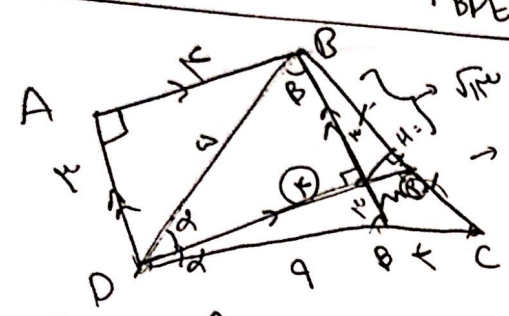


$$\frac{S_{BDE}}{S_{ADE}} = \frac{1}{1} \Rightarrow \frac{1/4}{1/4} = 1$$

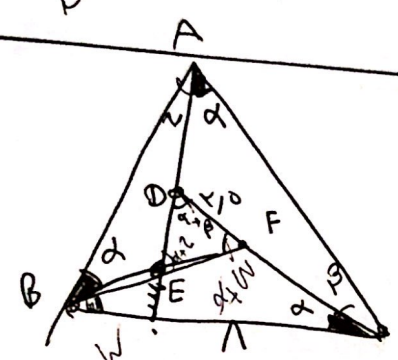
$$\frac{S_{BEC}}{S_{BDE}} = \frac{1/4}{1/4} = 1 \Rightarrow \frac{1/4}{1/4} = 1$$

$$\frac{S_{BDE} + S_{BEC}}{S_{ABC}} = \frac{1/4 + 1/4}{1} = \frac{1}{2}$$



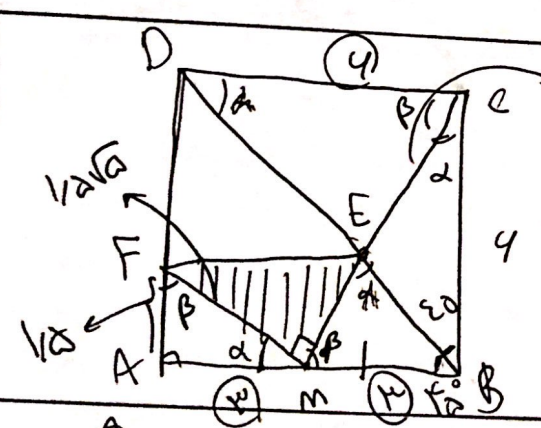
$$r = \sqrt{13} \times MH$$

$$\frac{9 \times \sqrt{13}}{13} = MH$$



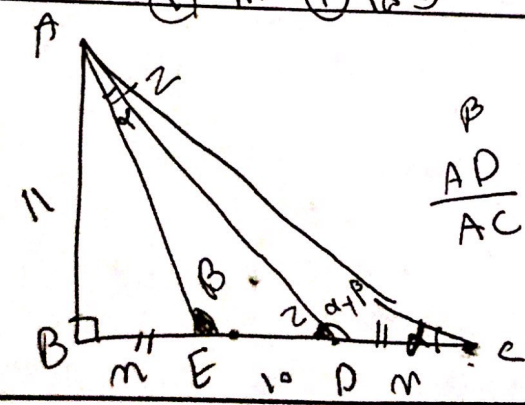
$$AB = ?$$

$$\frac{DF}{BC} = \frac{EF}{AB} \Rightarrow \frac{1/4}{1} = \frac{1/4}{1} \Rightarrow \frac{1}{4} = \frac{1}{4}$$



$$\frac{EM}{EC} = \frac{1}{1} \Rightarrow \frac{1}{1} = \frac{1}{1} \Rightarrow \frac{1}{1} = \frac{1}{1}$$

$$\frac{1/4 \times \sqrt{2} \times \sqrt{2}}{2} = \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$$



$$\frac{AD}{AC} = \frac{1}{1} = \frac{AE}{10+n} \Rightarrow (AE)^2 = 1 \cdot (1+n)$$

$$AE = \sqrt{1+n}$$

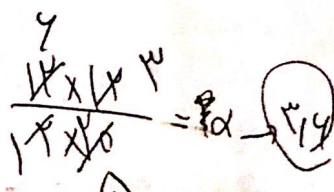
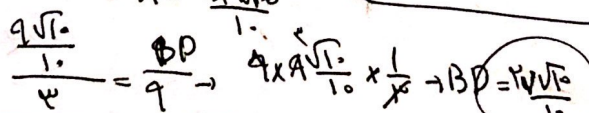
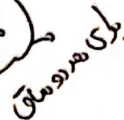
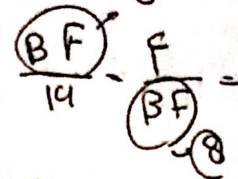
$$10 + 1 \cdot n = 11 + n$$

$$n = 7$$

$$n = 3$$

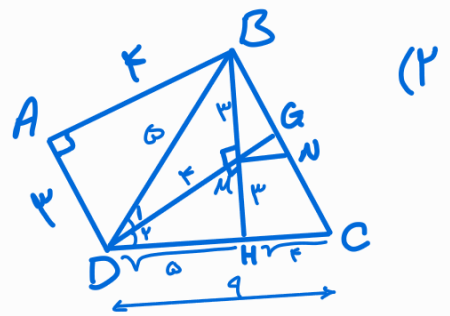
$$n^2 - 10n + 11 = 0$$

$$(n-3)(n-7) = 0$$



$$\frac{1 \wedge L^0}{1 \wedge} \quad \frac{1 \wedge}{1 \wedge}$$

$\hat{D}_1 = \hat{D}_2 = \hat{D}_3 \leftarrow DMH$ ، BDM هم نهشت هسند
 در مثلث BMC ، BMN با نسبت ۲ معشابه اند پس $MC = \frac{1}{2} HC$ است
 بنابراین فاصله M از وسط ضلع BC برابر ۲ است

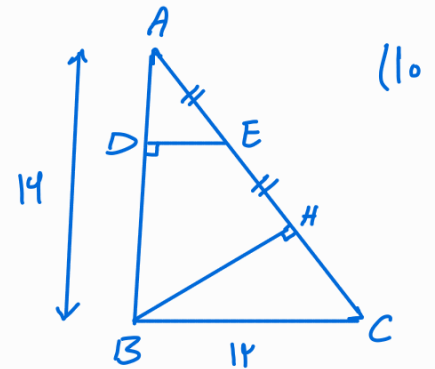


$$AB^2 + BC^2 = AC^2 \rightarrow AC = 10$$

$$\triangle ADE \sim \triangle ABH \rightarrow \begin{cases} \hat{A} = \hat{A} \\ \hat{D} = \hat{H} = 90^\circ \end{cases} \rightarrow \frac{DE}{BH} = \frac{AE}{14} \quad (1)$$

$$S_{\triangle ABC} = \frac{AB \times BC}{2} = \frac{BH \times AC}{2} \rightarrow BH = 9,4$$

$$\triangle ABC \rightarrow 14^2 = AH \times 10 \rightarrow AH = 12,1 \rightarrow AE = \frac{AH}{2} = 4,6$$



$$\xrightarrow{(1)} \frac{DE}{BH} = \frac{AE}{14} = \frac{DE}{9,4} = \frac{4,6}{14} \rightarrow DE = 3,16$$