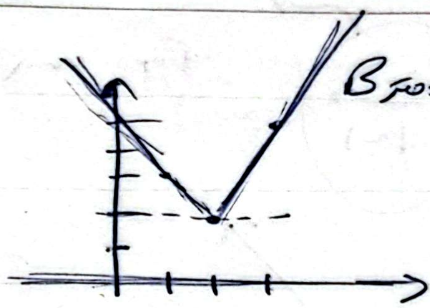
کیمیا عطایی یازدهم دختر B

۱) الف)



$y = x + |2x - 4|$

$R_f = [2, +\infty)$

ب)

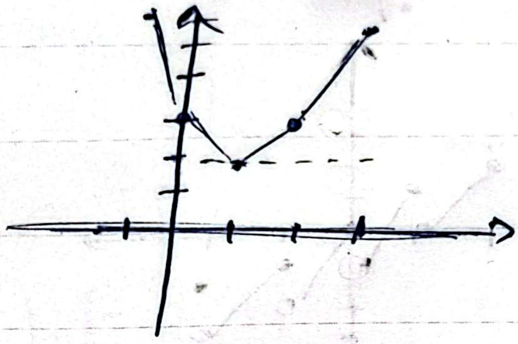
$|x-2| + |x-1| - |x|$

$x > 2 : \quad x - 2 + x - 1 + x = 3x - 3$

$2 > x > 1 : \quad 2 - x + x - 1 + x = x + 1$

$1 > x > 0 : \quad 2 - x + x + 1 - x \Rightarrow 3 - x$

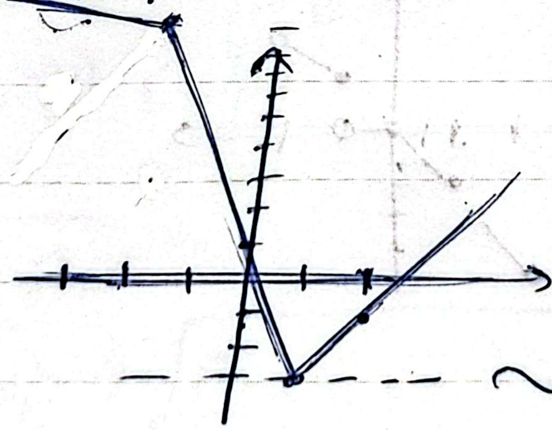
$x < 0 : \quad 2 - x + 1 - x - x = 3 - 3x$



$R_f = [2, +\infty)$

۲)

$|2x - 3| - |x + 2| = k \qquad k ?$



$\rightsquigarrow k = -3$

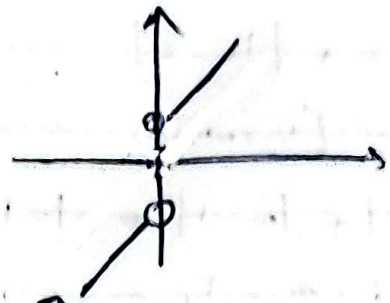
Subject:

Date: / /

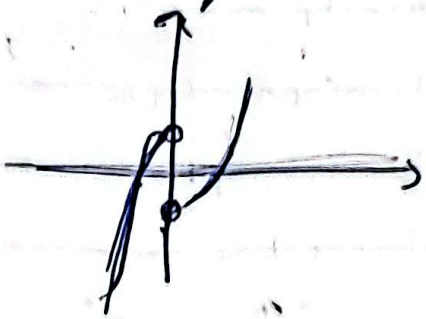
$y = x + \frac{x}{|x|}$ for $x > 0 \Rightarrow 1$

for $x < 0 \Rightarrow -1$

(10)

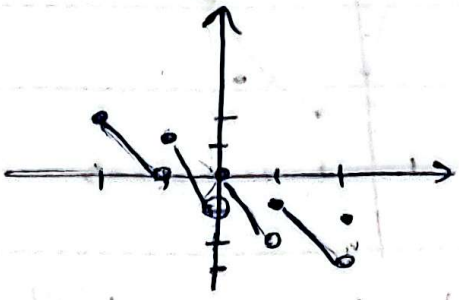


$y = x|x| - \frac{x}{|x|}$

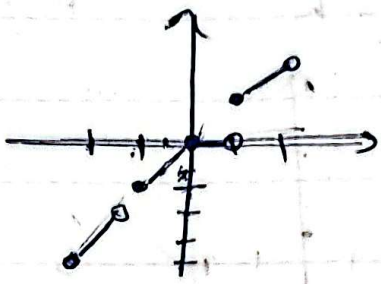


$y = [x] - 2x$

(11)



$y = [x]|x|$



(12)

$y = e_x - [e_x]$ $\quad e_x = \alpha \cdot 10^x - [\alpha \cdot 10^x] < 1$

$[0, 1)$

$10^x - [10^x] = \epsilon(x - [x]) \quad \epsilon \in [0, 1) = [0, \epsilon)$

SuperBind

Subject:

Date: / /

$y = x - 5\left[\frac{x}{5}\right] \rightsquigarrow 5\frac{x}{5} - 5\left[\frac{x}{5}\right] = 5\left(\frac{x}{5} - \left[\frac{x}{5}\right]\right)$

$5 \times [0,1) = [0,5)$

$y = [\tan x] - \tan x = (-1, 0]$

$y = 3\sin x + 4\cos x$ ⑨ $\quad |a\sin x + b\cos x| \leq \sqrt{a^2+b^2}$

$\sqrt{a^2+b^2}$

$\hookrightarrow [-\sqrt{25}, +\sqrt{25}]$

$y = 3\sin x - 4\cos x \hookrightarrow [-5, +5]$

$y = [2\sin x + 5\cos x]$

$\hookrightarrow [-\sqrt{29}] = -6$

$[\sqrt{29}] = 5$

$\{k \in \mathbb{Z}, -6 \leq k \leq 5\}$

$y = \sqrt{\cos x - 2\sin x}$

زیر رادیکال مثبت شود $\hookrightarrow \sqrt{[-\sqrt{5}, \sqrt{5}]} = [0, \sqrt[4]{5}]$

Subject:
Date: / /

$y = \sin^2 x + 3\sin x + 2 \xrightarrow{-1} 0$ $\quad 1 \to 6 \quad [0, 6]$ (7)

$\sin x_{ext} = \frac{-3}{2}$ ✗

$y = 2\sin^2 x + 3\sin x + 2 \longrightarrow \sin x\ ext = -\frac{3}{4} \longrightarrow$

$2\left(\frac{9}{16}\right) - 3\left(\frac{3}{4}\right) + 2 = \frac{7}{8}$

$1 \to 7$

$-1 \to 2 - 3 + 2 = 1 \quad [\frac{7}{8}, 7]$

$y = \sin^2 x + 4\cos^2 x = 1 + 3\cos^2 x \longrightarrow [1, 4]$ (8)

$y = \frac{2\cot x}{1+\cot^2 x}$, $1+\cot^2 x \to \csc^2 x$, $\frac{2\sin^2 x\cos x}{\sin x} = \sin 2x \to [-1, 1]$

$y = \sin^6 x + \cos^6 x \longrightarrow k = 3$ (9)

$[\frac{1}{4}, 1]$

$y = [\sin^8 x + \cos^8 x] \Rightarrow \{0, 1\}$

$y = \frac{2x^2 + 7x - 4}{x + 4}$ (10)

$2x^2 + 7x - 4 \mid x+4$

$2x^2 + 8x \quad\quad 2x - 1$

$-x - 4$

$2(-4) - 1 \longleftarrow$

$\mathbb{R} - \{-9\}$

SuperBind