

$$f(x^r + n) = r x^r - 1$$

$$x^r + n = r \rightarrow n = 1$$

$$x^r + n = 1 \rightarrow n = r$$

$$f(r) + f(1) = r(1)^{r-1} - 1 + r(r)^{r-1} - 1 = r - 1 + 1 - 1 = \Delta$$

5

$$f(x) = x^r - 5x^r + 12x$$

$$g(x) = x^r + 9x^r + 12x$$

$$(x-1)^r + 1 \quad (x+1)^r - 12$$

$$\frac{g(\sqrt{r}-1)}{f(\sqrt{r}+1)} = \frac{(\sqrt{r}-1)^r - 12}{(\sqrt{r}+1)^r + 1} = \frac{1-12}{1+1} = \frac{-11}{2} = -\frac{11}{2}$$

5

$$f(x) = \sqrt{x+1} \sqrt{x-1} = \sqrt{(x+1)(x-1)} = \sqrt{x^2-1} = x + \sqrt{x-1}$$

$$g(x) = \sqrt{x-1} \sqrt{x-1} = \sqrt{(x-1)(x-1)} = \sqrt{x-1} = \sqrt{x-1} - 1$$

$$f(x) + g(x) = a + b\sqrt{x+c} \Rightarrow x + \sqrt{x-1} + \sqrt{x-1} - 1$$

$$a = 0 \quad b = 1 \quad c = -1 \quad \frac{a+b}{c} = \frac{0+1}{-1} = -1$$

$$Df = (n-1)(n-3) \rightarrow n \neq 1, 3$$

$$g(n) = \{(1,1), (1,0), (3,0), (0,3)\}$$

$$\frac{g}{f} = \left\{ \left(1, \frac{1}{1}\right), \left(1, \frac{0}{1}\right), \left(3, \frac{0}{1}\right), \left(0, \frac{3}{1}\right) \right\}$$

1, 1, 3

$$f(x) = \left\{ \left(\frac{1}{2}, 2\right), \left(\frac{3}{2}, -1\right), (2, 2), \left(-\frac{1}{2}, 5\right) \right\}$$

$$f(x^2) = \left\{ (1, 2), (\sqrt{3}, -1), (2, 2), (\sqrt{-1}, 5) \right\}$$

$$g(x) + 1 = \{(-2, 19), (1, 3), (3, 9), (-1, 1)\}$$

$$\frac{g}{f} = \left\{ (1, -4), (3, -1), (-1, \frac{1}{5}) \right\}$$

1, 0

$$y = \sqrt{x^3 f(x+1)} \rightarrow x^3 \times \left(\frac{1}{x}\right)^{x+1-1} = x^3 \times \left(\frac{1}{x}\right)^x = x^3 \times \frac{1}{x^x} = \frac{x^3}{x^x} = x^{3-x}$$

$$\frac{x^3}{x^{x-1}} - x^3 \geq 0 \rightarrow x^3 \left(\frac{1}{x^{x-1}} - 1\right) \geq 0 \rightarrow x^3 (1 - x^{x-1}) \geq 0$$

$$D_y = [0, 1]$$

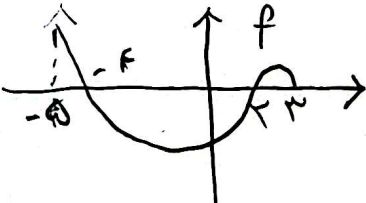
$$f(x) = \sqrt{x + |x+2|}$$

$$f(-x) = \sqrt{-x + |2-x|}$$

$$-x + |2-x| \geq 0 \rightarrow \begin{cases} x \geq 2 \rightarrow -x + x - 2 = -2 < 0 \times \\ x < 2 \rightarrow -x + 2 - x = -2x + 2 \geq 0 \Rightarrow -2x \geq -2 \Rightarrow x \leq 1 \end{cases}$$

$$D_f = [1, +\infty)$$

$$D_f = (-\infty, 1]$$

$$y = \sqrt{\frac{x-1}{f(x)}} \quad \frac{x-1}{f(x)} \geq 0$$


$$D_y = (-1, 1] \cup (2, 3)$$

$$y = \sqrt{x^3 + x - \frac{7x}{x^3} - \frac{4}{x}} \rightarrow x^3 + x^3 - 7x^2 - 4x \geq 0$$

$$(x^3 - 4x) + (x^3 - 7x^2) \Rightarrow (x^2 - 4) + x(x^2 - 7x) \Rightarrow (x-2)(x+2) + x^2(x-7)$$

$$\Rightarrow (x-2)(x^2 + 7x + 14) + x^2(x-7) \Rightarrow (x-2)(x^2 + 7x + 14 + x^3 - 7x^2) \Rightarrow (x-2)(x^3 - 6x^2 + 14x + 14)$$

$$\Rightarrow (x-2)(x-2)(x^2 + 10x + 7) \Rightarrow (x-2)^2(x^2 + 10x + 7) \Rightarrow (x-2)^2(x+2)(x+7)$$

$$D_y = [-2, 0) \cup [2, +\infty)$$

$$9x^4 - x^2 - 5x^2 - 4x - 3$$

$$(3x^2 - x)(3x^2 + x) \rightarrow (3x^2 - x + 1)(3x^2 - x - 3) \rightarrow a=+1, b=+1 \rightarrow \sqrt{-(-1)} \times$$

$$(3x^2 - x + 0)(3x^2 + x + 0) \rightarrow a=-1, b=-3 \rightarrow \sqrt{-(-1)} \times$$

$$9x^4 + (3x^2 + 1)(-1)x^2 + (-0 + 0)x + 0 \times 0 = 9x^4 - 3x^2 - x^2 - 0x - 0 = 9x^4 - 4x^2$$

$$3x^2 + 1 = -1 \Rightarrow 3x^2 = -2 \Rightarrow x^2 = -\frac{2}{3} \Rightarrow x = \pm i\sqrt{\frac{2}{3}}$$

$$3x^2 - x = -3 \Rightarrow 3x^2 - 1 = -2 \Rightarrow 3x^2 = -1 \Rightarrow x^2 = -\frac{1}{3} \Rightarrow x = \pm i\sqrt{\frac{1}{3}}$$

$$\text{ب ۱۰) } \left\{ \begin{array}{l} x^r = 1 \rightarrow x = \pm 1 \\ x^r = r \rightarrow x = \pm r \\ x^r = r \rightarrow x = \pm r \\ x^r = -1 \rightarrow x \end{array} \right. \rightarrow \left\{ (\pm 1, r) (\pm \sqrt{r}, -1) (\pm r, r) \right\}$$