

کتاب شماره ۷

بزرگم و صبرانه

بدرستی

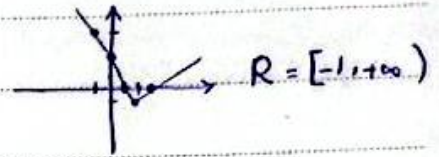
الف) $y = x + \frac{|x-2|}{x-2}$

$\Rightarrow \frac{2}{-x+2} \quad x-2$
 $x=2 \rightarrow y=5$
 $x=0 \rightarrow y=4$

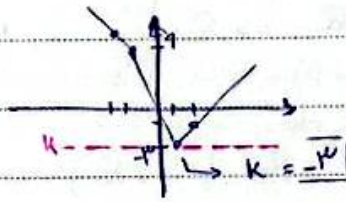


ب) $y = |x-2| + |x-1| - |x|$

$\Rightarrow \frac{0}{-x+2} \quad \frac{1}{-x+1} \quad \frac{2}{x-3}$
 $x=2 \rightarrow 0$
 $x=-1 \rightarrow 5$



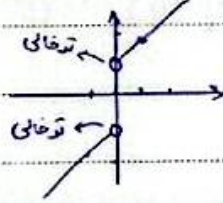
$\frac{-2}{-x+2} \quad \frac{1}{-x+1} \quad \frac{2}{x-3}$
 $x=2 \rightarrow -1$
 $x=-3 \rightarrow 11$



۲. همیشه در هر K مقدار K در یک نقطه مشترک هستند.

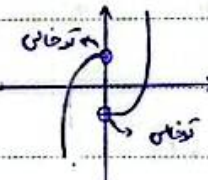
الف) $y = x + \frac{x}{n}$

$\frac{0}{x-1} \quad \frac{1}{x+1}$



ب) $y = x/n - \frac{n}{|n|}$

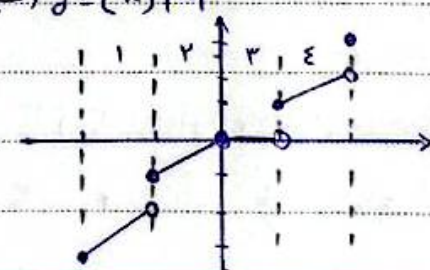
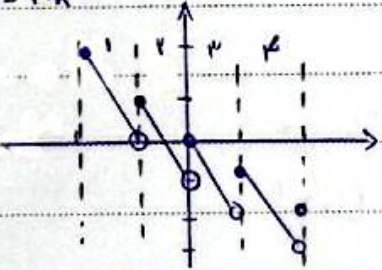
$\frac{0}{-x+1} \quad \frac{1}{x-1}$



الف) $y = [x] - 2x$

ب) $y = [x]/|x|$

$1 \rightarrow -2-2x$
 $2 \rightarrow -1-2x$
 $3 \rightarrow 0-2x = -2x$
 $4 \rightarrow 1-2x$
 $x=2 \rightarrow -2$



$1 \rightarrow -2/|x|$
 $2 \rightarrow -1/|x|$
 $3 \rightarrow 0$
 $4 \rightarrow 1/|x|$
 $x=2 \rightarrow 2$

الف) $y = f(x) - [f(x)] \rightarrow R = [0, 1)$

ب) $y = f(x) - f([x]) = f(\underbrace{x - [x]}_{[0, 1)}) \rightarrow [0, 1)$

$$c) y = n - a \left[\frac{n}{a} \right] = a \left(\frac{n}{a} - \left[\frac{n}{a} \right] \right) \rightarrow R = [0, a)$$

$$d) y = [x_n] - x_n = - \left(x_n - [x_n] \right) \rightarrow R = (-1, 0]$$

$$-\sqrt{a^2 + b^2} \leq a \sin n + b \cos n \leq \sqrt{a^2 + b^2} \quad -4$$

$$i) y = r \sin n + r \cos n \rightarrow -\sqrt{1^2 + 1^2} \leq y \leq \sqrt{1^2 + 1^2} \Rightarrow R = [-\sqrt{2}, \sqrt{2}]$$

$$ii) y = r \sin n - r \cos n \rightarrow -\sqrt{r^2 + r^2} \leq y \leq \sqrt{r^2 + r^2} \Rightarrow R = [-r, r]$$

$$e) y = [r \sin n + a \cos n] \xrightarrow{t} -\sqrt{r^2 + a^2} \leq t \leq \sqrt{r^2 + a^2} \Rightarrow R = \left\{ \begin{matrix} -y \\ -a \\ -r \\ a \end{matrix} \right\} \Rightarrow R = \{-y, -a, \dots, a\}$$

$$f) y = \sqrt{\cos n - r \sin n} \xrightarrow{t} -\sqrt{a} \leq t \leq \sqrt{a} \Rightarrow R = [0, \sqrt{a}]$$

$$iii) \sin^2 n + r \sin n + r$$

$$\sin n = 1 \rightarrow y = 4 \quad \sin n = \frac{-b}{ra} = \frac{-r}{r} \rightarrow y = \frac{-1}{r} \Rightarrow R = \left[\frac{-1}{r}, 4 \right]$$

$$\sin n = -1 \rightarrow y = 0$$

$$iv) r \sin^2 n + r \sin n + r$$

$$\sin n = 1 \rightarrow y = v \quad \sin n = \frac{-b}{ra} = \frac{-r}{r} \rightarrow y = \frac{v}{r} \Rightarrow R = \left[\frac{v}{r}, v \right]$$

$$\sin n = -1 \rightarrow y = 1$$

$$v) y = \sin^2 n + r \cos n = \sin^2 n + r(1 - \sin^2 n) = -r \sin^2 n + r$$

$$\sin n = 1 \rightarrow 1 \quad \sin n = \frac{-b}{ra} = 0 \rightarrow r \Rightarrow R = [1, r]$$

$$vi) y = \frac{r \cot n}{1 + \cot^2 n} = \frac{r \cos n}{\sin n} \times \sin^2 n = r \sin n \cos n = \sin^2 n \Rightarrow R = [-1, 1]$$

$$(a) y = \sin^k n + \cos^k n$$

$$1-k \leq \sin^{2k} n + \cos^{2k} n \leq 1 \quad -9$$

$$k=3 \rightarrow \frac{1}{8} \leq y \leq 1 \Rightarrow R = [\frac{1}{8}, 1]$$

$$(b) y = [\sin^k n + \cos^k n]$$

$$k=2 \rightarrow \frac{1}{2} \leq \sin^2 n + \cos^2 n \leq 1 \Rightarrow \frac{1}{2} \leq \sin^2 n + \cos^2 n \leq 1 \xrightarrow{\text{بالتالي}} R = \{0, 1\}$$

$$(c) y = 2n^2 + 7n - 9$$

$$\frac{2n^2 + 7n - 9}{n-1} \Rightarrow \text{if } n = -9 \rightarrow y = 2(-9) - 1 = -19 \Rightarrow R = \mathbb{R} - \{-9\}$$

$$(d) \frac{n-1}{n-1} = \frac{(n-1)(n^2+1+n)}{n-1} = n^2 + n + 1$$

$$\text{if } n=1 \rightarrow y=3 \Rightarrow R = \mathbb{R} - \{3\}$$