

$$EO = 2AE \quad \frac{EF}{AF} = ?$$

$$\frac{AE}{BE} = \frac{EF}{FB} = \frac{AF}{FC} = \frac{1}{2}$$

$$\Rightarrow \frac{EF}{FB+EF} = \frac{AF}{FC+AF} = \frac{1}{3}$$

$$\Rightarrow \frac{EF}{\sqrt{10}} = \frac{AF}{3\sqrt{2}} = \frac{1}{3}$$

$$\frac{EF}{AF} = \frac{\frac{\sqrt{10}}{3}}{\frac{\sqrt{2}}{3}} = \frac{\sqrt{10}}{\sqrt{2}}$$

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$$\frac{x}{x+13} = \frac{4}{x+1} \Rightarrow x^2 + x = 40 \Rightarrow x(x+1) = 40 \Rightarrow x = 8$$

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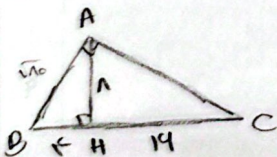
$$DE \parallel BC \quad 2y = 5x \quad BF = 3 \quad BC = ? \Rightarrow y = \frac{5}{2}x$$

$$ADE \sim ABC \Rightarrow \frac{AE}{AC} = \frac{DE}{BC} \Rightarrow \frac{x}{3x} = \frac{DE}{BC} = \frac{1}{3} \Rightarrow BC = 3DE \Rightarrow BC = 9$$

$$AC = x+1, y = x+1, \left(\frac{5}{2}x\right) = 3x$$

$$\frac{DE}{BC} = \frac{1}{3} \Rightarrow DE = 3$$

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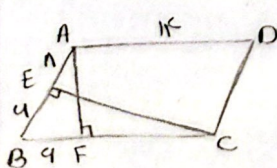


$$AH^2 = BH \times HC = 4 \times 1 \Rightarrow AH = 2$$

$$\triangle ABH \sim \triangle ABC \Rightarrow \frac{AB}{AC} = \frac{BH}{AH} = \frac{4}{2} = \frac{1}{2}$$

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$$AD = 14 \quad BF = 4 \quad AE = 1 \quad AF = ?$$



$$\triangle ABF \sim \triangle ECF$$

$$\frac{AB}{EC} = \frac{BF}{FC} = \frac{AF}{EF} \Rightarrow \frac{1+EB}{14} = \frac{4}{EB} \Rightarrow EB^2 + EB - 14 = 0$$

$$(EB-4)(EB+14) = 0 \Rightarrow EB = 4$$

$$AB^2 = AF^2 + BF^2 \Rightarrow 14^2 = AF^2 + 4^2 \Rightarrow AF = \sqrt{140} = 2\sqrt{35}$$

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