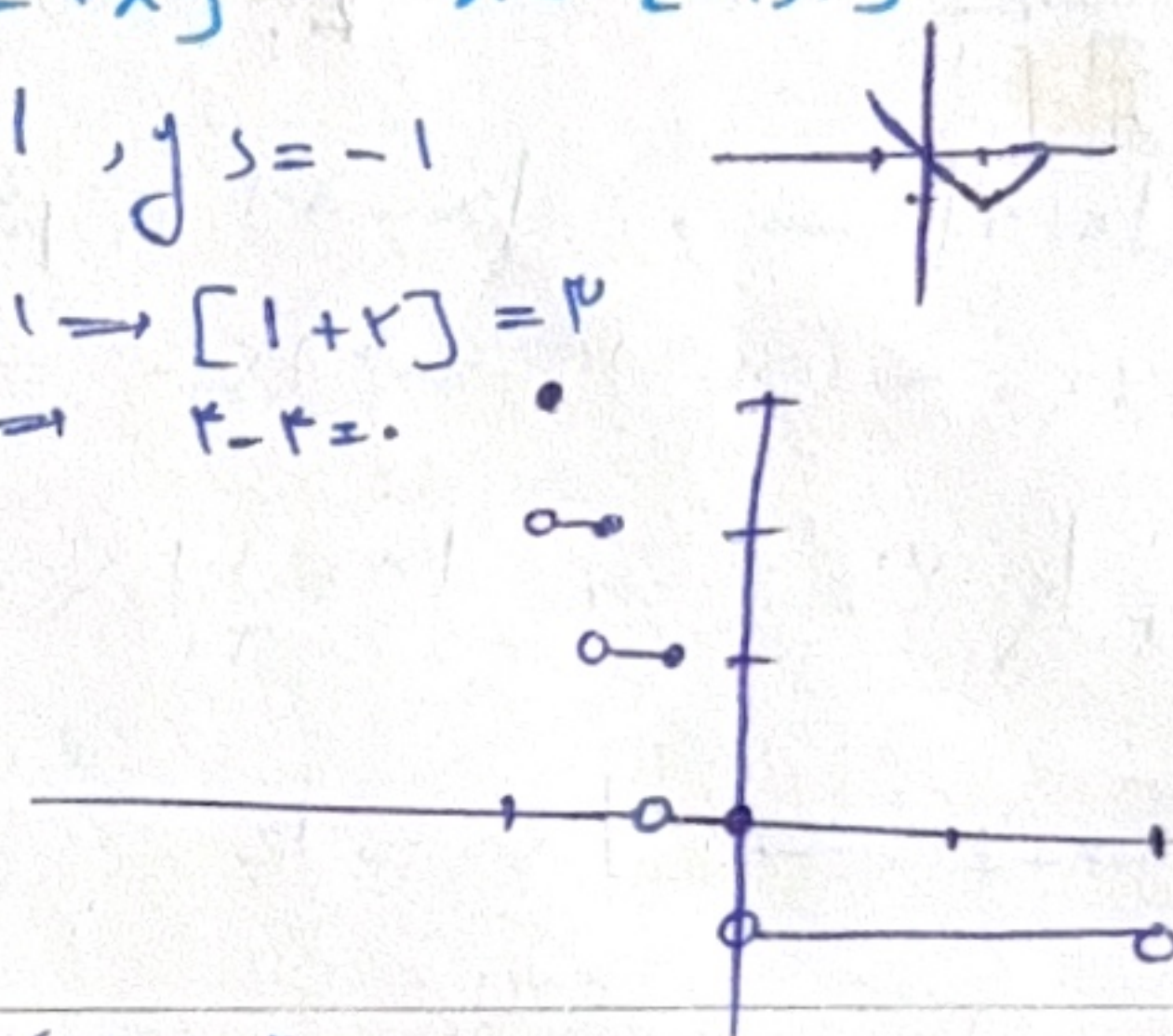


ب) $y = [x^2 - rx]$ $x \in [-1, r]$

$x \in [-1, r] \Rightarrow y \in [-1, r]$

if $x = -1 \Rightarrow [1 - r] = r$

if $x = r \Rightarrow r - r = 0$



$a + [b] = fr$

$a = x + yr$

$b - [a] = r/r$

$b = y + 1/r$

$a + b = ?$

$a + [b] = fr \Rightarrow x + yr + [y + 1/r] = fr$

$x + y + 0 = fr \Rightarrow x + y = fr$ (1)

$b - [a] = r/r$

$y + 1/r - [x + yr] = y + 1/r - x = r/r = y - x = r$ (2)

(1) $x + y = fr$

(2) $y - x = r$

$y = r \Rightarrow y = r \Rightarrow x = 1$

$a = 1 + yr = 1/r$

$b = r + 1/r = r/r$

$\oplus \begin{matrix} 1/r + r/r \\ = \\ fr \end{matrix}$

$(1+\sqrt{2})^4 + (1-\sqrt{2})^4 = 198$

$(1+\sqrt{2})^4 \rightarrow (1+\sqrt{2})^4$

$(1+\sqrt{2})^4 = 198 - (1-\sqrt{2})^4$

عدد صحیح منفی $\frac{1}{2}$ عدد صحیح منفی $\frac{1}{2}$ عدد صحیح منفی $\frac{1}{2}$

$\Rightarrow (1+\sqrt{2})^4 = 198 - 0$

$(1+\sqrt{2})^4 = 198$

$[(1+\sqrt{2})^4] = 198$