

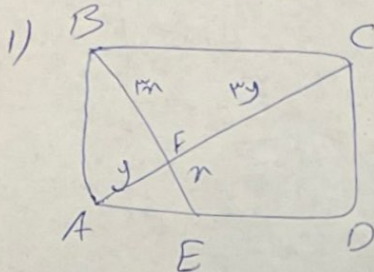
بسمه تعالی

# موسسه مالی و اعتباری ثامن الحجج (ع)



(تحت نظارت بانک مرکزی)

تاریخ: .....  
شماره: .....  
پیوست: .....



$$\left. \begin{array}{l} \triangle ABC : (xy)^2 = 1n \\ \triangle ABE : (xn)^2 = 1 \end{array} \right\} \div \frac{x^2}{y^2} = \frac{10}{18} = \frac{5}{9} \rightarrow \frac{x}{y} = \frac{\sqrt{5}}{3}$$

۲)  $\triangle AED \sim \triangle ABC \Rightarrow \frac{x}{x+1} = \frac{n}{10} \rightarrow n^2 + n = 10 \rightarrow n^2 + n - 10 = 0$   
 $(n+4)(n-5) = 0$   
 $n = -4 \text{ یا } n = 5 \checkmark$

۳)

$$\frac{x}{y} = \frac{2}{8} \rightarrow \frac{x}{y} = \frac{1}{4} \rightarrow x = \frac{1}{4}y$$

$$\frac{10}{x} = \frac{10}{\frac{1}{4}y} = \frac{40}{y} = \frac{10}{2} = 5 \rightarrow y = 8$$

$$BF + FC = 2 + 10 = 12 \text{ یا } 4, 10 \checkmark$$

۴)

$$\begin{array}{l} a^2 = 8 \times 12 \\ b^2 = 14 \times 12 \end{array} \rightarrow \frac{b^2}{a^2} = \frac{14}{8} = \frac{7}{4} \rightarrow \frac{b}{a} = \frac{\sqrt{7}}{2}$$

۵)

$$\triangle EFC \sim \triangle AFB \Rightarrow \frac{n}{4} = \frac{1}{n+1} \rightarrow n^2 + n - 4 = 0$$

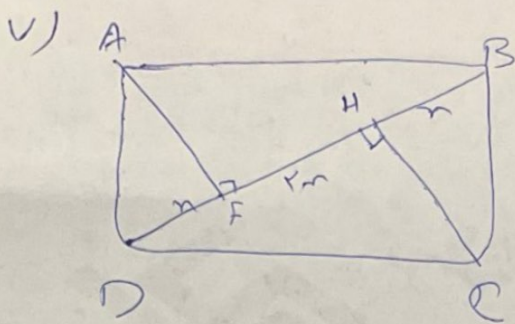
$$(n+2)(n-2) = 0 \rightarrow n = 2 \checkmark$$

$$AF = 12 \checkmark$$

۶)

$$\frac{n+20}{20} = \frac{50}{10} \rightarrow \frac{n}{20} = \frac{30}{10} \rightarrow n = 60 \checkmark$$

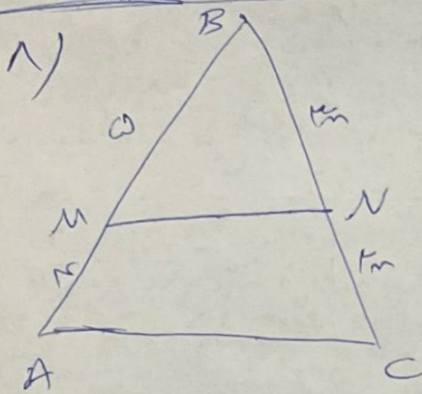




$$BH \leq DF \leq \frac{1}{r} FH$$

$$\frac{S_{HBC}}{S_{BCD}} \leq \frac{1}{\varepsilon} \rightarrow \frac{S_{ABC}}{S_{BCD}} \times \frac{S_{BCD}}{S_{ABCD}} \leq \frac{S_{HBC}}{S_{ABCD}}$$

$$\frac{1}{\varepsilon} \times \frac{1}{r} \leq \frac{1}{\Lambda} \leq \frac{S_{ABCD}}{S_{HBC}}$$



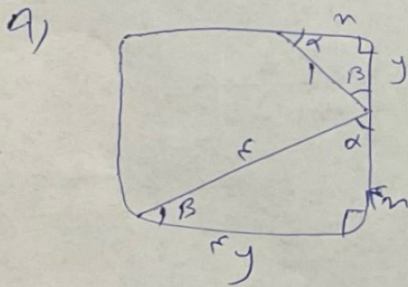
$$\frac{BN}{NC} \leq \frac{r}{r}$$

$$S_{ABC} = r S_{BMN}$$

$$\rightarrow \frac{1}{r} \times w \times AB \sin \alpha \leq r \times \frac{1}{r} \times \frac{r}{n} \times BM \sin \alpha$$

$$\rightarrow wAB \leq rBM$$

$$\frac{AB}{BM} = \frac{r}{w} \rightarrow \frac{BM}{AM} \leq \left\lceil \frac{w}{r} \right\rceil$$

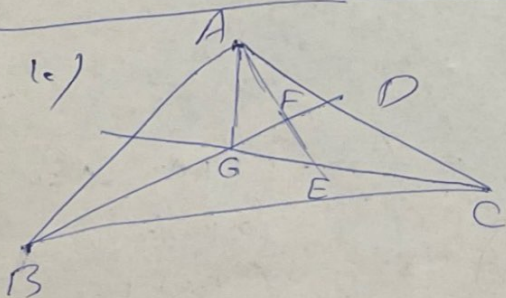


$$r_y \leq \varepsilon n + y \rightarrow r_y \leq \varepsilon n \rightarrow y \leq \frac{\varepsilon}{r} n$$

$$n + y \leq 1 \rightarrow n + \frac{\varepsilon}{r} n \leq 1 \rightarrow \frac{r + \varepsilon}{r} n \leq 1 \rightarrow n \leq \frac{r}{r + \varepsilon}$$

$$S \leq 145 = 14 \times \frac{14}{r} \leq \left\lceil \frac{1}{r} \right\rceil$$

$$y \leq \frac{\varepsilon}{r}$$



$$GB \leq \frac{1}{r} BD$$

$$FD \leq \frac{1}{r} GD \rightarrow FD \leq \frac{1}{r} \times \frac{1}{r} BD$$

$$\rightarrow 9 FD \leq BD \rightarrow \frac{BD}{FD} \leq 9$$