



$$2x \times 2x \times \frac{\sin 150^\circ}{1} = 84 \rightarrow 4x^2 = 84 \rightarrow x^2 = 21 \rightarrow x = 3\sqrt{2}$$

$$2(2x + 2x) = 10x \rightarrow \boxed{\text{محیط} = 30\sqrt{2}}$$

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$$\frac{1}{4} \times 16 \times \sin \hat{A} - \frac{1}{4} \times 2 \times 2 \times \sin \hat{A} = \frac{1}{4} \rightarrow \frac{1}{4} \times \sin \hat{A} \left(\frac{16}{4} \right) = \frac{1}{4} \rightarrow \boxed{\sin \hat{A} = \frac{1}{4}}$$



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$$\frac{|\sin \alpha|}{\cos \alpha} = -\tan \alpha \rightarrow \sin \alpha < 0 \text{ و } \frac{1}{|\cos \alpha|} \frac{\sin \alpha}{\cos \alpha} = \frac{1 + \sin \alpha}{|\cos \alpha|}$$

$$\boxed{\alpha \text{ در ربع سوم قرار دارد.}} \leftarrow \cos \alpha > 0$$

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$$\tan\left(\frac{\pi}{4} - \alpha\right) = \cot \alpha \text{ و } \tan \alpha = \frac{-1/8}{2} = \frac{-1}{4} \rightarrow \boxed{\cot \alpha = \frac{-4}{1}}$$

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$$\alpha = 22^\circ \rightarrow \frac{3 \cos\left(\frac{3\pi}{4} - \alpha\right) - 2 \sin(\pi - \alpha)}{\sin(\pi + \alpha) - \cos\left(\frac{3\pi}{4} + \alpha\right)} = \frac{-3 \sin \alpha - 2 \sin \alpha}{-\sin \alpha - \sin \alpha} =$$

$$\frac{-5 \sin \alpha}{-2 \sin \alpha} = \boxed{\frac{5}{2}}$$

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$$\frac{\cos \alpha + \sin \alpha}{|\tan^2 \alpha - 1|} \rightarrow \cos \alpha = \frac{r}{r} \rightarrow \begin{array}{c} r \\ \swarrow \searrow \\ \sqrt{a} \quad \sqrt{a} \\ \downarrow \quad \downarrow \\ \sqrt{a} \quad \sqrt{a} \\ \downarrow \quad \downarrow \\ \sqrt{a} \quad \sqrt{a} \end{array} \rightarrow \frac{\frac{r}{r} + \frac{-\sqrt{a}}{r}}{\frac{1}{r}} = \boxed{\frac{r(r-\sqrt{a})}{r}}$$

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$$\sin \alpha = r \cos \alpha \rightarrow \cos^2 \alpha + r \cos^2 \alpha = 1 \rightarrow 2 \cos^2 \alpha = 1 \rightarrow \cos^2 \alpha = \frac{1}{2}$$

$$|\cos \alpha| = \frac{\sqrt{a}}{a} \rightarrow \boxed{\cos \alpha = -\frac{\sqrt{a}}{a}}$$

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$$\frac{-r m}{m^2 - 1} = \sqrt{r} \rightarrow \sqrt{r} m^2 + r m - \sqrt{r} = 0 \rightarrow m^2 + r m - r = 0$$

$$(m+r)(m-1) = 0 \rightarrow \begin{cases} m = \frac{\sqrt{r}}{r} \\ m = -\sqrt{r} \end{cases}$$

$$\boxed{\frac{\sqrt{r}}{r} \oplus \frac{r\sqrt{r}}{r} = \frac{r\sqrt{r}}{r}}$$

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$$-\frac{\pi}{r} < \alpha < \frac{\pi}{r} \rightarrow -\frac{\pi}{r} < -\alpha < \frac{\pi}{r}, \quad 0 < \alpha + \frac{\pi}{r} < \frac{\pi}{r}$$

$$0 < \tan \theta \rightarrow \frac{1-m}{r+m} > 0 \rightarrow \frac{-r}{\frac{r}{r} + \frac{1}{r}} \rightarrow \boxed{m \in (-r, 1)}$$

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$$\underbrace{-\sqrt{r} \times -\frac{\sqrt{r}}{r}}_{+\frac{r}{r}} + \underbrace{-\sqrt{r} \times \frac{\sqrt{r}}{r}}_{-\frac{r}{r}} = \boxed{0}$$

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