

$$\log_n m = a$$

$$n^a = m$$

$$\log_{mn} m^r n = b$$

a)

[b] = ?

$$b = \log_{n^a \times n} n^{ra} = \log_{n^{a+1}} n^{ra+1} \rightarrow \frac{ra+1}{a+1} \log_n n \rightarrow b = \left[\frac{a+1+1}{a+1} \right]$$

$$y = \sqrt{\frac{a}{\log \frac{a}{r}}}$$

$$\log \frac{a}{r} \neq 0 \rightarrow a \neq r \quad D_f = (0, \infty)$$

$$\frac{0}{+} + \frac{1}{-}$$

$$y = \frac{\log^{(ar-a-r)}}{\sqrt{m^r-1} + 1}$$

$$m^r - a - r \neq 0$$

$$\alpha = r$$

$$m^r - r \rightarrow m^r > 1 \rightarrow m > 1$$

$$m^r - 1 \neq -1 \checkmark$$

$$\Rightarrow D_f = (-\infty, -1) \cup (1, \infty)$$

$$r \log_a^a + \log_a^r = r \quad a = 9 \quad a = ?$$

$$r \log_a^a + \frac{1}{r} \log_a^a = r \rightarrow r \log_a^a + r \log_a^a = r \rightarrow \log_a^a = \frac{1}{r}$$

$$a = \sqrt{9} = 3 \quad a = a^{\frac{1}{r}} = \sqrt{a}$$

$$\log^r = r^r \quad \log^r = r^r \quad (r \log^a)^{ar} + (\log^r)^a - \log^a = 0$$

$$(\log^a - \log^r)^{ar} + (r \log^r)^a - (\log^r + \log^a) = 0$$

$$\frac{c}{a} = \frac{-\log^r - \log^a}{\log^a - \log^r} = \frac{-\log^r - \log^1 + \log^r}{\log^1 - \log^r - \log^r} = \frac{-1/r}{1/r} = -1$$

$$a - m = 1 - (-1) = \frac{1}{r}$$

$$\log_r^v = r/a \quad \log_r^r = r/a \quad \log_{1/r}^1 = r$$

$$\log_a^r \times \log_r^v = r/a \times r/a \rightarrow \log_a^v = 1/r$$

$$\log_{1/r}^1 = \frac{\log_{1/a}^1}{\log_{1/r}^1}$$

$$\log_{1/r}^1 = \frac{\log_a^r + \log_a^a}{\log_r^r + \log_r^v} = \frac{1/a + 1}{r/a + r} = \frac{1/a}{1/a}$$

$$\log_{1/r}^a = 1/a \quad \log_r^r = 1/r \quad \log_{1/a}^r = r$$

$$\log_{1/r}^a \times \log_r^r = \log_{1/r}^a = r/a$$

$$\log_{1/a}^r = \frac{\log_r^r}{\log_{1/a}^1} = \frac{\log_r^r + \log_r^r}{\log_r^r + \log_r^v} = \frac{r/r}{r/r + r/a} = \frac{1}{1 + ra} = \frac{1}{1+a}$$

Date

$$\log_{\lambda} \lambda = m$$

$$\log_{\lambda} \lambda = 1$$

$$\log_{\lambda} \lambda^r = \frac{\log_{\lambda} \lambda^r}{\log_{\lambda} \lambda}$$

$$\rightarrow \log_{\lambda} \lambda^r = \log_{\lambda} \lambda + \log_{\lambda} \lambda^r = \frac{r}{\lambda} + \frac{1}{\lambda} \log_{\lambda} \lambda^r$$

$$\log_{\lambda} \lambda = m \rightarrow \log_{\lambda} \lambda + \log_{\lambda} \lambda = m$$

$$\rightarrow \frac{r}{\lambda} \log_{\lambda} \lambda + \frac{1}{\lambda} \log_{\lambda} \lambda = m \rightarrow \frac{r}{\lambda} \log_{\lambda} \lambda + \frac{1}{\lambda} = m$$

$$\log_{\lambda} \lambda = \frac{r(m-1)}{r}$$

$$\log_{\lambda} \lambda = \frac{\frac{r}{\lambda} + \frac{1}{\lambda} \log_{\lambda} \lambda}{\frac{r}{\lambda}} = \frac{\frac{r}{\lambda} + \frac{1}{\lambda} \left(\frac{r(m-1)}{r} \right)}{\frac{r}{\lambda}} = \frac{r + r(m-1)}{r}$$

$$\log_{\lambda} \lambda^{r+1}$$

$$= \frac{\log_{\lambda} \lambda^{r+1}}{\log_{\lambda} \lambda} = \left(\frac{\lambda}{\lambda} \right)^{r+1}$$

$$\left(\frac{\lambda}{\lambda} \right)^{r+1} = \left(\frac{\lambda}{\lambda} \right)^{r+1} \rightarrow \left(\frac{\lambda}{\lambda} \right)^{r+1} = \left(\frac{\lambda}{\lambda} \right)^{r+1} \rightarrow r+1 = \frac{r+1}{\lambda}$$

$$r+1 + r - 1 = 0 \rightarrow r+1 + r - r = 0 \rightarrow r = -1 \text{ (not possible)}$$

$$\log_{\lambda} \lambda^{r+1} = \log_{\lambda} \lambda^r = \frac{r}{\lambda} \log_{\lambda} \lambda = \frac{r}{\lambda} \cdot 1 = \frac{r}{\lambda}$$

$$\log_{\lambda} \lambda = a$$

$$\log_{\lambda} \lambda = \frac{r}{\lambda} (1+a) \log_{\lambda} (\lambda - 1) = 1$$

$$\log_{\lambda} \lambda = \frac{1}{\lambda} \log_{\lambda} \lambda = \frac{r}{\lambda} (1+a) \rightarrow \log_{\lambda} \lambda = r + ra$$

$$\lambda^r \times \lambda^{ra} = \lambda \rightarrow \lambda^r \times \lambda^{ra} = \lambda^1 = \lambda$$

$$\log_{\lambda} (\lambda^r \times \lambda^{ra}) = \log_{\lambda} \lambda = 1$$

$$-ra + b + \frac{1}{\lambda} = 0 \rightarrow S = \frac{-b}{-ra} = \frac{b}{ra} = \log_{\lambda} \lambda$$

$$\frac{a}{b} = \frac{\log_{\lambda} \lambda}{\lambda} = \frac{r \log_{\lambda} \lambda}{\lambda}$$

$$ra = b + c \rightarrow \frac{ra}{b} = 1 + \frac{c}{b} \rightarrow r \left(\frac{\log_{\lambda} \lambda}{\lambda} \right) = 1 + \frac{c}{b}$$

$$\frac{c}{b} = -1 + \log_{\lambda} \lambda \rightarrow \frac{c}{a} = \frac{-1 + \log_{\lambda} \lambda}{\log_{\lambda} \lambda} \Rightarrow \frac{c}{a} = \frac{\log_{\lambda} \lambda - \log_{\lambda} 1}{\log_{\lambda} \lambda}$$

$$= \frac{\log_{\lambda} \lambda}{\log_{\lambda} \lambda} = \log_{\lambda} \frac{\lambda}{1} \rightarrow \left(\frac{\lambda}{1} \right)^{\frac{1}{\lambda}} = \sqrt[\lambda]{\lambda}$$