

$$\lim_{n \rightarrow 1} \frac{f_n^2 - \sqrt{1+n^2}}{2n^2 - 1 + n^2} = \frac{(n-1)(f_n^2)}{(n-1)(2n^2)} = \frac{f_n^2}{2n^2} = \frac{1}{2}$$

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$$\lim_{n \rightarrow 0} \frac{|f_n - 1| - |f_n + 1|}{n} \begin{cases} \rightarrow \frac{(\sqrt{n} - 1) - (\sqrt{n} + 1)}{n} = \frac{-2}{n} = -2 \\ \rightarrow \frac{(-\sqrt{n} - 1) - (-\sqrt{n} + 1)}{n} = \frac{-2}{n} = -2 \end{cases}$$

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$$\lim_{n \rightarrow f} \frac{n-f}{\sqrt{n}-f} = \frac{(\sqrt{n}-f)(\sqrt{n}+f)}{\sqrt{n}-f} = \sqrt{n}+f$$

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$$\lim_{n \rightarrow 2} \frac{n - \sqrt{n}}{n^2 - n - 4} = \frac{\sqrt{n}(\sqrt{n} - 1)}{(n-2)(n+4)} = \frac{\sqrt{n}}{(\sqrt{n}+2)(n+4)} = \frac{\sqrt{2}}{2\sqrt{2} \cdot 6} = \frac{\sqrt{2}}{12\sqrt{2}} = \frac{1}{12}$$

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$$\lim \frac{1-\sqrt{n}}{n\sqrt{a}-n} \times \frac{1+\sqrt{n}}{1+\sqrt{n}} \times \frac{1}{1+\sqrt{n}} = \frac{(1-n)\sqrt{n}}{(1-n)(n)} = \frac{(1-\sqrt{n})\sqrt{n}}{-(1-\sqrt{n})n} = \frac{-\sqrt{n}}{n} = -\frac{1}{\sqrt{n}}$$

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$$\lim_{x \rightarrow \frac{\pi}{2}} \frac{\sqrt{4x+1} - 2}{\sqrt{2x+1} - \sqrt{x}} \times \frac{\sqrt{4x+1} + 2}{\sqrt{4x+1} + 2} = \frac{4x - 4}{(\sqrt{4x+1} + 2)(\sqrt{2x+1} - \sqrt{x})} = \frac{4(x-1)}{4(x-1)} \times \frac{2}{\sqrt{2x+1} + \sqrt{x}} = \frac{2}{\sqrt{2x+1} + \sqrt{x}} = \frac{2}{\sqrt{2 \cdot \frac{\pi}{2} + 1} + \sqrt{\frac{\pi}{2}}} = \frac{2}{\sqrt{\pi+1} + \sqrt{\frac{\pi}{2}}}$$

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$$\lim_{x \rightarrow 1} \frac{\sqrt{4x+1} - 2}{\sqrt{x} - 1} \times \frac{\sqrt{4x+1} + 2}{\sqrt{4x+1} + 2} \times \frac{\sqrt{x} + \sqrt{x+1}}{\sqrt{x} + \sqrt{x+1}} = \frac{(4x-4)(\sqrt{x} + \sqrt{x+1})}{(x-1)(\sqrt{4x+1} + 2)(\sqrt{x} + \sqrt{x+1})}$$

$$= \frac{4[(\sqrt{x}-1)(\sqrt{x} + \frac{1}{\sqrt{x}})]}{4(\sqrt{x}-1)(\sqrt{x+1})} = \frac{1}{\sqrt{x+1}}$$

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$$\lim_{x \rightarrow \pi} \frac{1 + \cos x}{\sin x} = \frac{(1 + \cos x)(1 - \cos x + \cos x)}{(1 - \cos x)(1 + \cos x)} = \frac{1 - \cos x + \cos^2 x}{1 - \cos x} = \frac{1 + 1}{1 + 1} = \frac{2}{2} = 1$$

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$$\lim_{x \rightarrow \frac{\pi}{2}} \frac{1 - \tan x}{\sin x - \cos x} = \frac{1 - \frac{\sin x}{\cos x}}{\frac{\sin x}{\cos x} - \cos x} = \frac{\frac{\cos x - \sin x}{\cos x}}{\frac{\sin x - \cos^2 x}{\cos x}} = \frac{\cos x - \sin x}{\sin x - \cos^2 x} = \frac{-1}{\cos x} = \frac{-1}{\sqrt{\frac{\pi}{2}}} = -\sqrt{\frac{2}{\pi}}$$

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$$\lim_{x \rightarrow \frac{\pi}{2}} \frac{\tan x - 1}{\cos x} = \frac{\frac{\sin x}{\cos x} - 1}{\cos x} = \frac{\frac{\sin x - \cos x}{\cos x}}{\cos x} = \frac{\sin x - \cos x}{\cos^2 x} = \frac{-1 - 1}{1} = -2$$

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