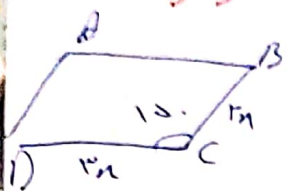


مسئله ۲۰

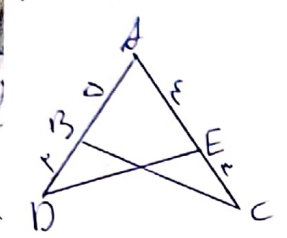
$$\frac{DC}{BC} = \frac{r}{r} \Rightarrow \alpha \text{ و } \beta \text{ را پیدا کن!}$$

۲۰

مسئله ۲۰ سوال ۱



مسئله ۲۰ سوال ۱
 $S_{\triangle ABC} = \frac{1}{2} r \cdot r \cdot \sin 120^\circ = \frac{1}{2} r^2 \cdot \frac{\sqrt{3}}{2} = \frac{\sqrt{3}}{4} r^2$
 $S_{\triangle ADE} = \frac{1}{2} r \cdot r \cdot \sin 60^\circ = \frac{1}{2} r^2 \cdot \frac{\sqrt{3}}{2} = \frac{\sqrt{3}}{4} r^2$
 $S_{ABCE} = S_{\triangle ABC} + S_{\triangle ADE} = \frac{\sqrt{3}}{2} r^2$

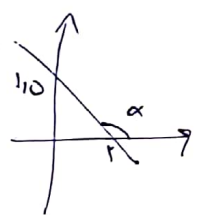


مسئله ۲۰ سوال ۲
 $\tan \hat{A} = ?$
 $S_{\triangle ABC} = \frac{1}{2} ab \sin A \rightarrow \frac{\sqrt{3}}{4} r^2 = \frac{1}{2} r \cdot r \cdot \sin A \Rightarrow \sin A = \frac{\sqrt{3}}{2}$
 $\sin A = \frac{\sqrt{3}}{2} \rightarrow A = 60^\circ \rightarrow \tan \hat{A} = \frac{\sqrt{3}}{1} = \sqrt{3}$

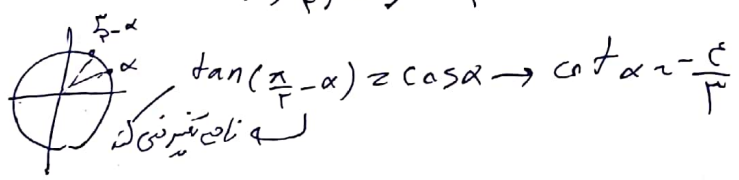
۱) $\frac{1}{\sqrt{\cos^2 \alpha}} - \tan \alpha = \frac{1 + \sin \alpha}{|\cos \alpha|}$
 ۲) $\frac{|\sin \alpha|}{\cos \alpha} = \frac{1}{\cot \alpha}$

۱) $\Rightarrow \frac{1}{|\cos \alpha|} - \frac{\sin \alpha}{\cos \alpha} = \frac{1 + \sin \alpha}{|\cos \alpha|} \rightarrow \frac{-\sin \alpha}{\cos \alpha} = \frac{\sin \alpha}{|\cos \alpha|} \rightarrow \cos \alpha < 0$ I
 I ∩ II \Rightarrow مورد ۱

۲) $\frac{|\sin \alpha|}{\cos \alpha} = \frac{-\sin \alpha}{\cos \alpha} \rightarrow \sin \alpha < 0$ II



مسئله ۲۰ سوال ۳
 $\tan(\frac{\pi}{4} - \alpha) = ?$
 $(r, 0) \rightarrow y = \tan x + \frac{\pi}{4} \rightarrow \tan \alpha + \frac{\pi}{4} = 0 \rightarrow \alpha = -\frac{\pi}{4}$
 $(0, \frac{\pi}{4}) \rightarrow y = \frac{\pi}{4}$
 $\Rightarrow y = \frac{-\pi}{4}x + \frac{\pi}{4}$




مسئله ۲۰ سوال ۵
 $\frac{r \cos(\pi - \alpha) - r \sin(10\pi)}{\sin(\pi - \alpha) - \cos(\pi - \alpha)} \Rightarrow \frac{r(\cos(\pi - \alpha) - \sin(10\pi))}{\sin(\pi - \alpha) - \cos(\pi - \alpha)} = \frac{-r \sin \pi - r \sin \pi}{-\sin \pi - \sin \pi}$

$\frac{-r \sin \pi}{-r \sin \pi} = \frac{0}{0}$

$$\frac{\sin(\frac{\pi}{r} + \alpha) - \sin(\alpha - \pi)}{|\tan^2 \alpha - 1|} \rightarrow +\sin(\pi - \alpha)$$

$$\frac{\cos \alpha + \sin \alpha}{|\tan^2 \alpha - 1|} =$$



$$\frac{\frac{r}{r} - \frac{\sqrt{5}}{r}}{\left|\frac{5}{r^2} - 1\right|} = \frac{r - \sqrt{5}}{r^2 - 5} = \frac{r - \sqrt{5}}{r^2 - 5}$$

سوال ۶: $\frac{r - \sqrt{5}}{r^2 - 5}$

$$\sin \alpha = r \cos \alpha$$

$$\sin^2 \alpha + \cos^2 \alpha = 1 \rightarrow \cos^2 \alpha = 1 - \sin^2 \alpha \rightarrow \cos^2 \alpha = 1 - r^2 \cos^2 \alpha \rightarrow |\cos \alpha| = \frac{1}{\sqrt{5}} \rightarrow \cos \alpha = \frac{1}{\sqrt{5}} = \frac{\sqrt{5}}{5}$$

سوال ۷: $\frac{\sqrt{5}}{5}$

$$r m x + (m^2 - 1) y = r$$

$$y = \frac{r m}{m^2 - 1} x + \frac{r}{m^2 - 1}$$


$$\frac{-r m}{m^2 - 1} = \tan \gamma \rightarrow \frac{-r m}{m^2 - 1} = \frac{-r}{m} \rightarrow \sqrt{r m^2 + r m - \sqrt{r}} = 0$$

$$m^2 + r m - r = 0 \rightarrow m^2 = 1 \rightarrow m = \pm 1$$

سوال ۸: $\frac{r}{m^2 - 1}$

$$\left| \frac{1}{\sqrt{r}} - \left(\frac{-r}{\sqrt{r}} \right) \right| = \frac{r}{\sqrt{r}} = \frac{r \sqrt{r}}{r}$$

$$\tan\left(\frac{\pi}{r} - u\right) = \frac{1 - m}{r + m} > -\frac{r}{r} < u < \frac{r}{r}$$

$$-\frac{r}{r} < u < \frac{r}{r} \rightarrow 0 < \frac{r}{r} - u$$


$$\tan\left(\frac{\pi}{r} - u\right) = \frac{1 - m}{r + m} > -\frac{r}{r} < u < \frac{r}{r}$$

$$\rightarrow m \in (-r, 1)$$

سوال ۹: $m \in (-r, 1)$

$$\tan(r_1) \cos(r_1) + \tan(r_2) \sin(r_2)$$

$$\tan(r_1) \cos(r_1) + \tan(r_1 + r_2) \sin(r_1 + r_2)$$

$$\left[(-\sqrt{r}) \times \left(\frac{-\sqrt{r}}{r} \right) + (-\sqrt{r}) \times \left(\frac{\sqrt{r}}{r} \right) = 0 \right]$$

سوال ۱۰: 0